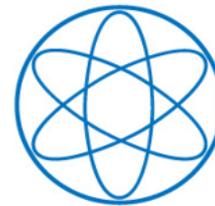


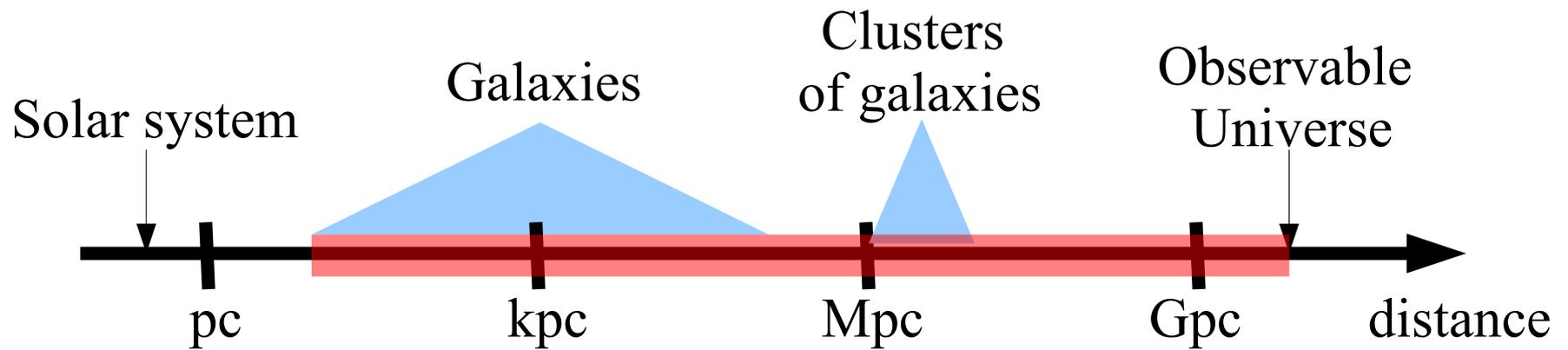
Particle Dark Matter

Alejandro Ibarra

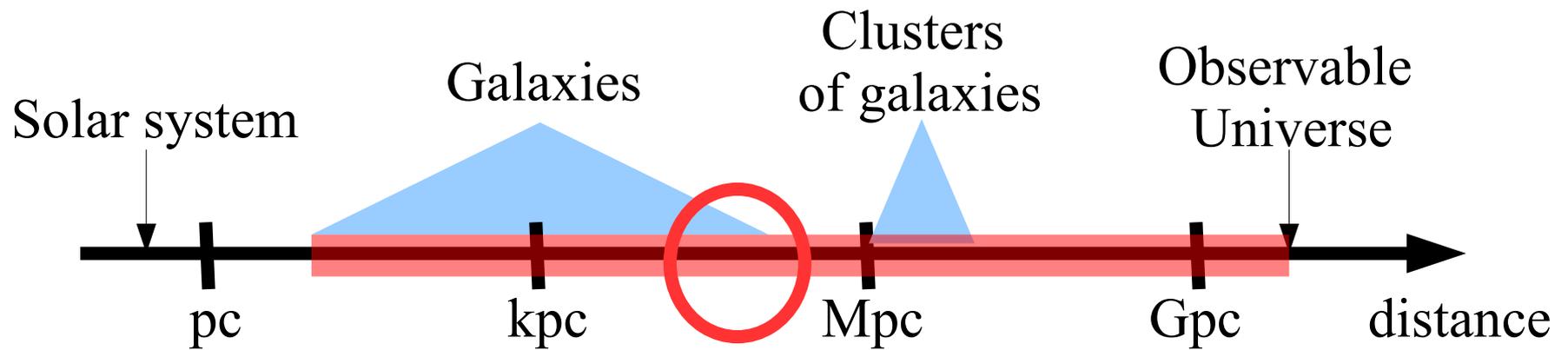


KMI/NITEP School 2026
Nagoya
March 2026

There is evidence for dark matter in a wide range of distance scales



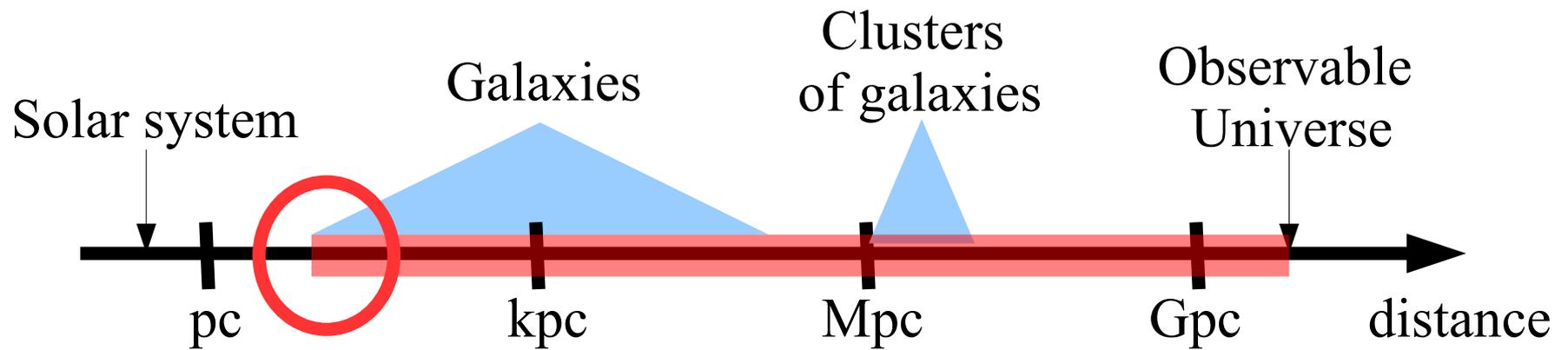
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M87

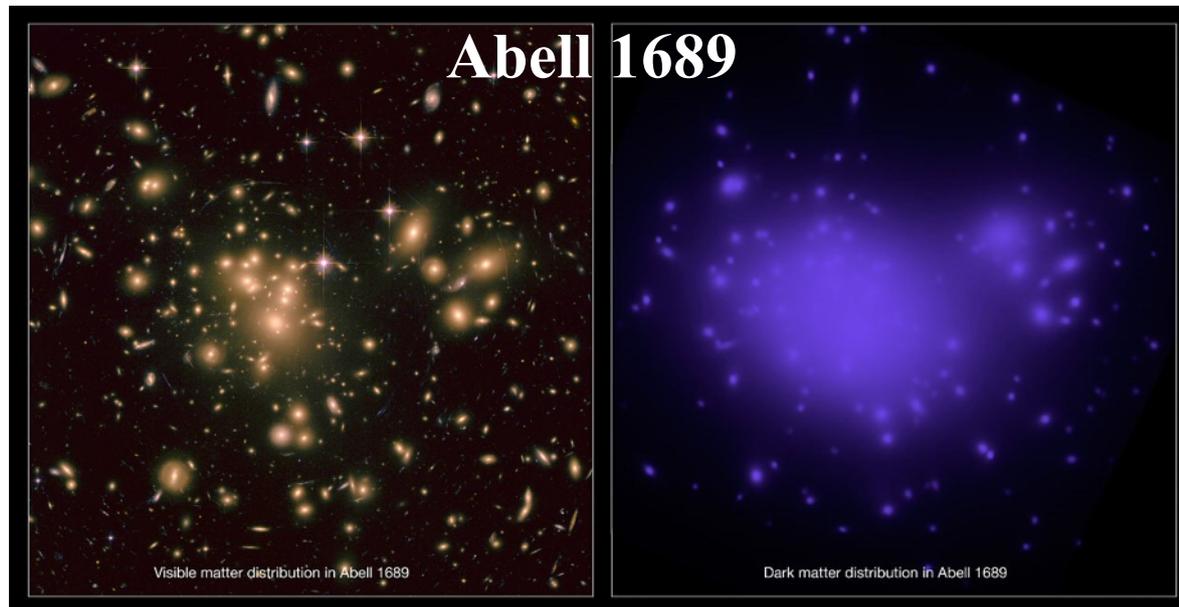
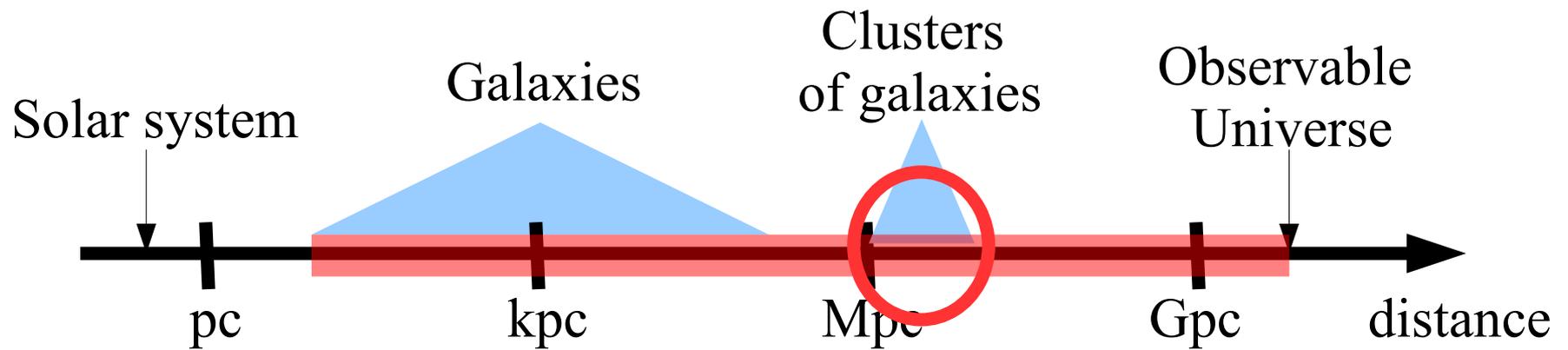


There is evidence for dark matter in a wide range of distance scales

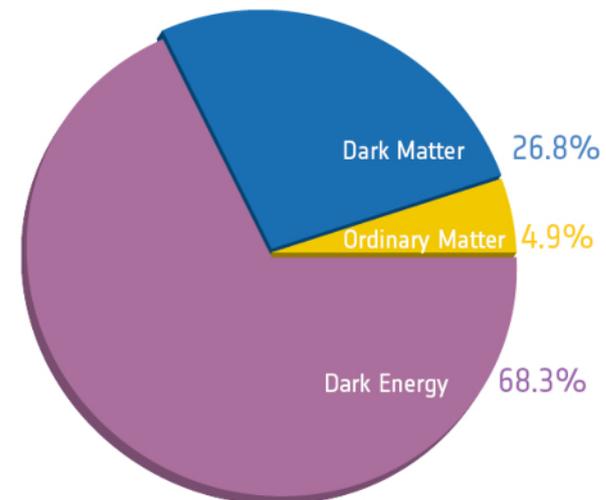
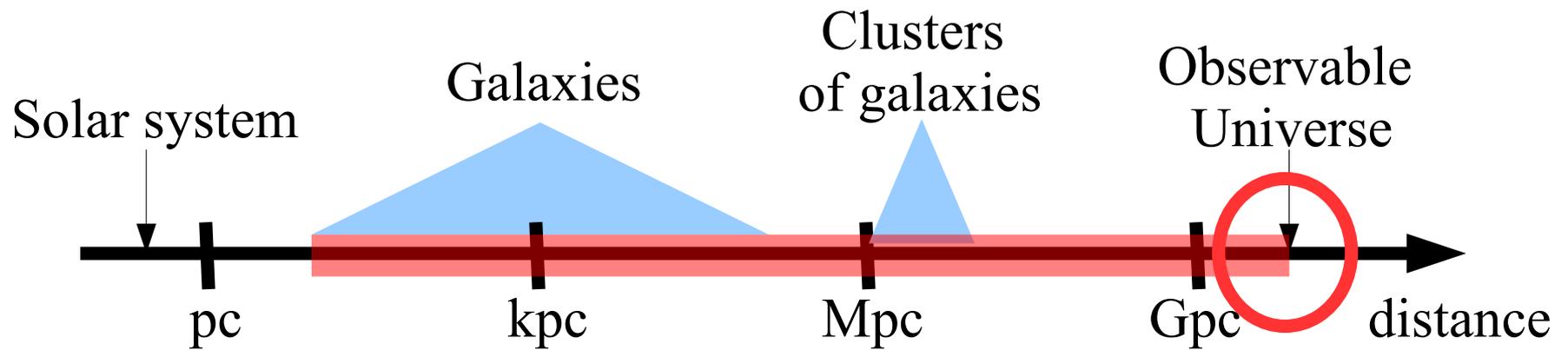


Segue 1

There is evidence for dark matter in a wide range of distance scales

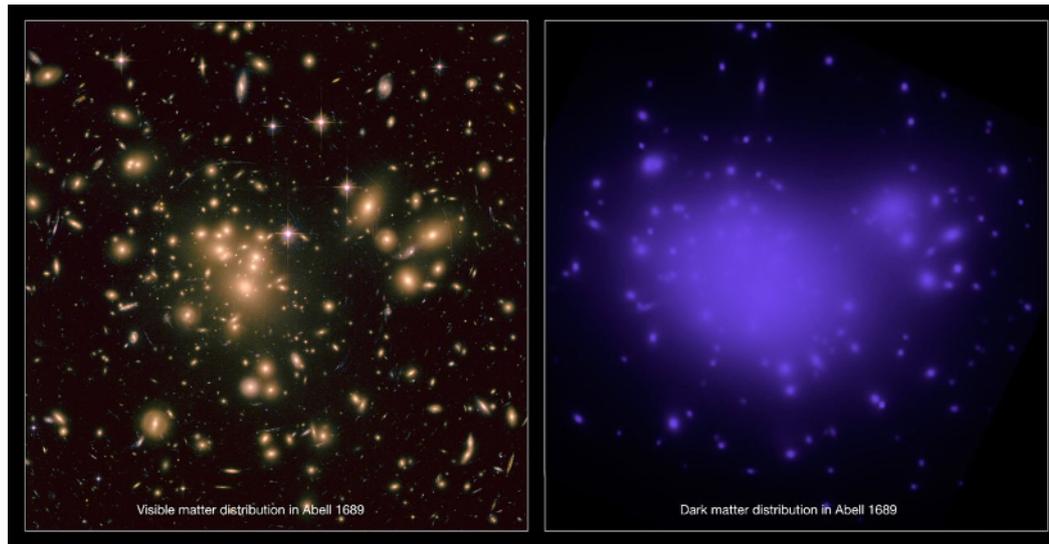


There is evidence for dark matter in a wide range of distance scales

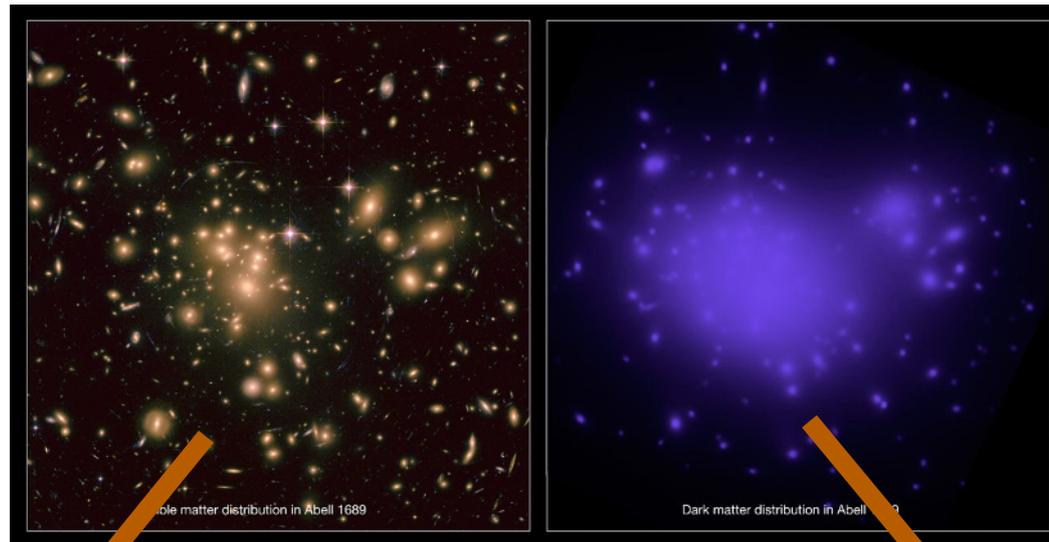


**What is dark matter
made of?**

What is dark matter made of?



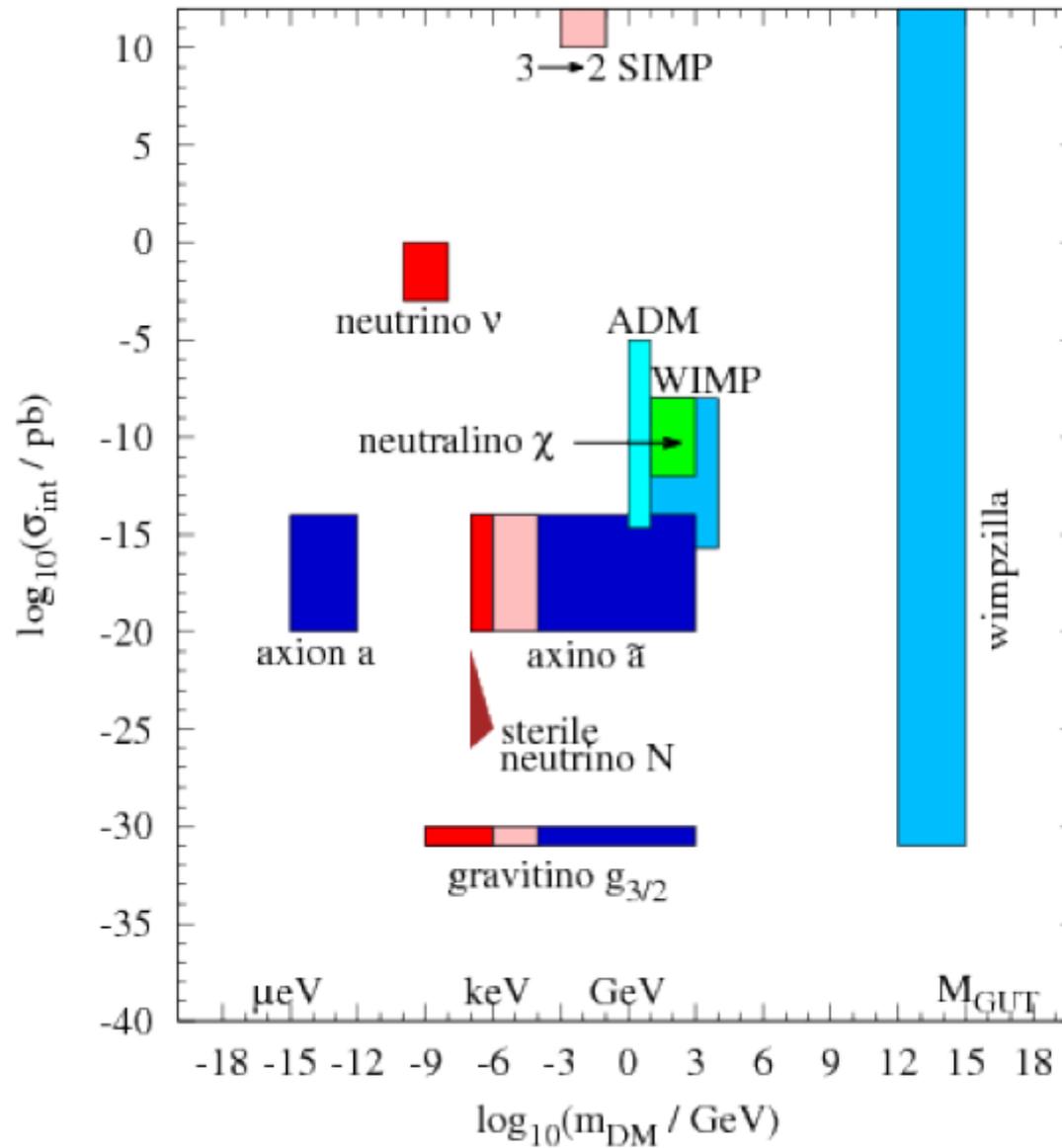
What is dark matter made of?



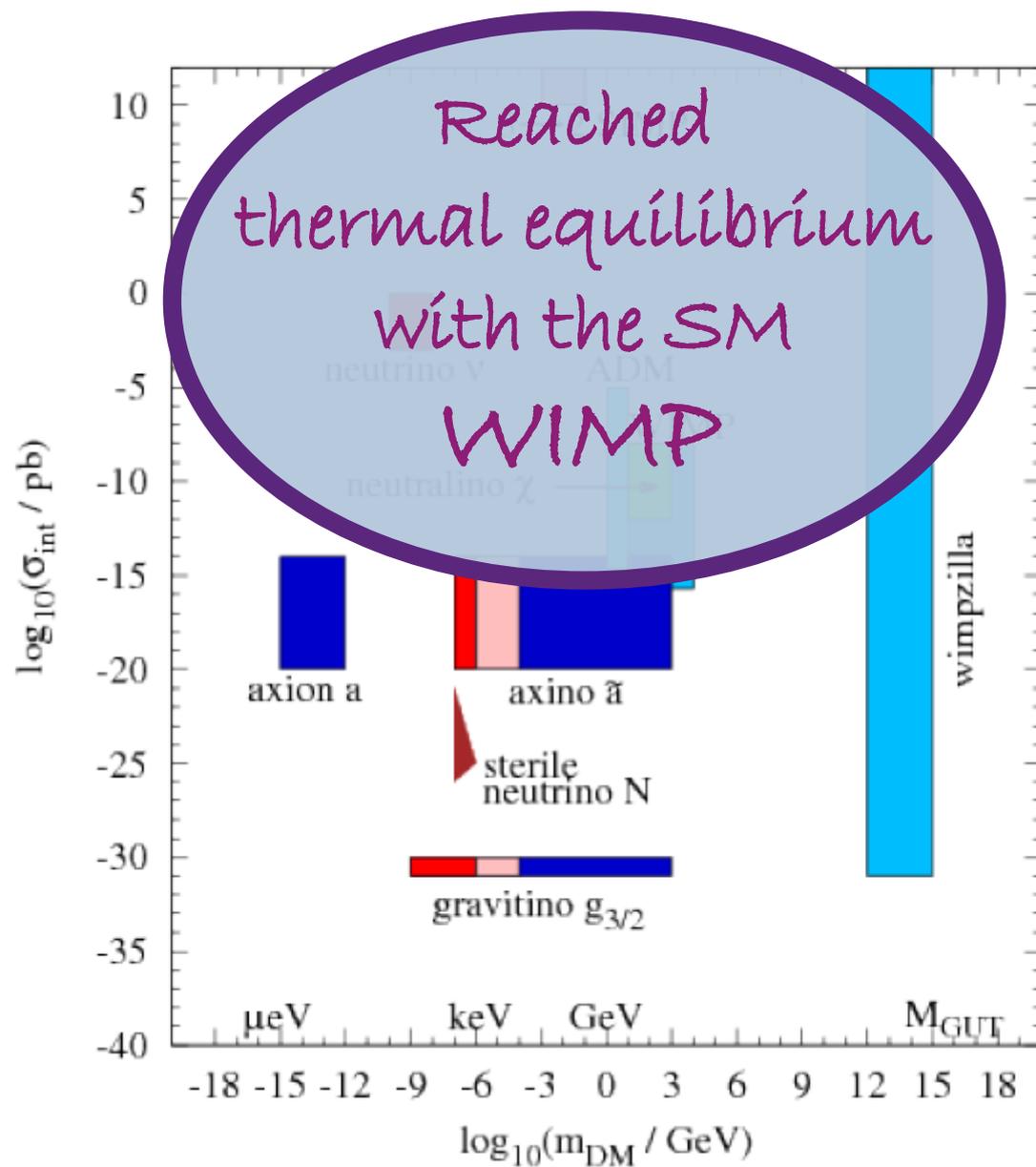
		Generation		
		I	II	III
FORCE CARRIERS	PHOTON Electromagnetism	0	0	0
	GLUON Strong force	0	0	0
	W Weak force	0	0	0
	Z Weak force	0	0	0
	HIGGS	0	0	0
		~125,000		
QUARKS	Up	+2/3	+2/3	+2/3
	Down	-1/3	-1/3	-1/3
	Charm	+2/3	+2/3	+2/3
	Strange	-1/3	-1/3	-1/3
	Top	+2/3	+2/3	+2/3
	Bottom	-1/3	-1/3	-1/3
	Electron Neutrino	0	0	0
	Muon Neutrino	0	0	0
	Tau Neutrino	0	0	0
LEPTONS	Electron	-1	-1	-1
	Muon	-1	-1	-1
	Tau	-1	-1	-1
	0.511	105.7	1,776.8	
BOSONS		FERMIONS		

Hypothesis:
Elementary particles,
interacting very weakly
with the Standard Model.

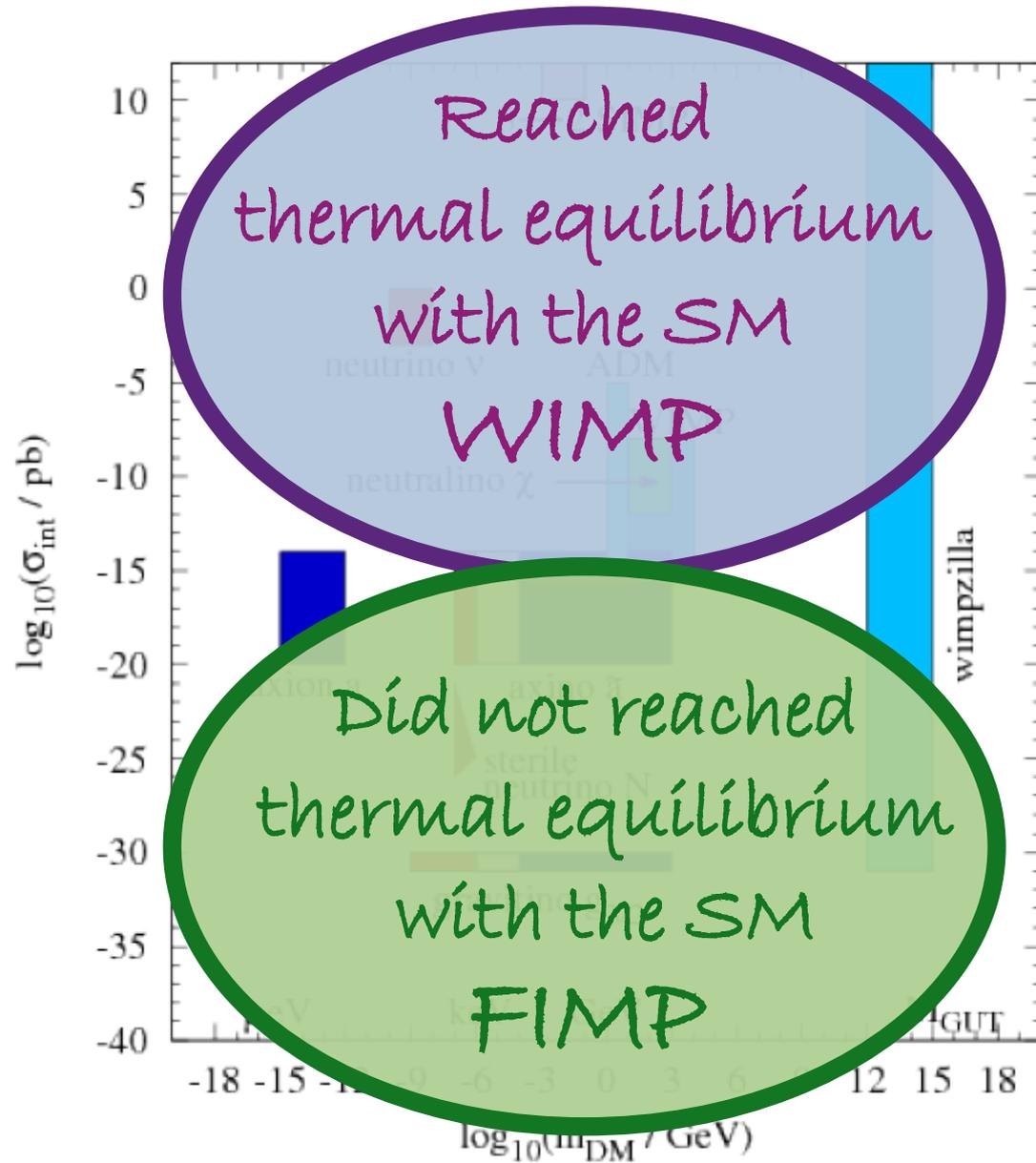
The dark particle zoo



The dark particle zoo



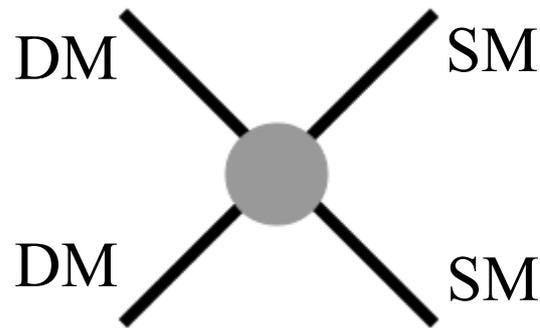
The dark particle zoo



WIMP history (in a nutshell)

Main assumptions on dark matter WIMPs:

- 1) The WIMP is stable in cosmological timescales.
- 2) WIMPs interact in pairs with the Standard Model particles



- 3) The WIMP interaction strength is *large enough* to keep the DM particles in thermal equilibrium with the SM plasma at very high temperatures.
- 4) The WIMP interaction strength is *small enough* to allow DM particles to chemically decouple from the SM plasma sufficiently early.

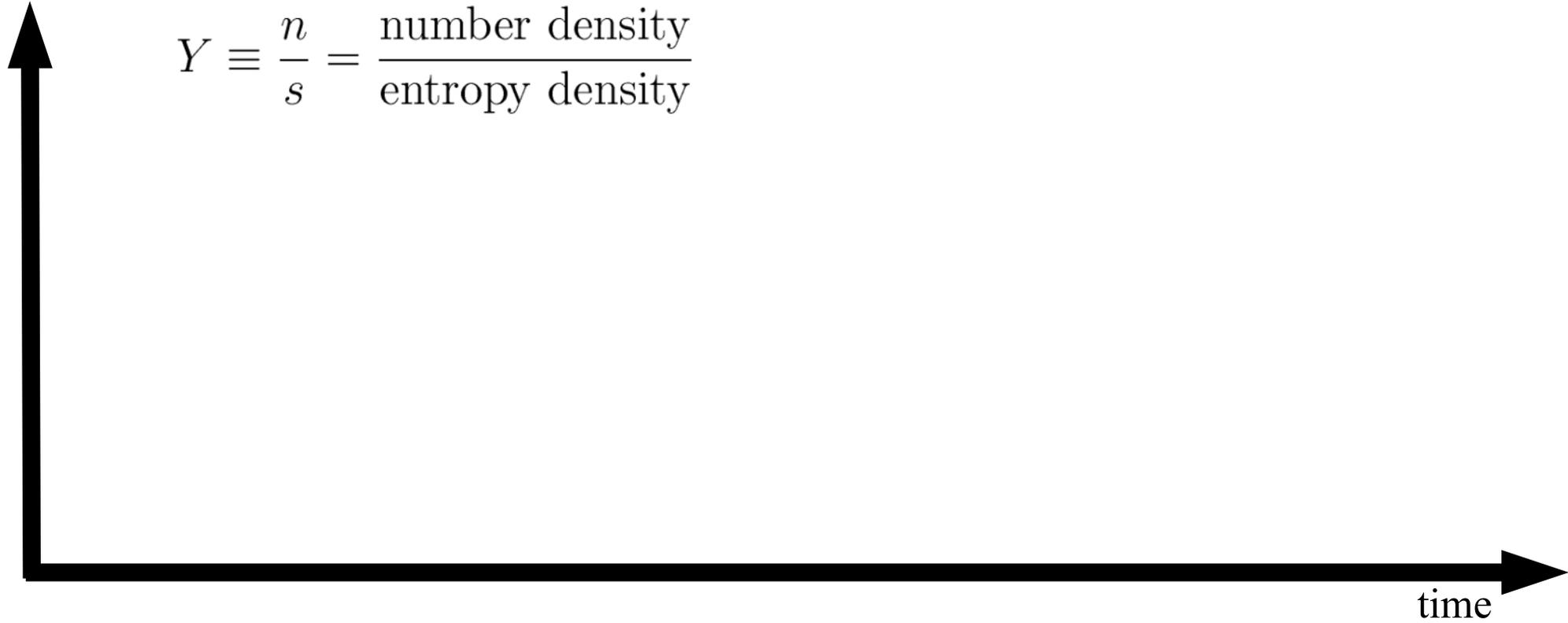
WIMP history (in a nutshell)



WIMP history (in a nutshell)

“yield” = number density of DM particles per comoving volume

$$Y \equiv \frac{n}{s} = \frac{\text{number density}}{\text{entropy density}}$$



WIMP history (in a nutshell)

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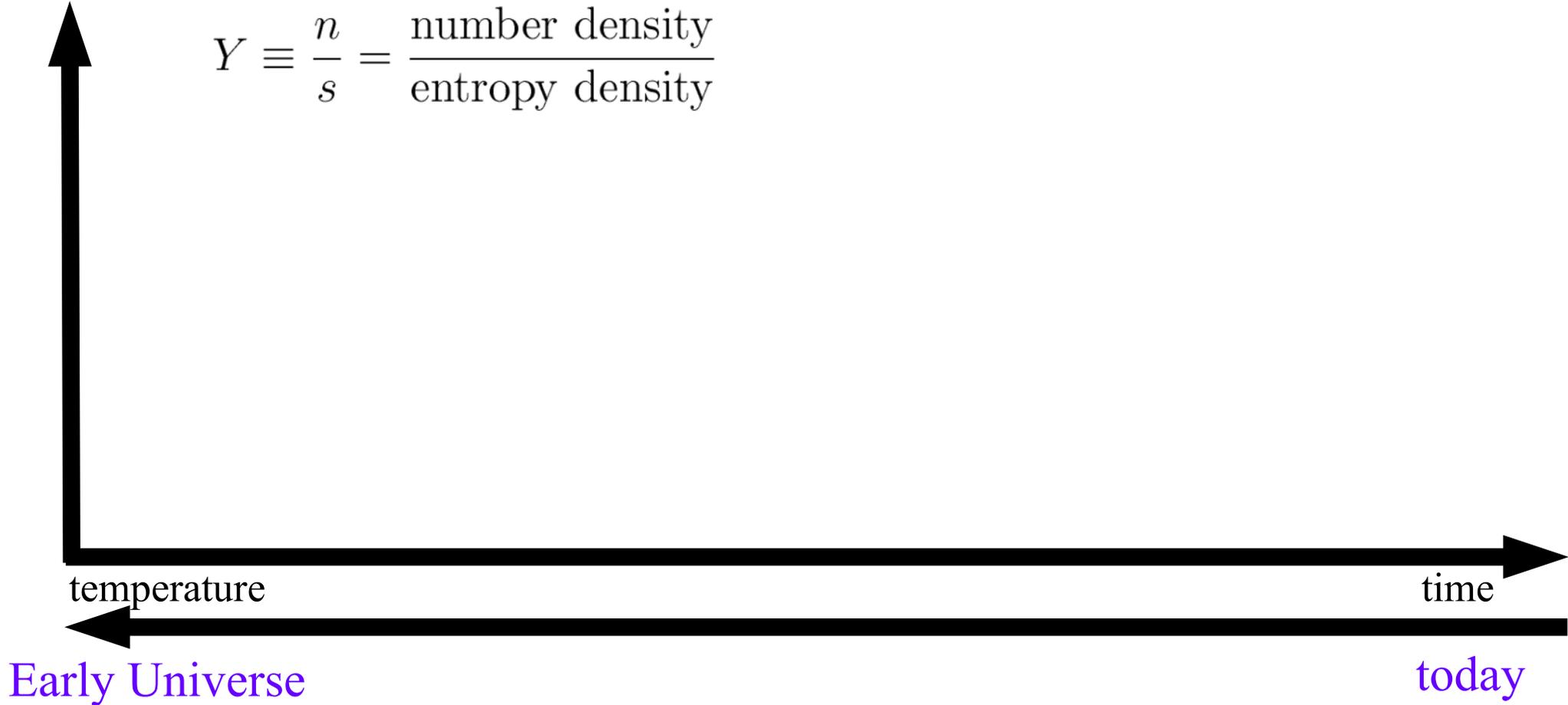
temperature

time

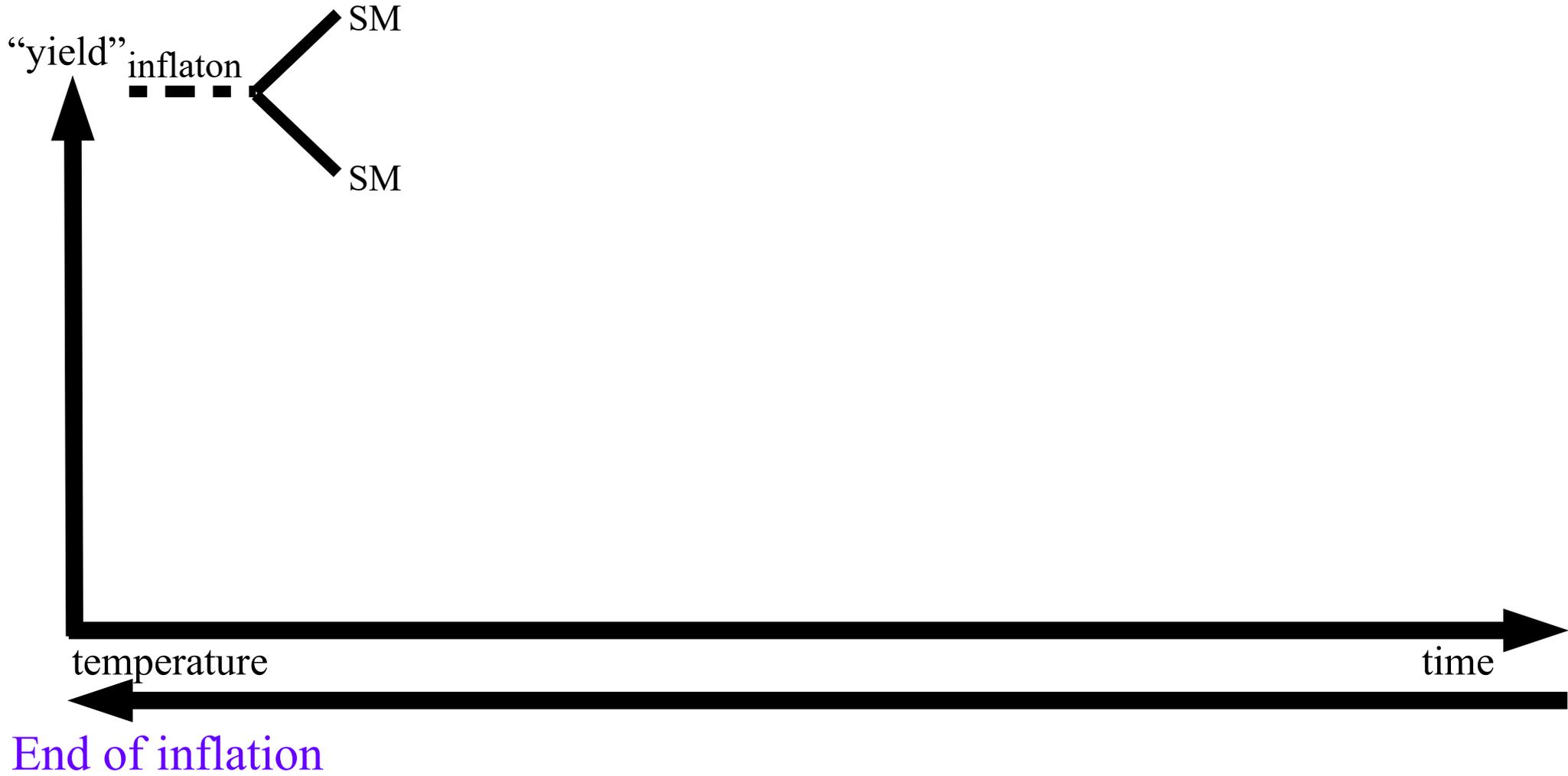
WIMP history (in a nutshell)

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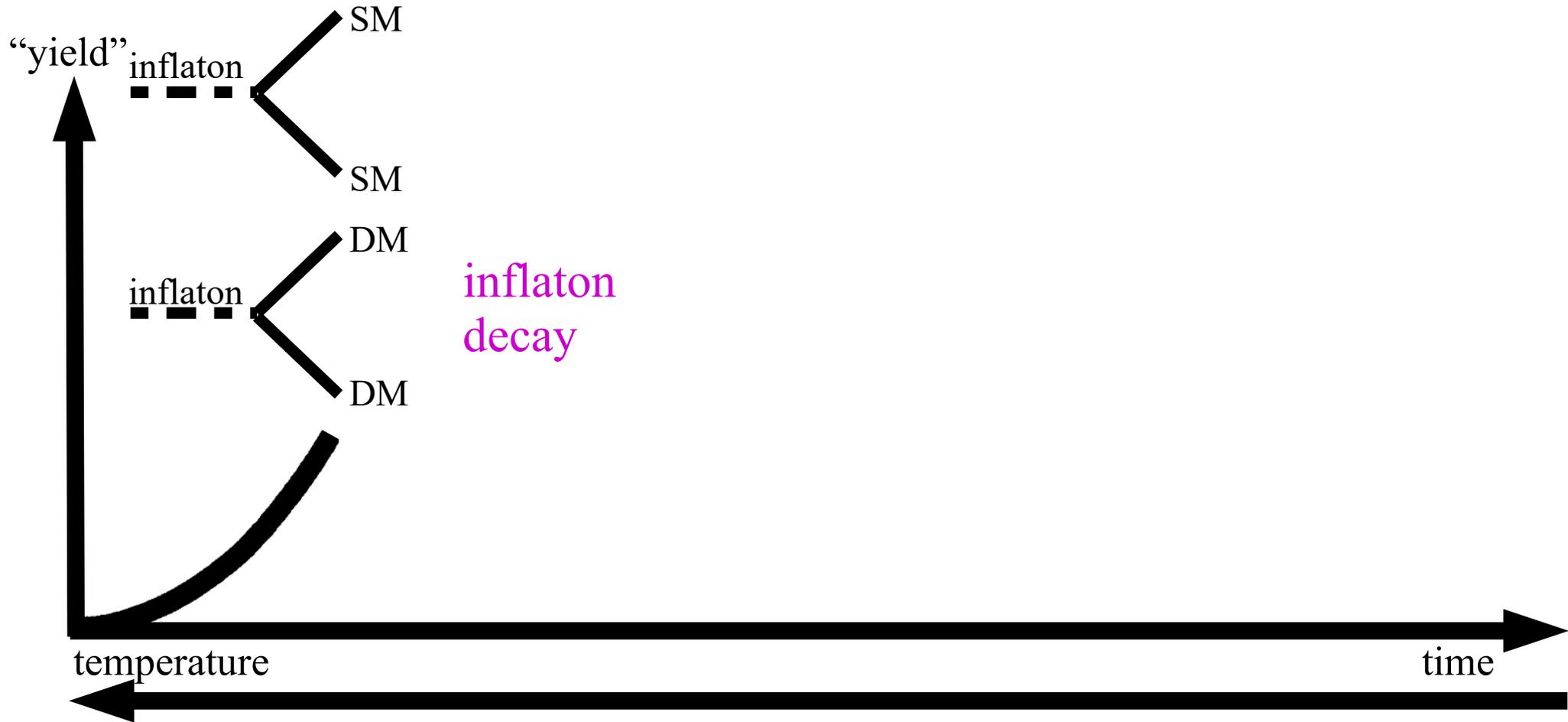
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WIMP history (in a nutshell)



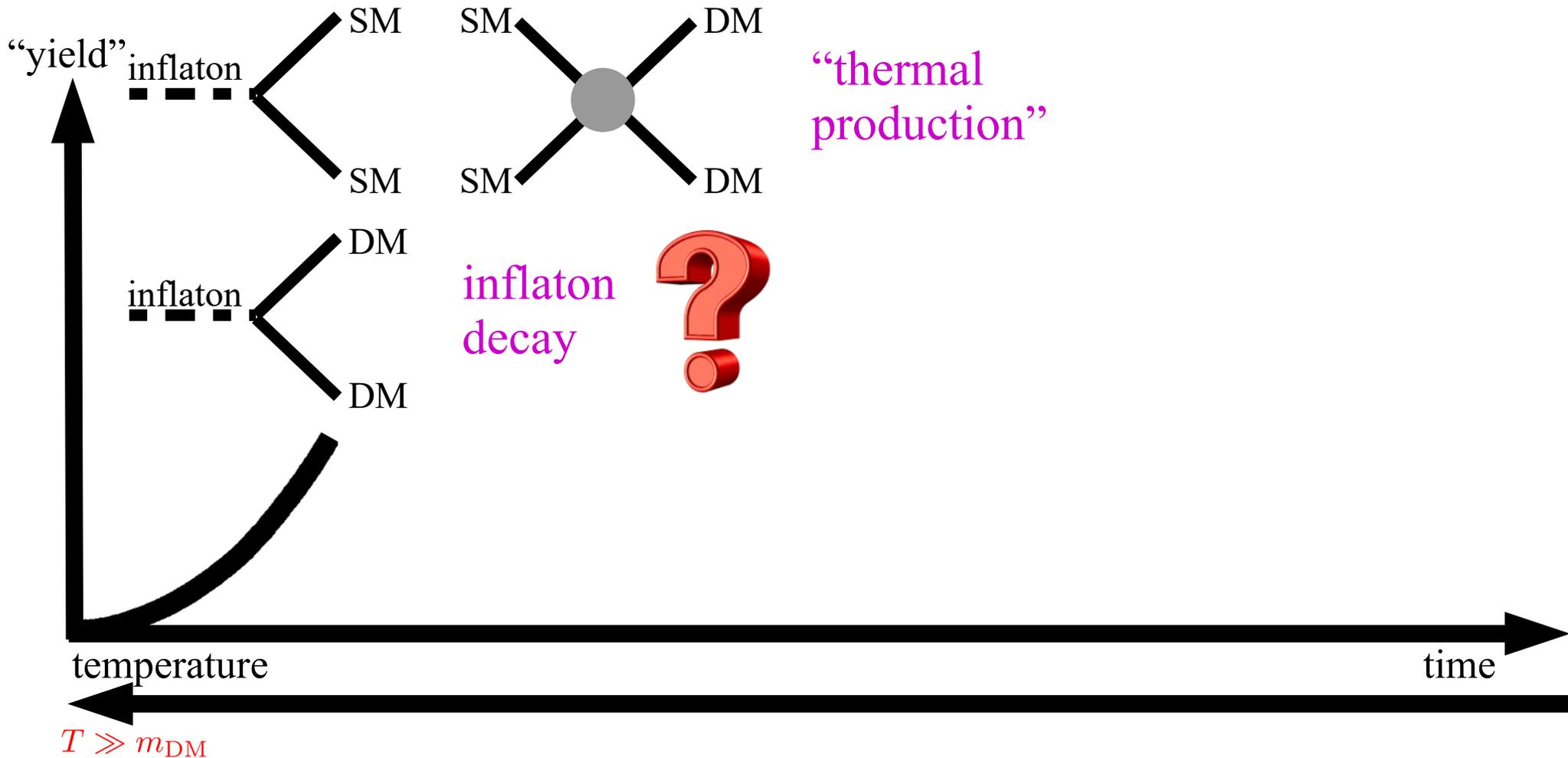
WIMP history (in a nutshell)



WIMP history (in a nutshell)

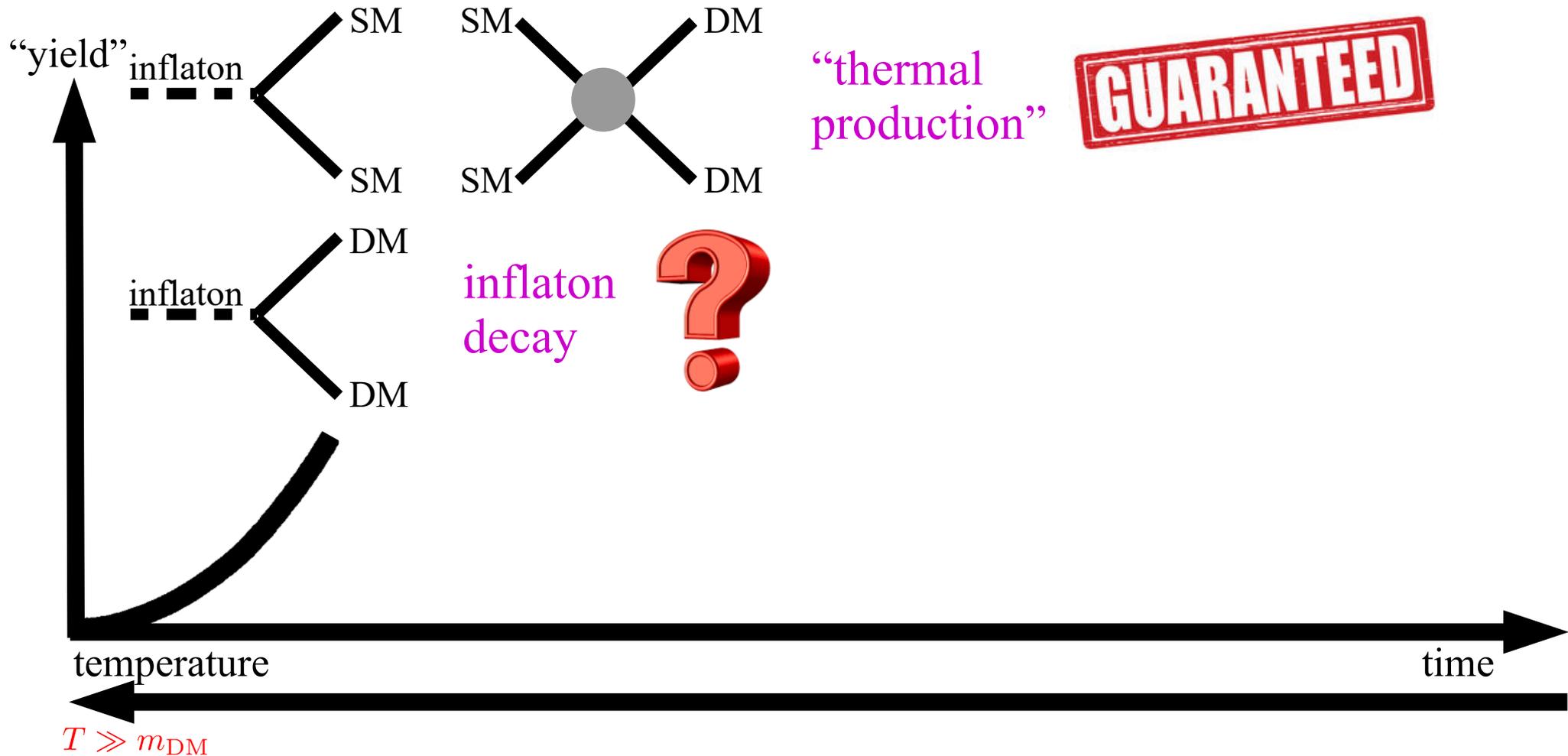


WIMP history (in a nutshell)



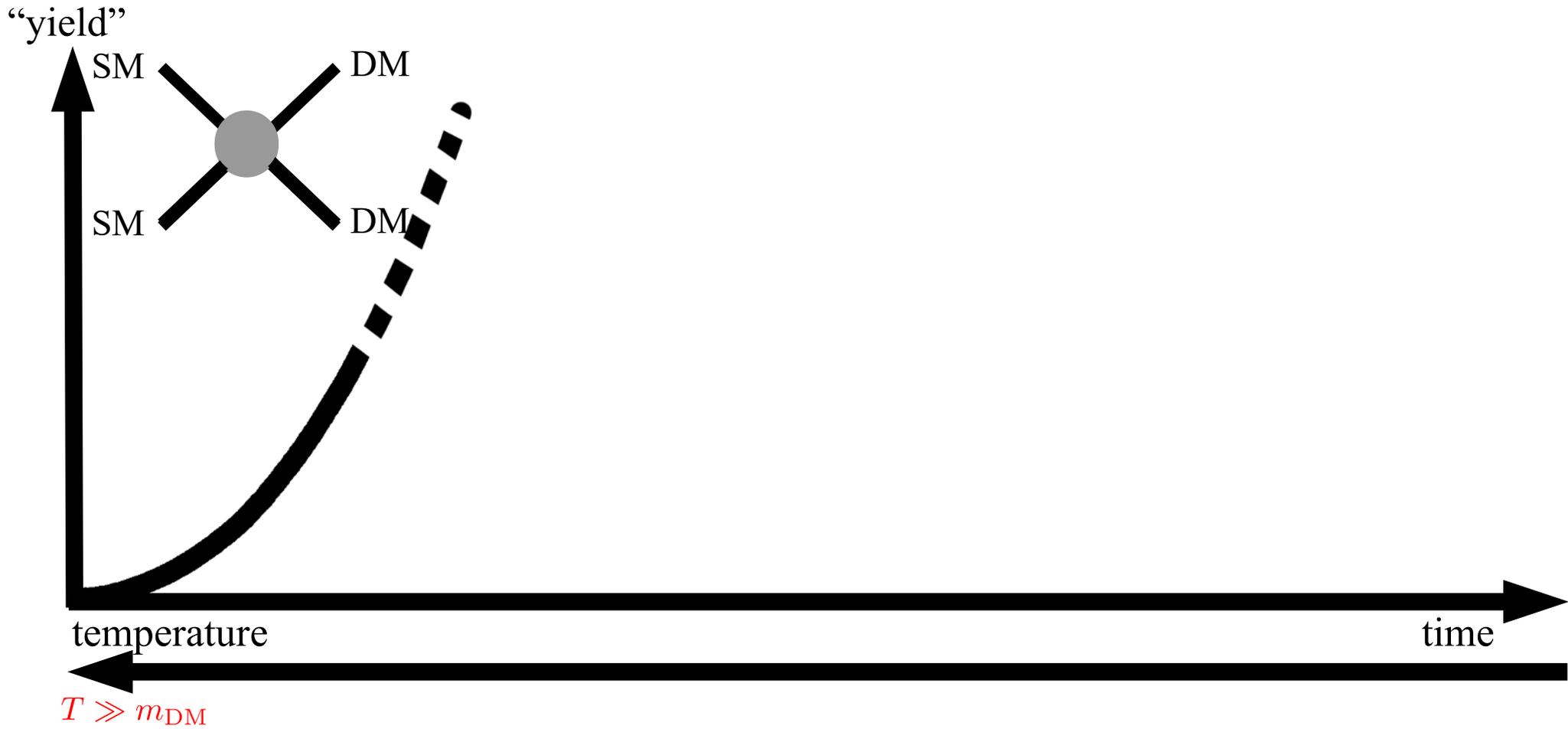
Assume that the temperature of the Universe after reheating was much larger than the DM mass.

WIMP history (in a nutshell)

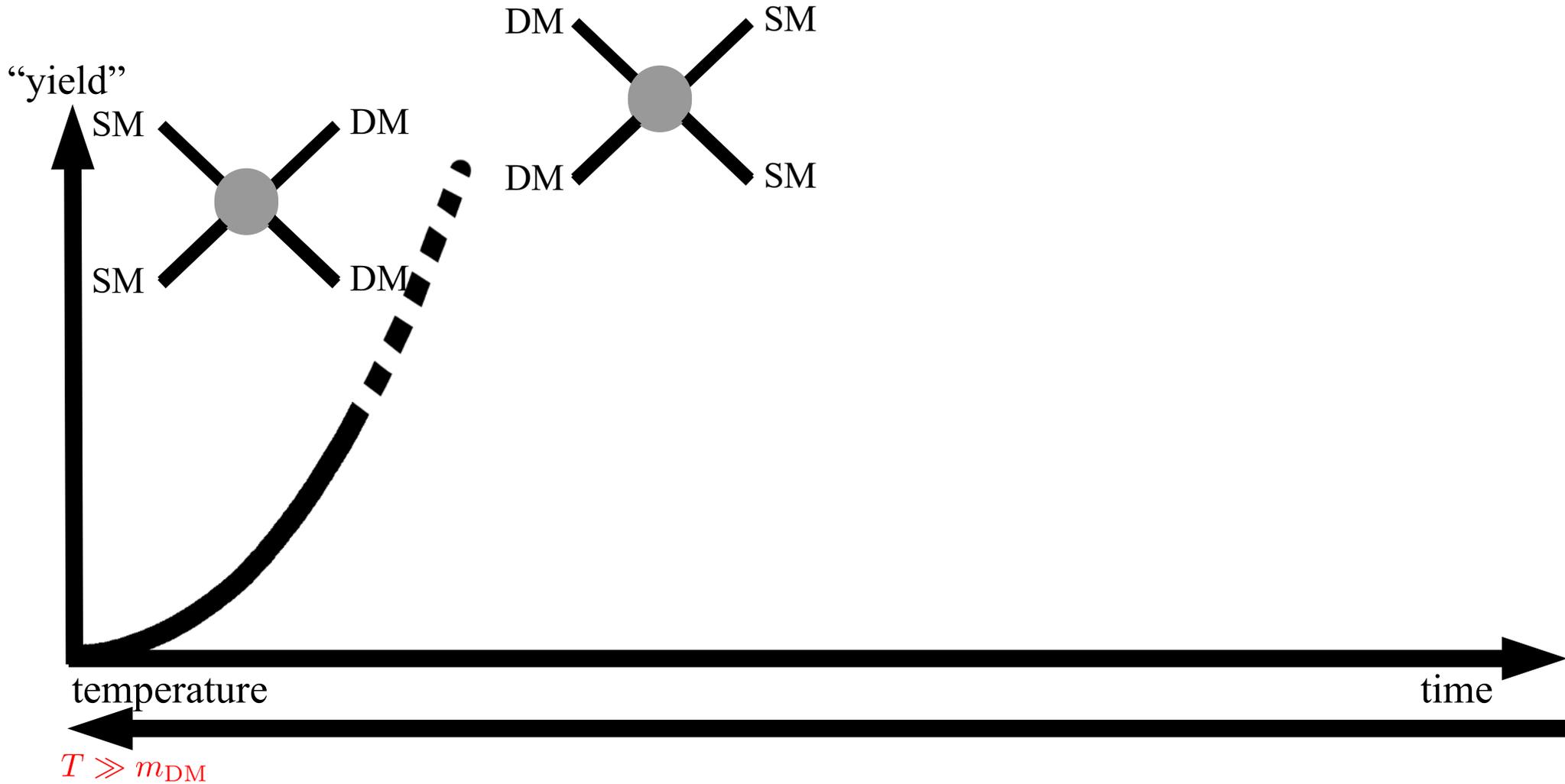


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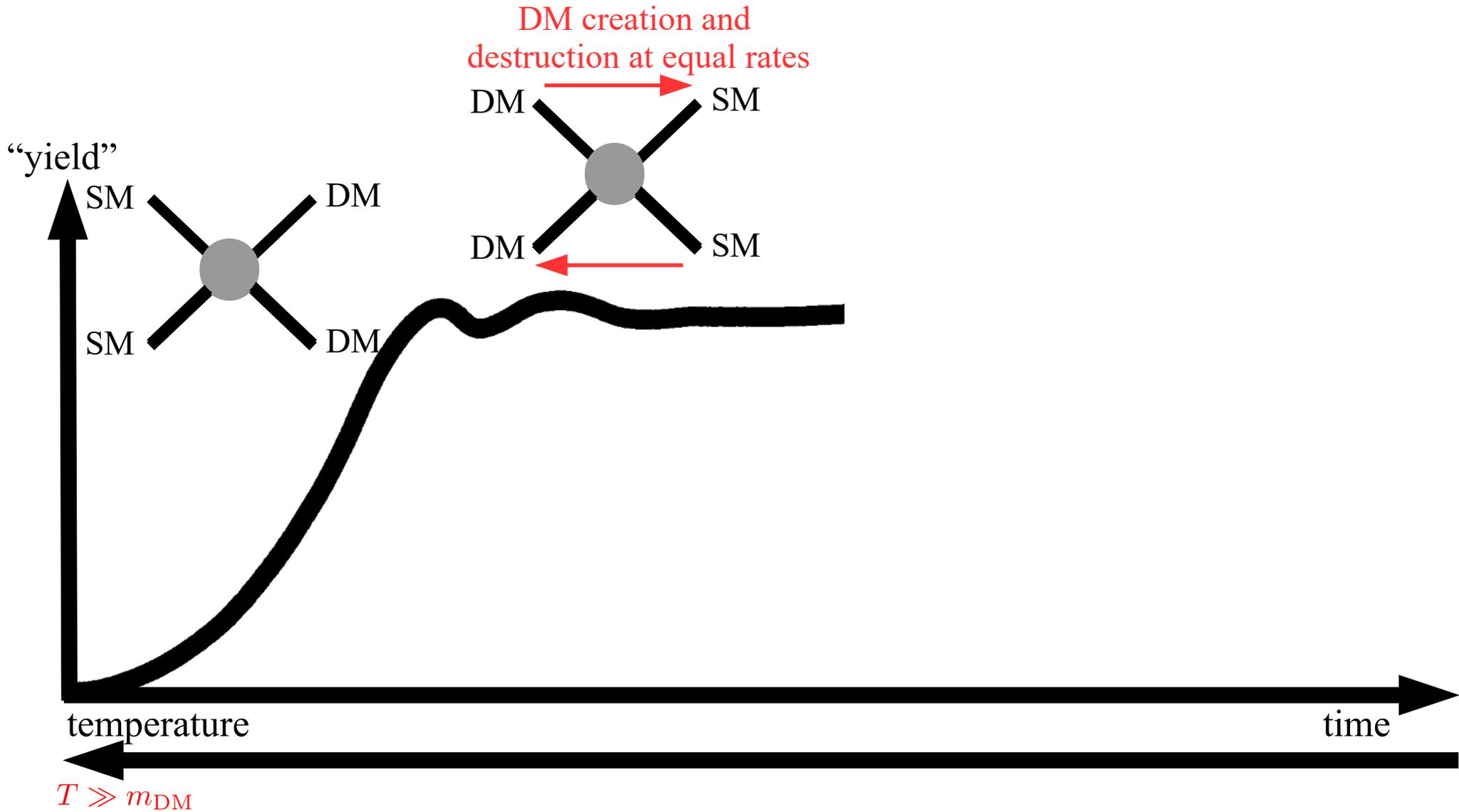
WIMP history (in a nutshell)



WIMP history (in a nutshell)

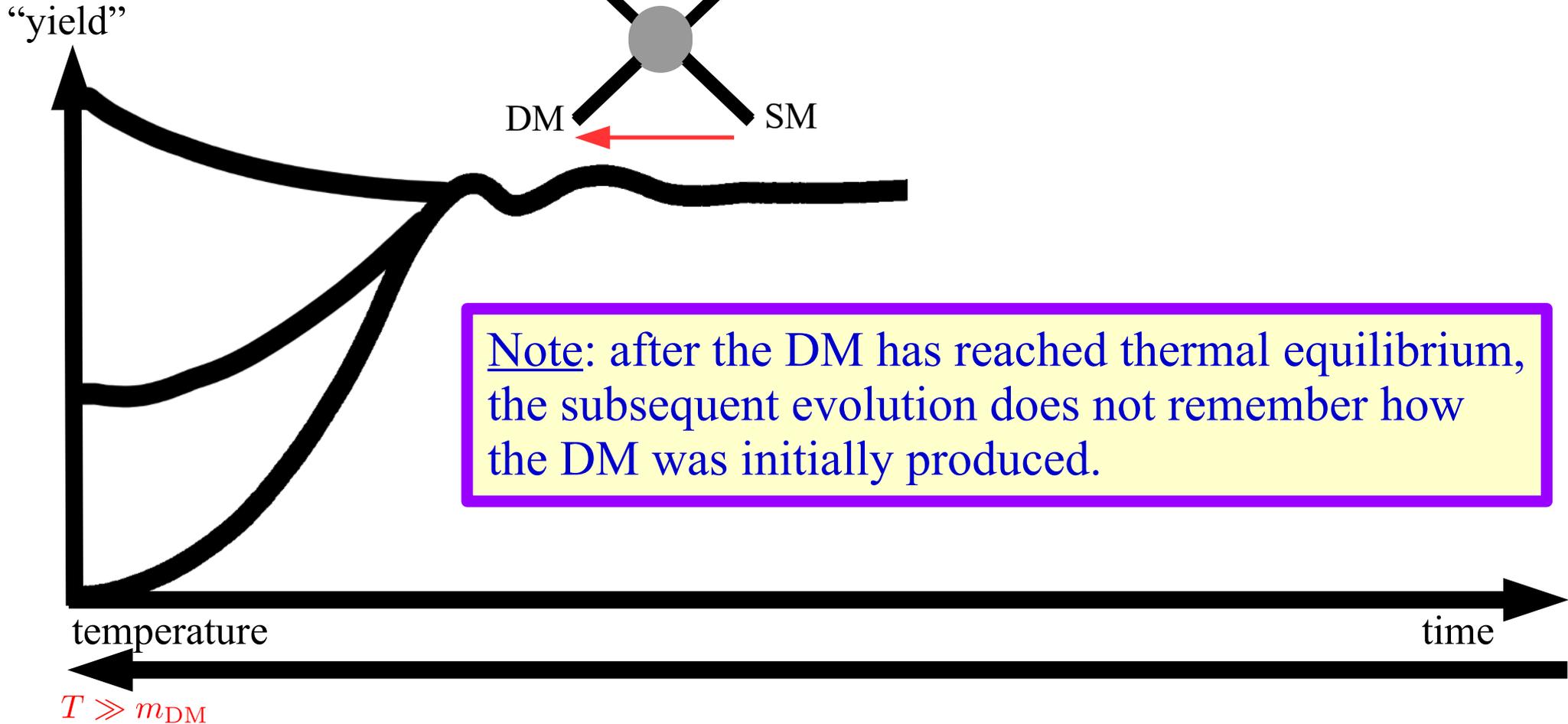
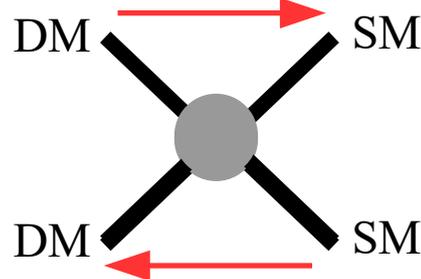


WIMP history (in a nutshell)



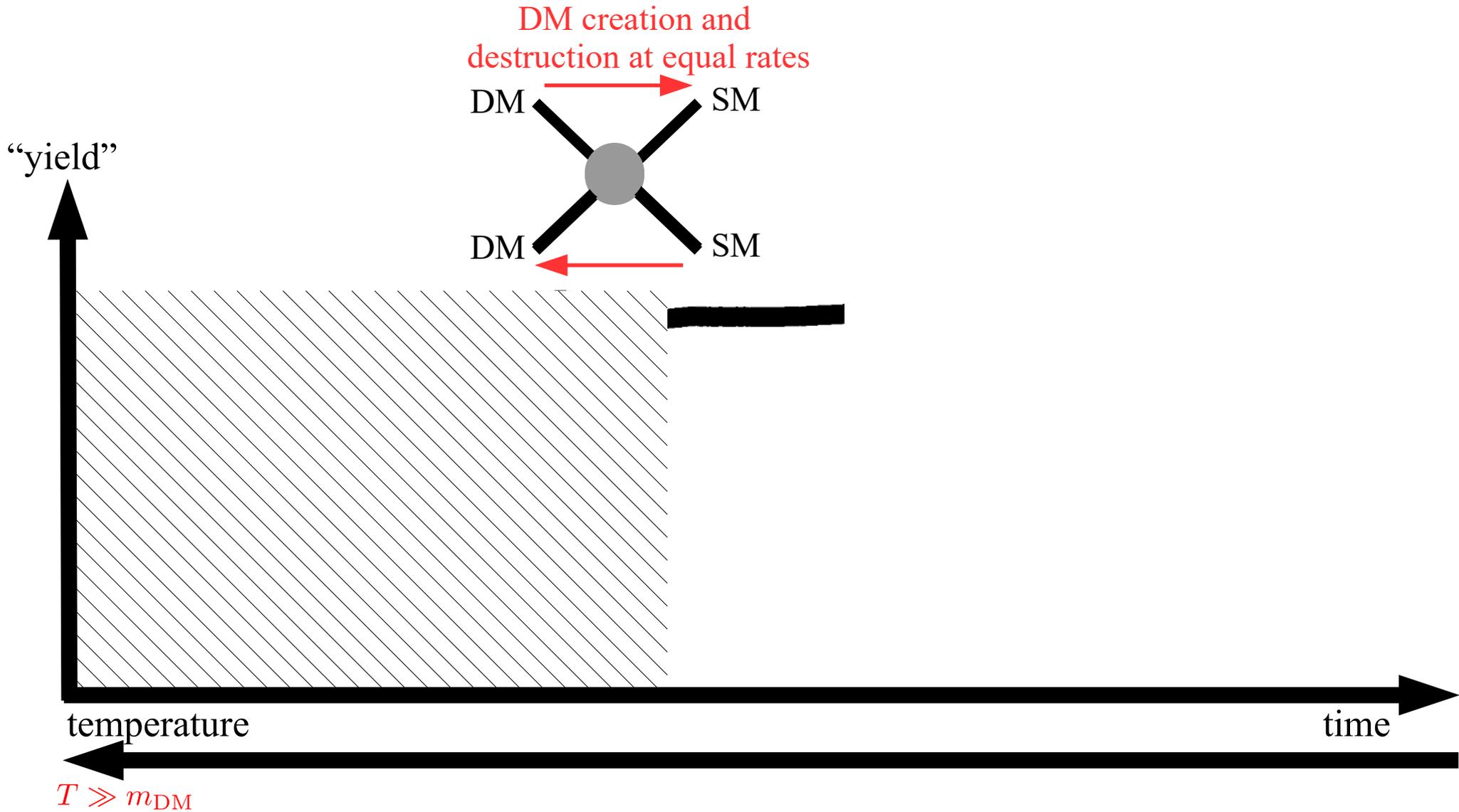
WIMP history (in a nutshell)

DM creation and
destruction at equal rates

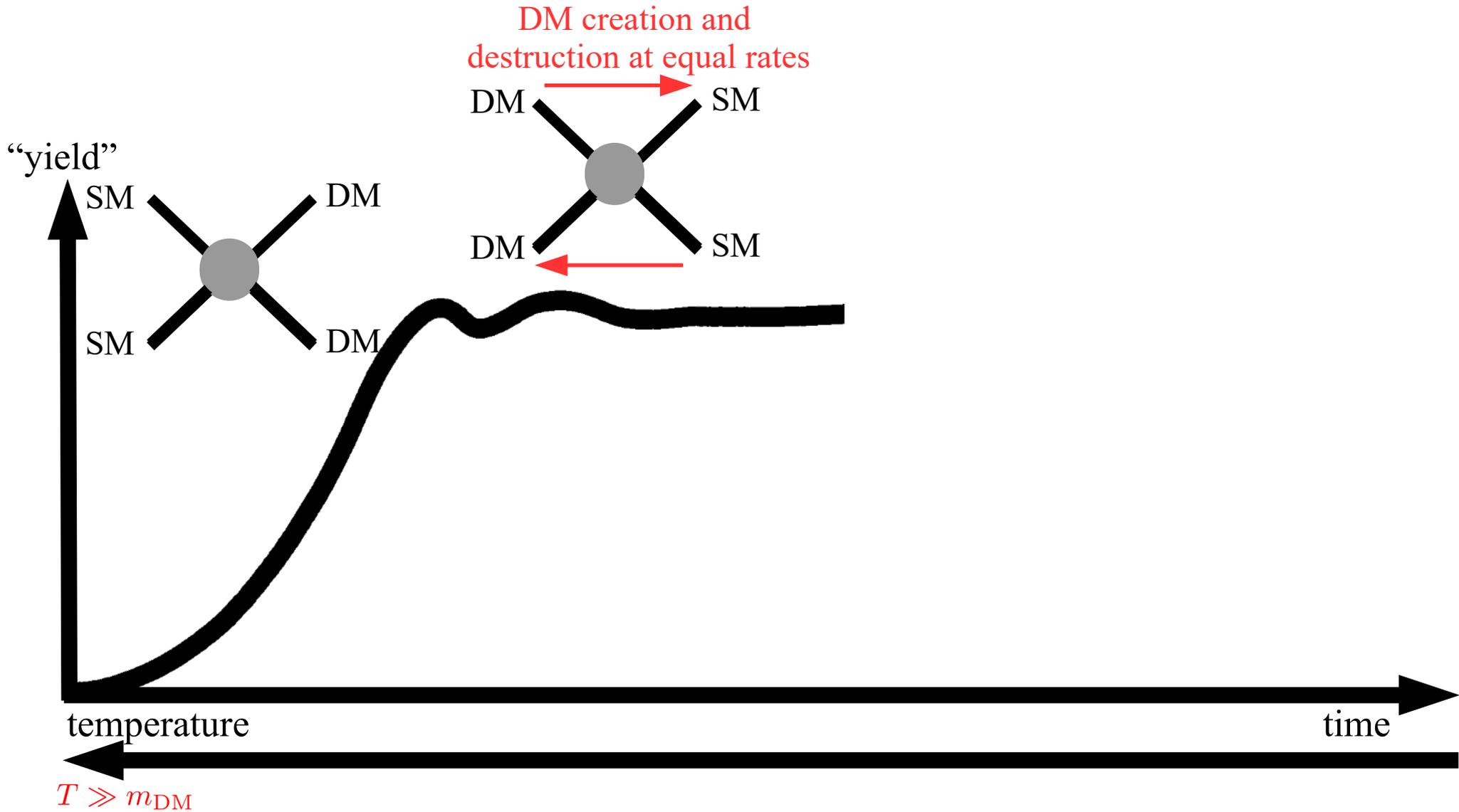


Note: after the DM has reached thermal equilibrium, the subsequent evolution does not remember how the DM was initially produced.

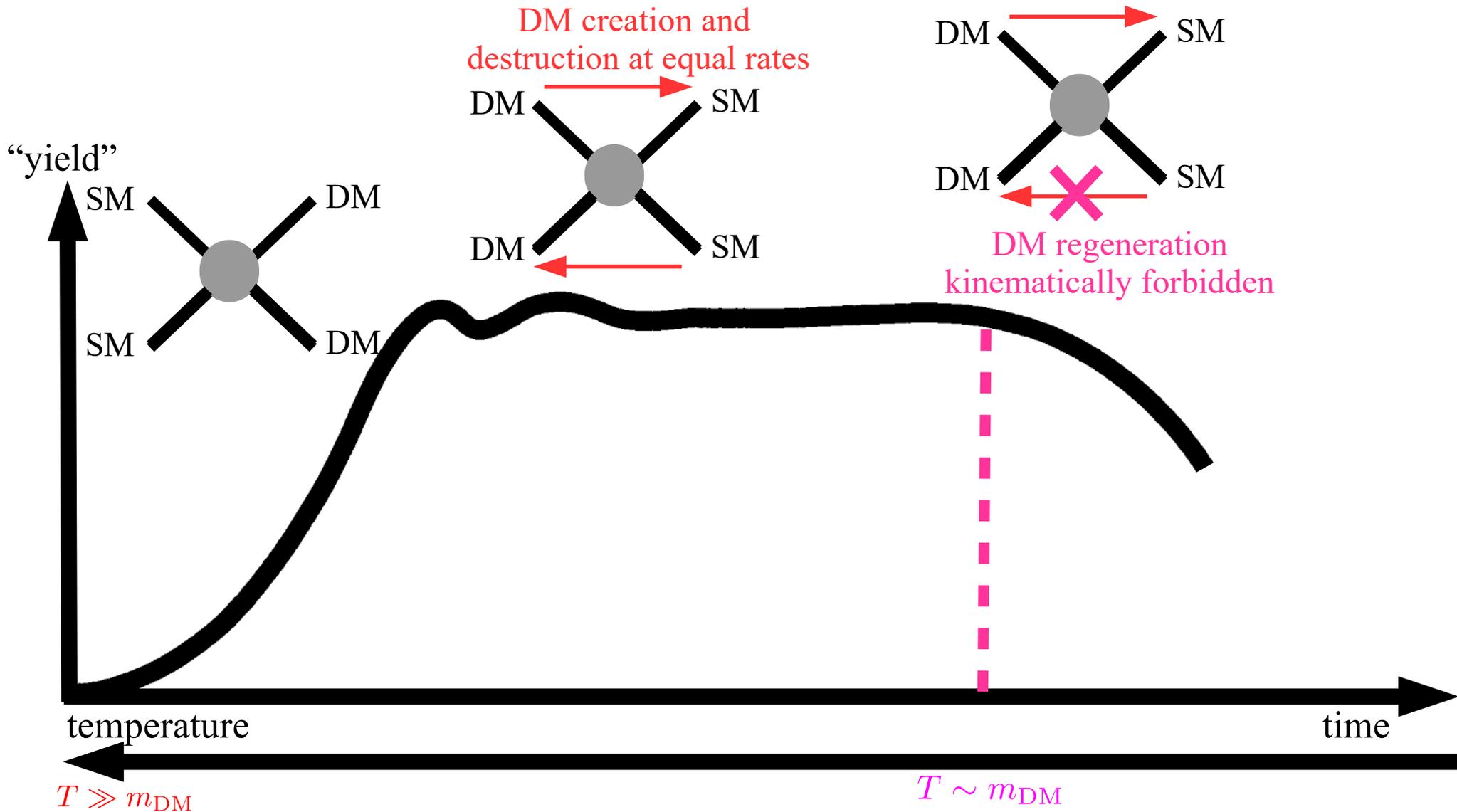
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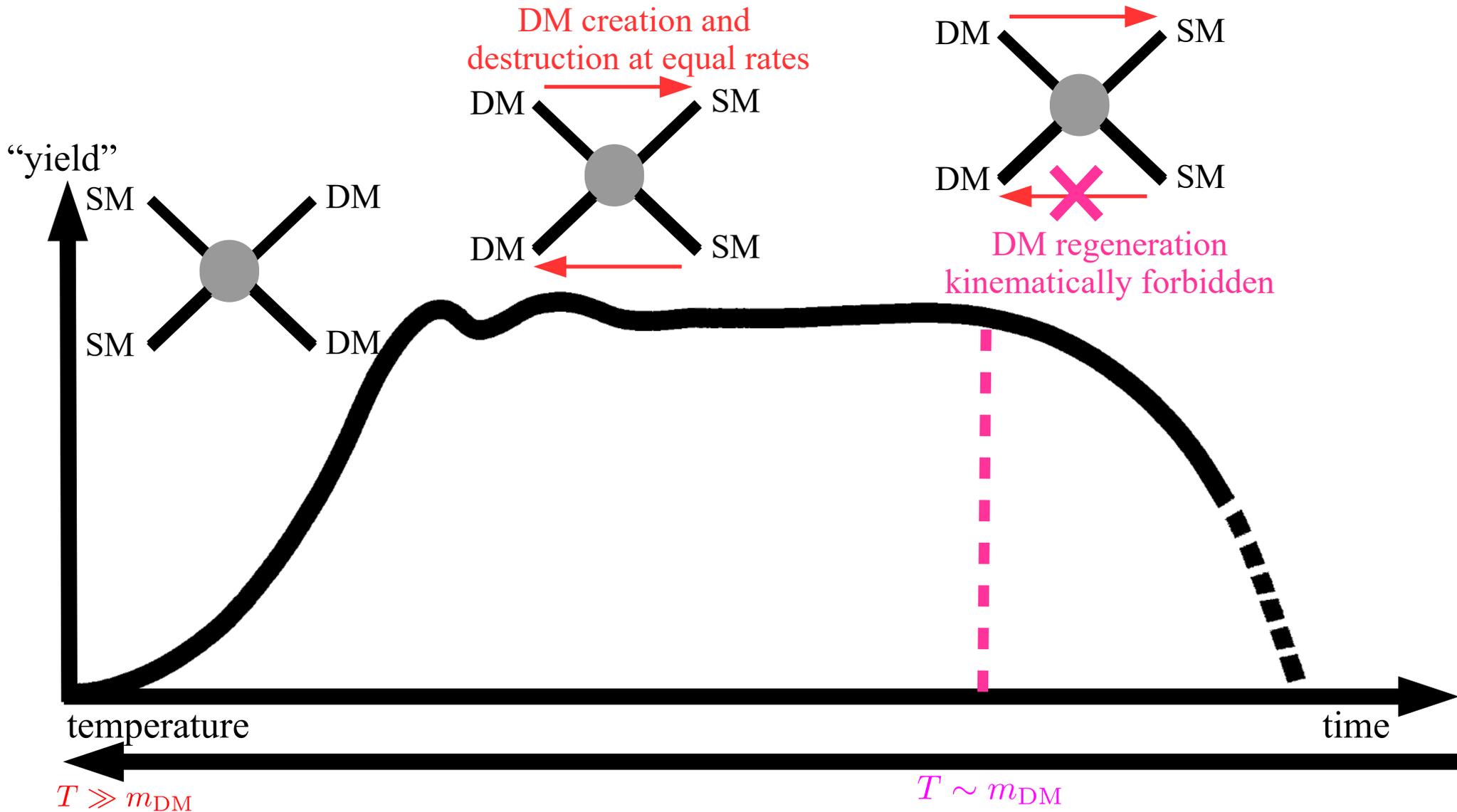
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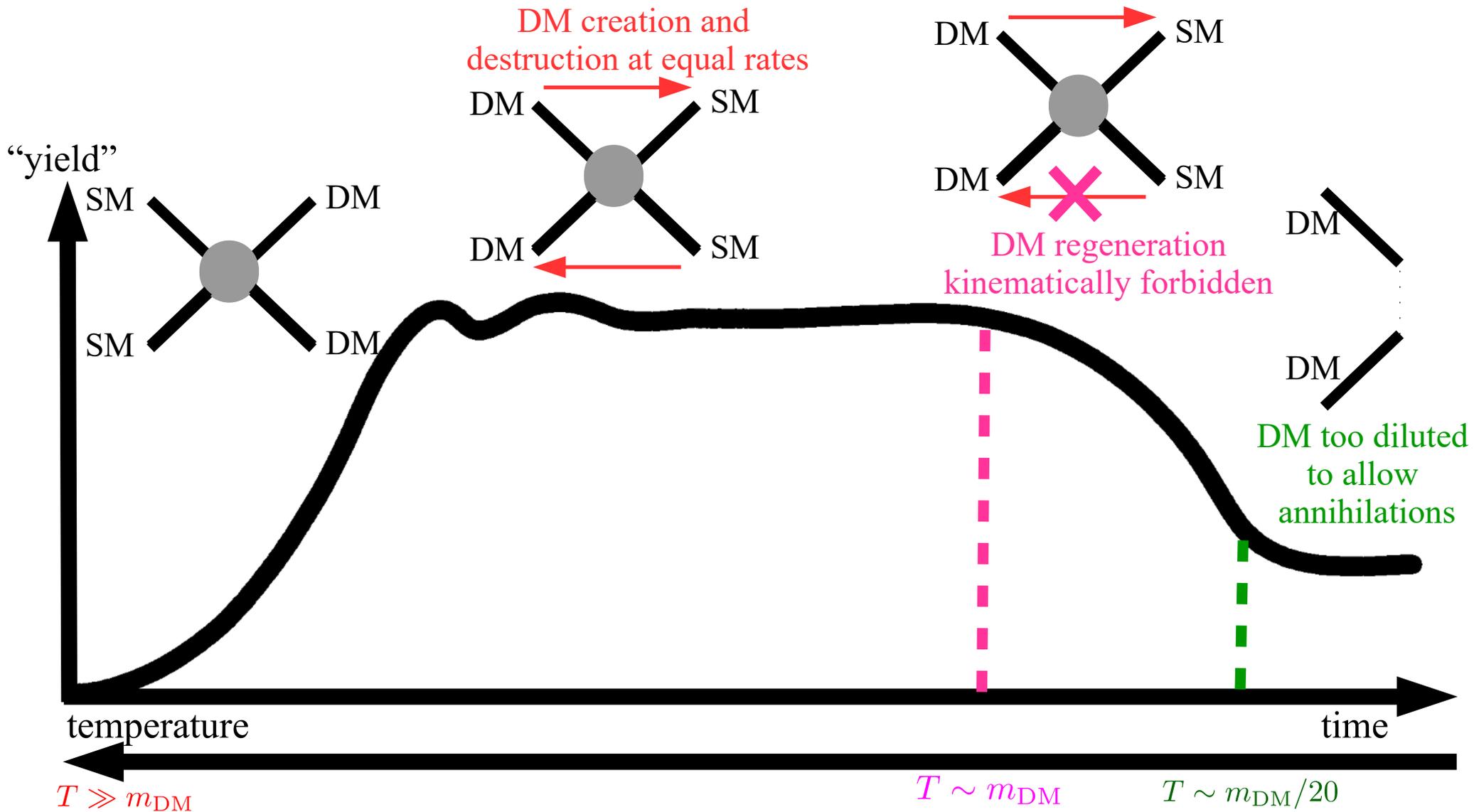
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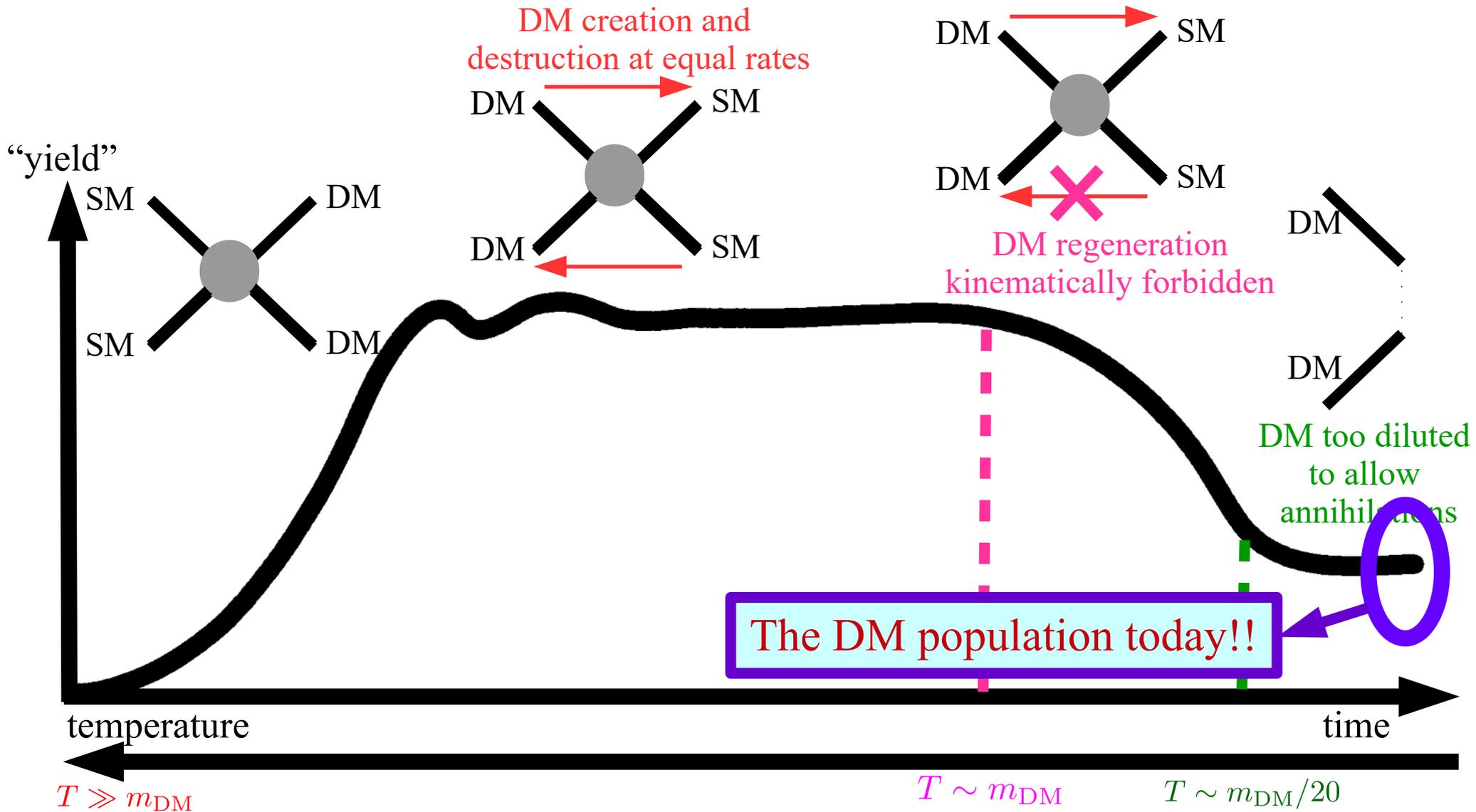
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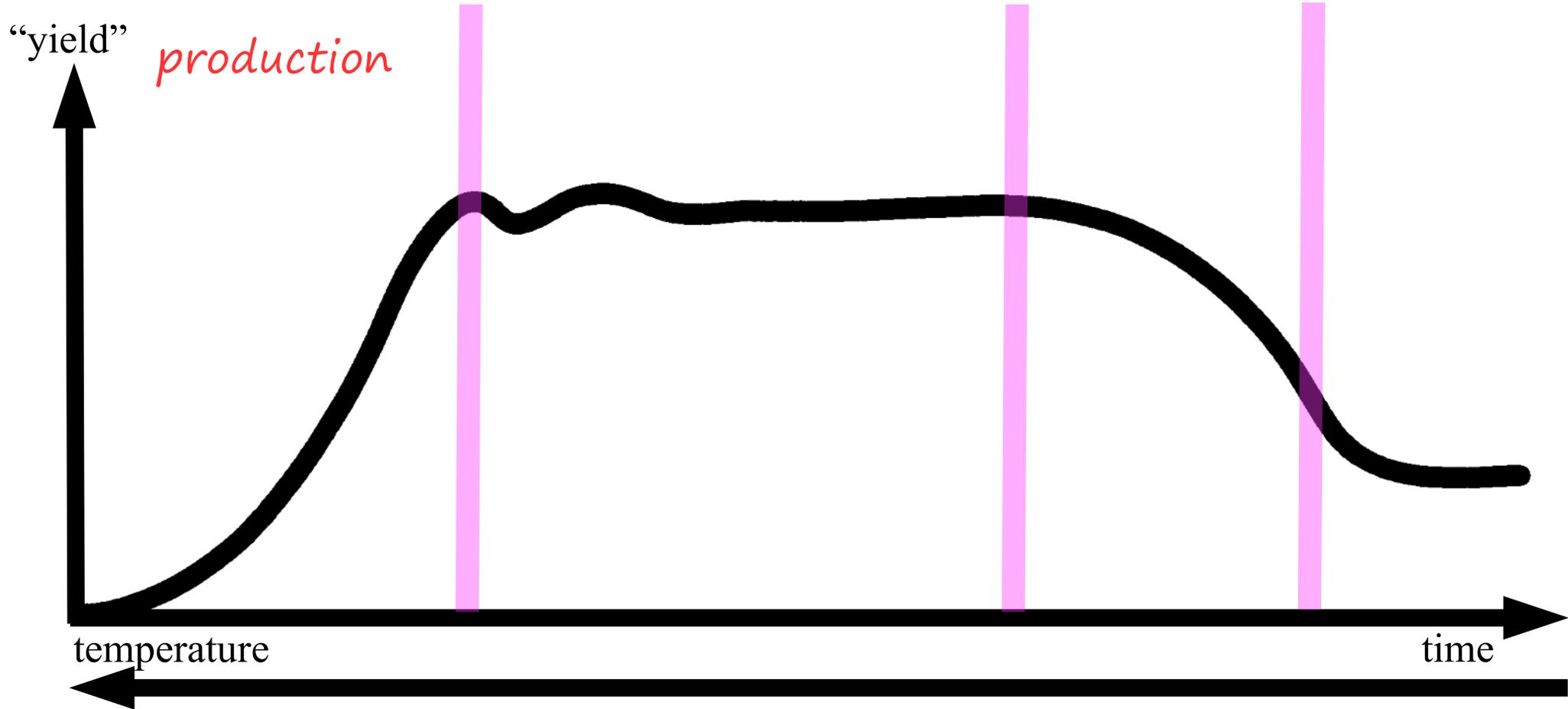
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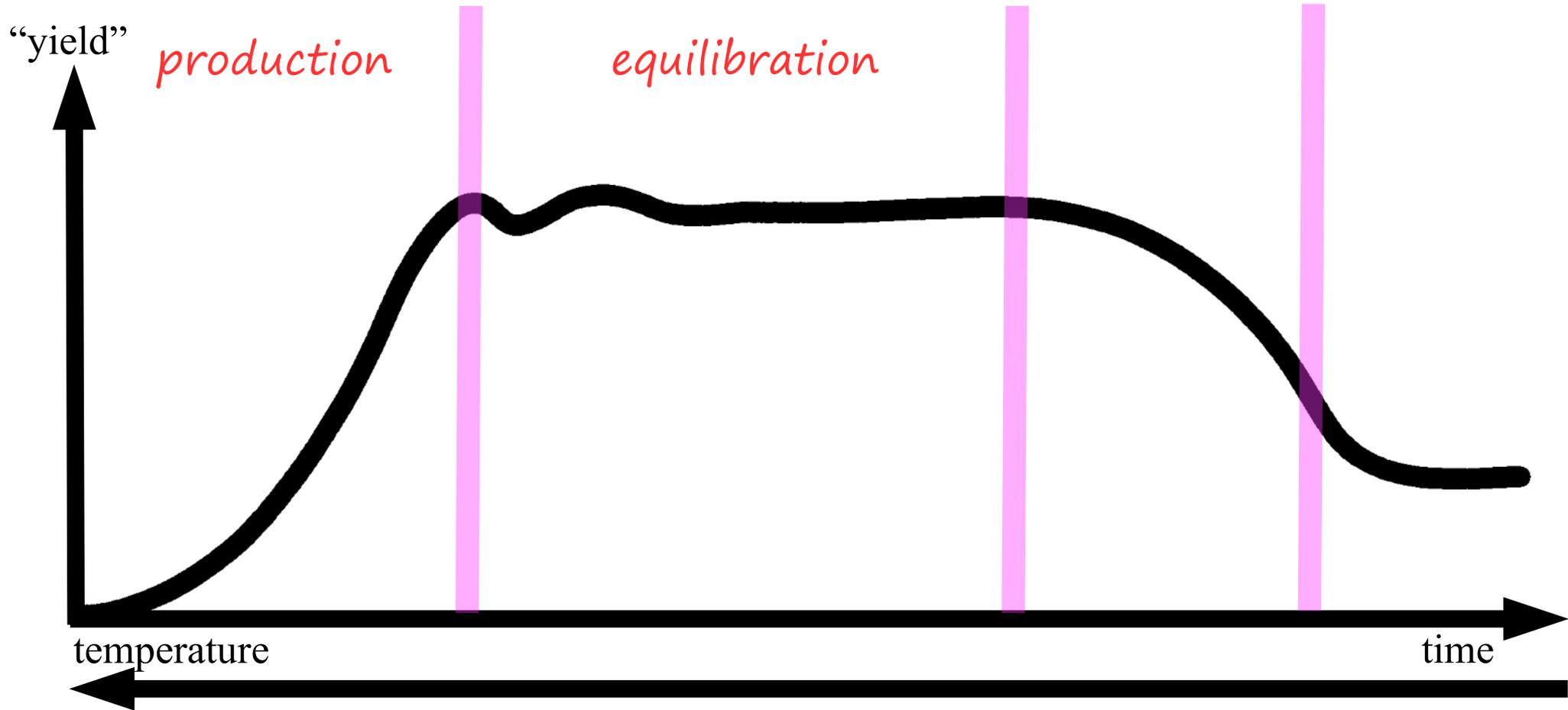
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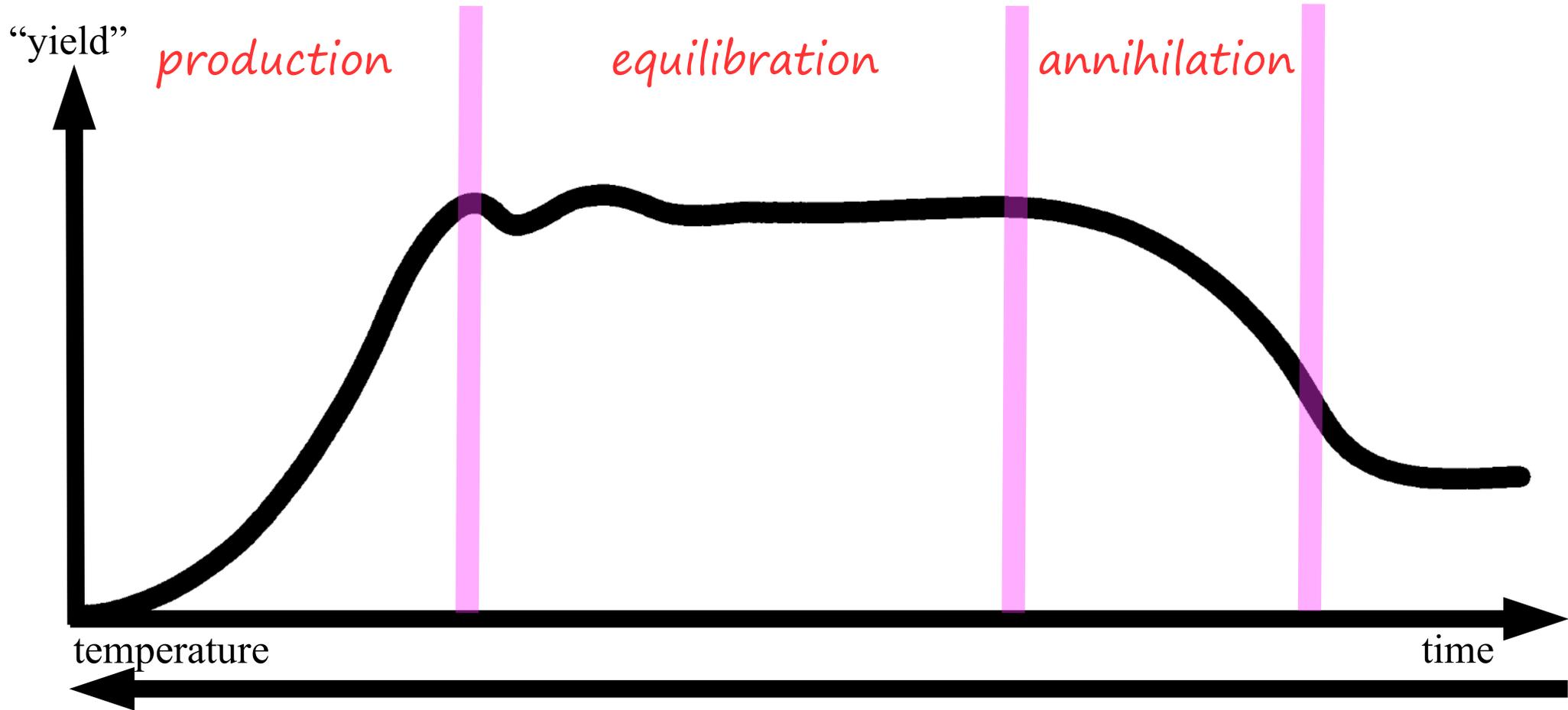
WIMP history (in a nutshell)



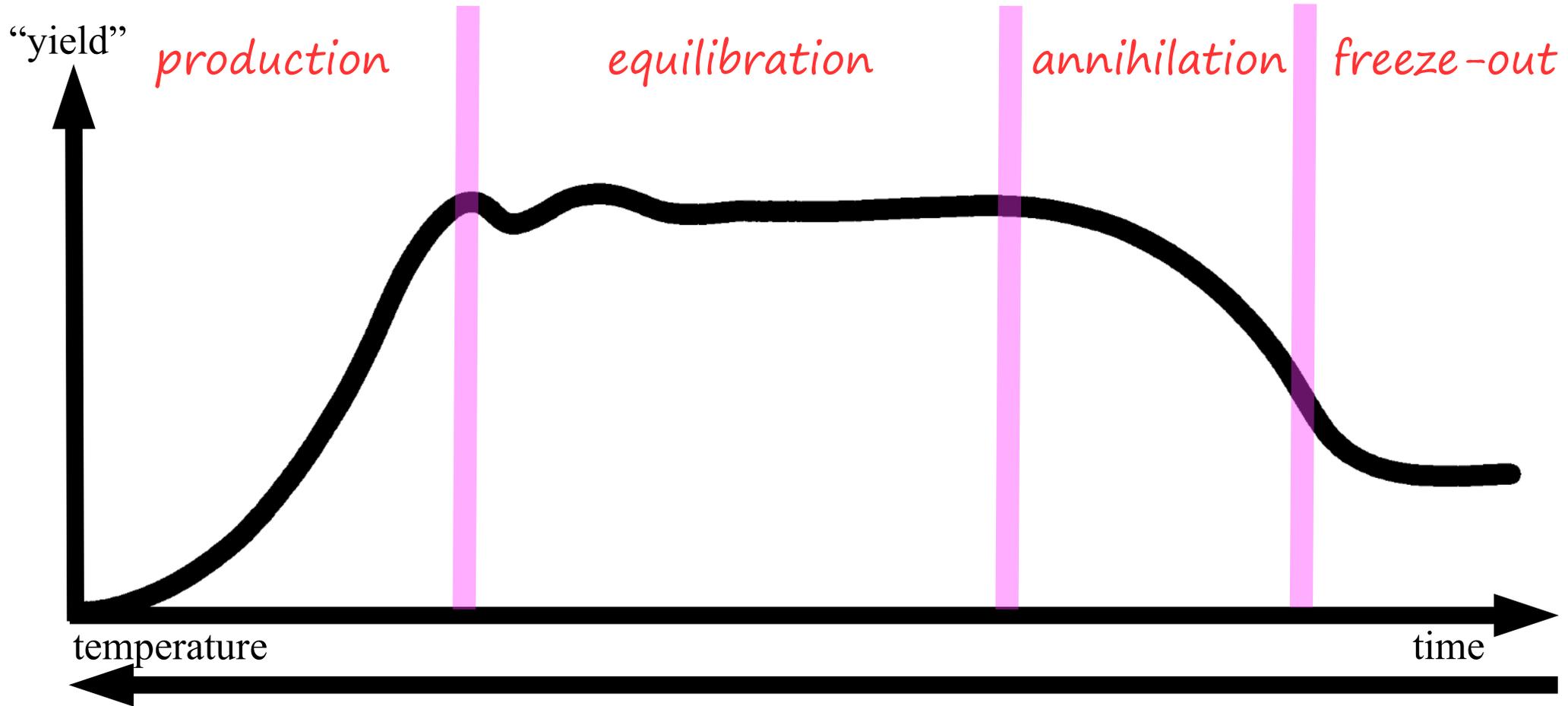
WIMP history (in a nutshell)



WIMP history (in a nutshell)

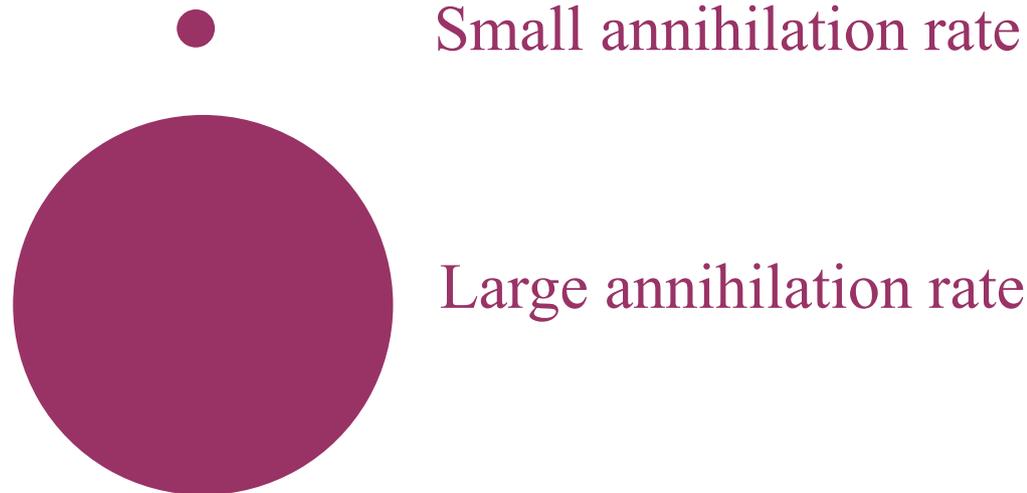


WIMP history (in a nutshell)



A heuristic view of the freeze-out

The probability of interaction is controlled by the cross-section

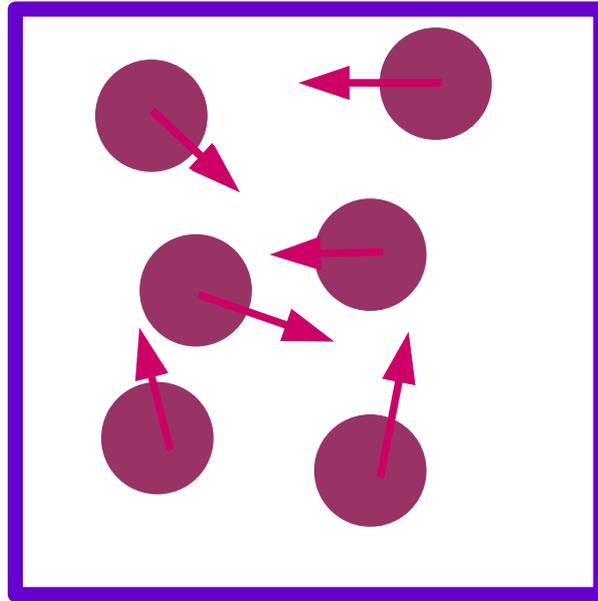


At very high temperatures, dark matter particles are annihilated and regenerated at the same rate.

However, at low temperatures, the Standard Model particles do not have enough kinetic energy to regenerate DM particles.

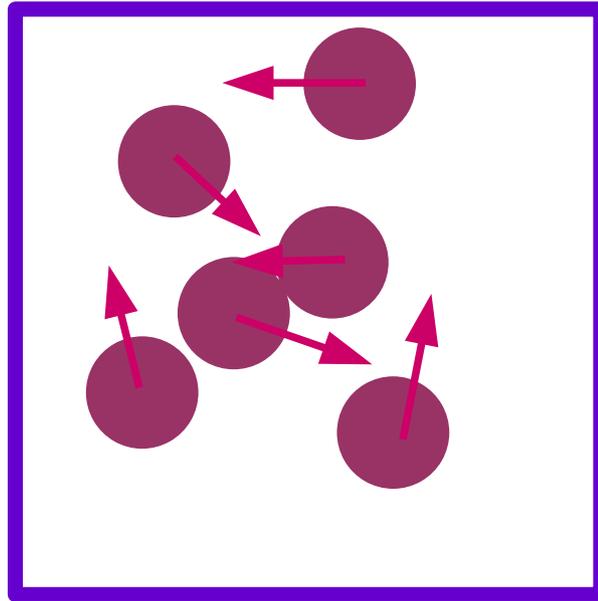
A heuristic view of the freeze-out

Dark matter population in a **static** Universe



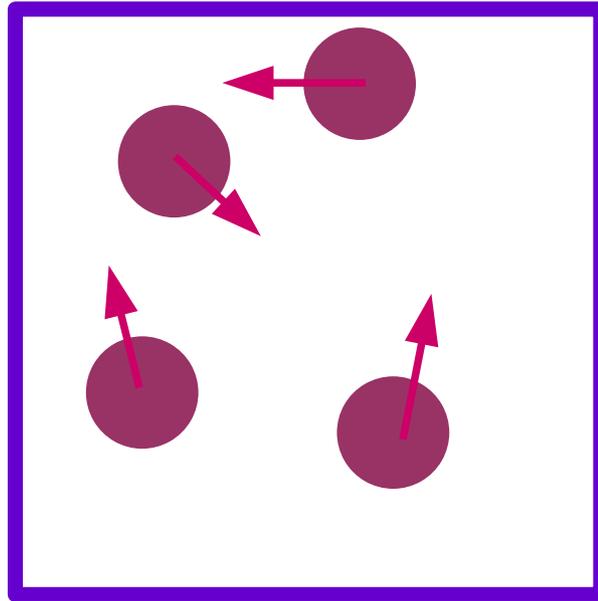
A heuristic view of the freeze-out

Dark matter population in a **static** Universe



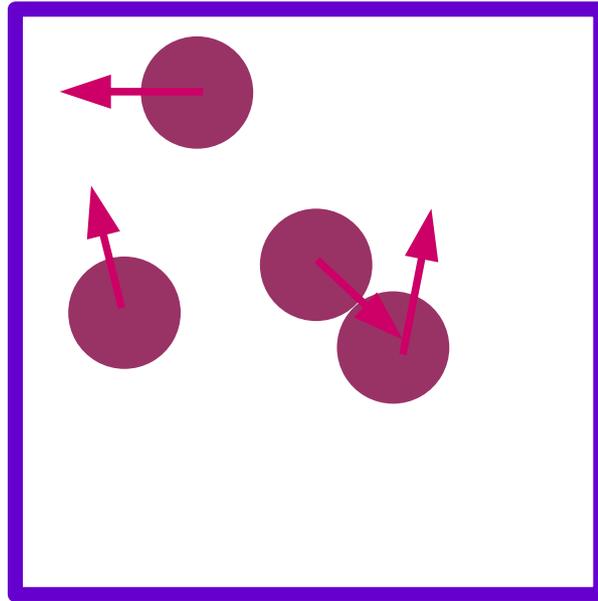
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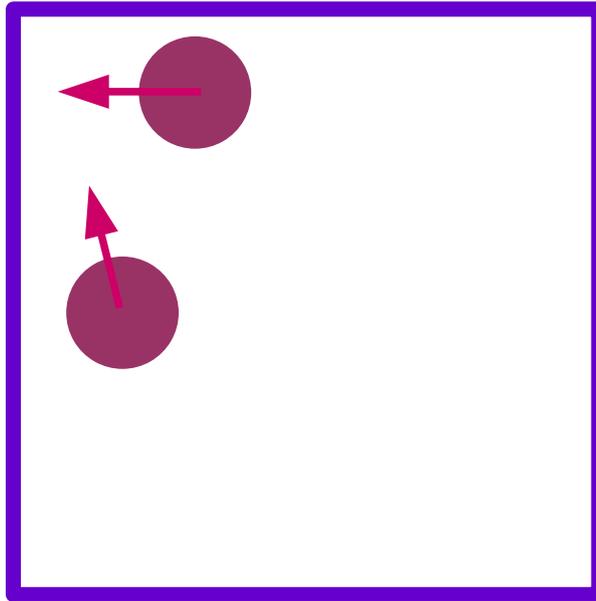
A heuristic view of the freeze-out

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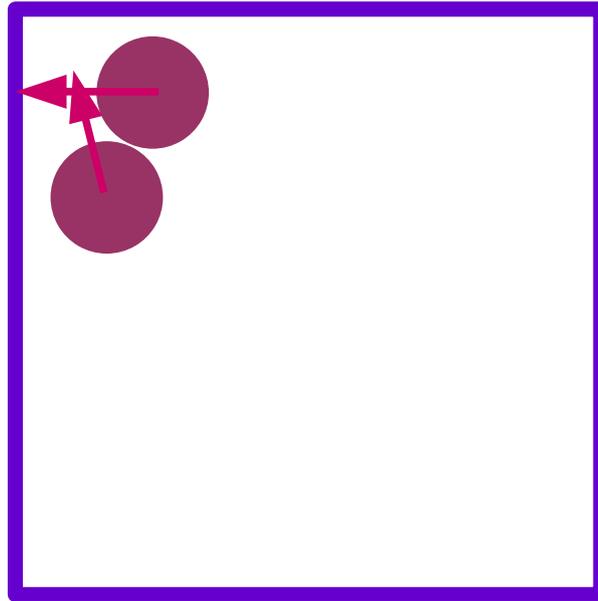
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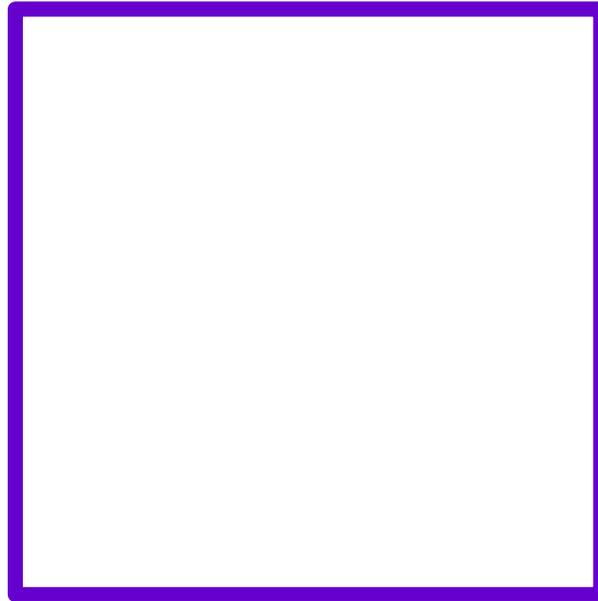
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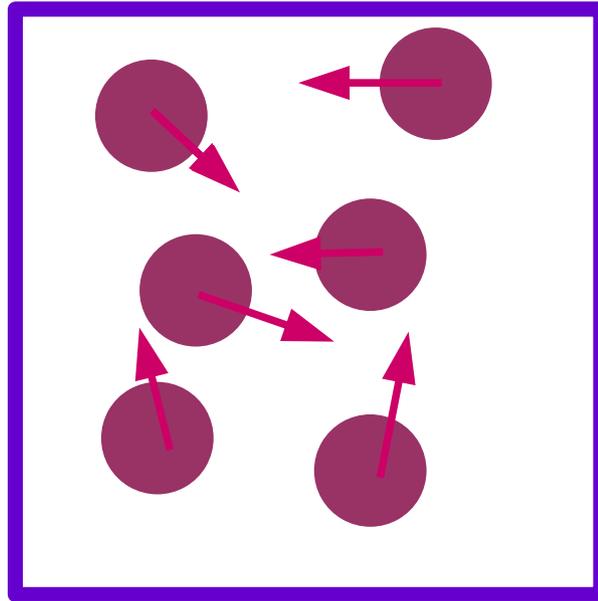
Dark matter population in a **static** Universe

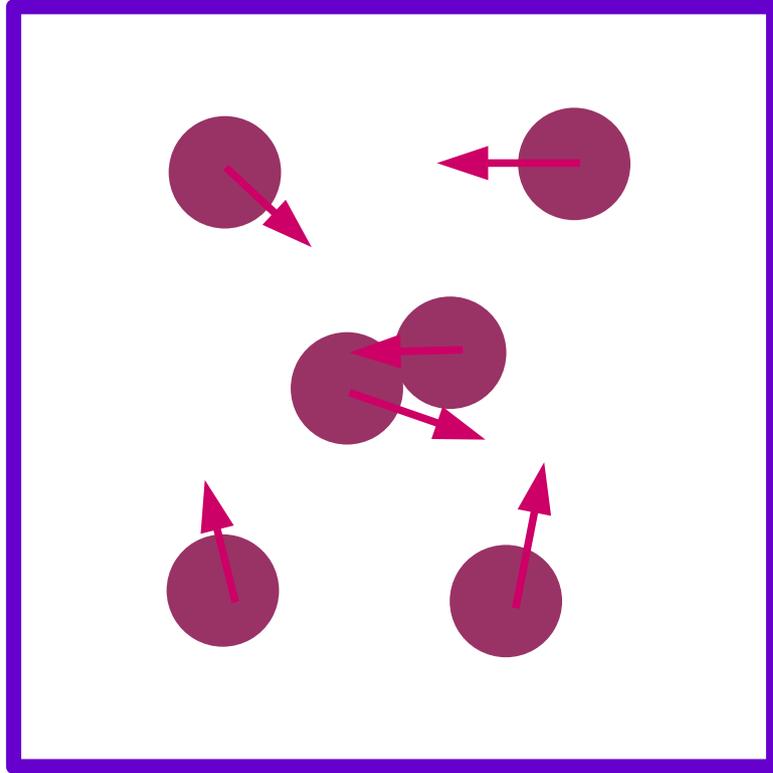


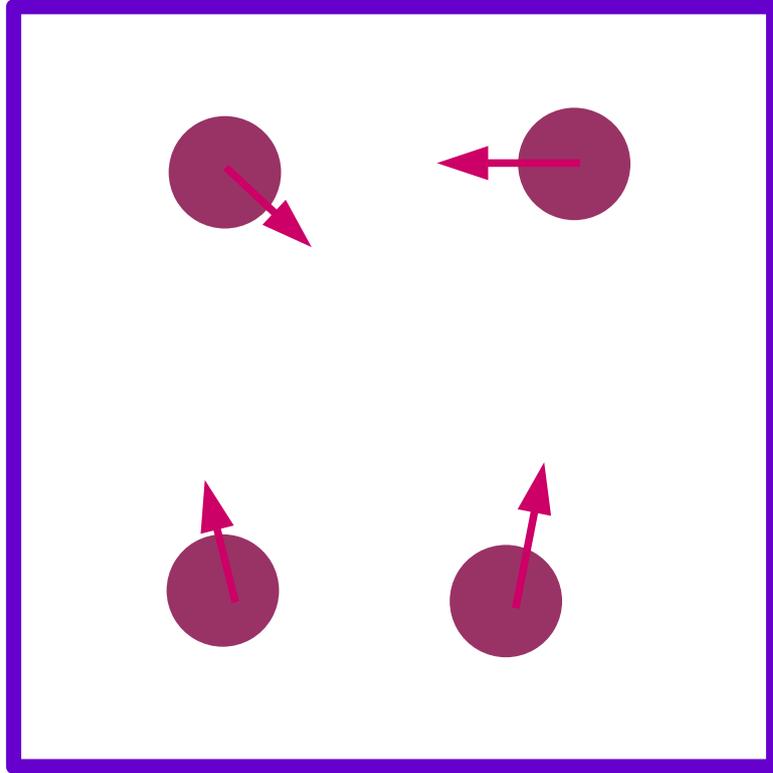
No DM particles at the end!

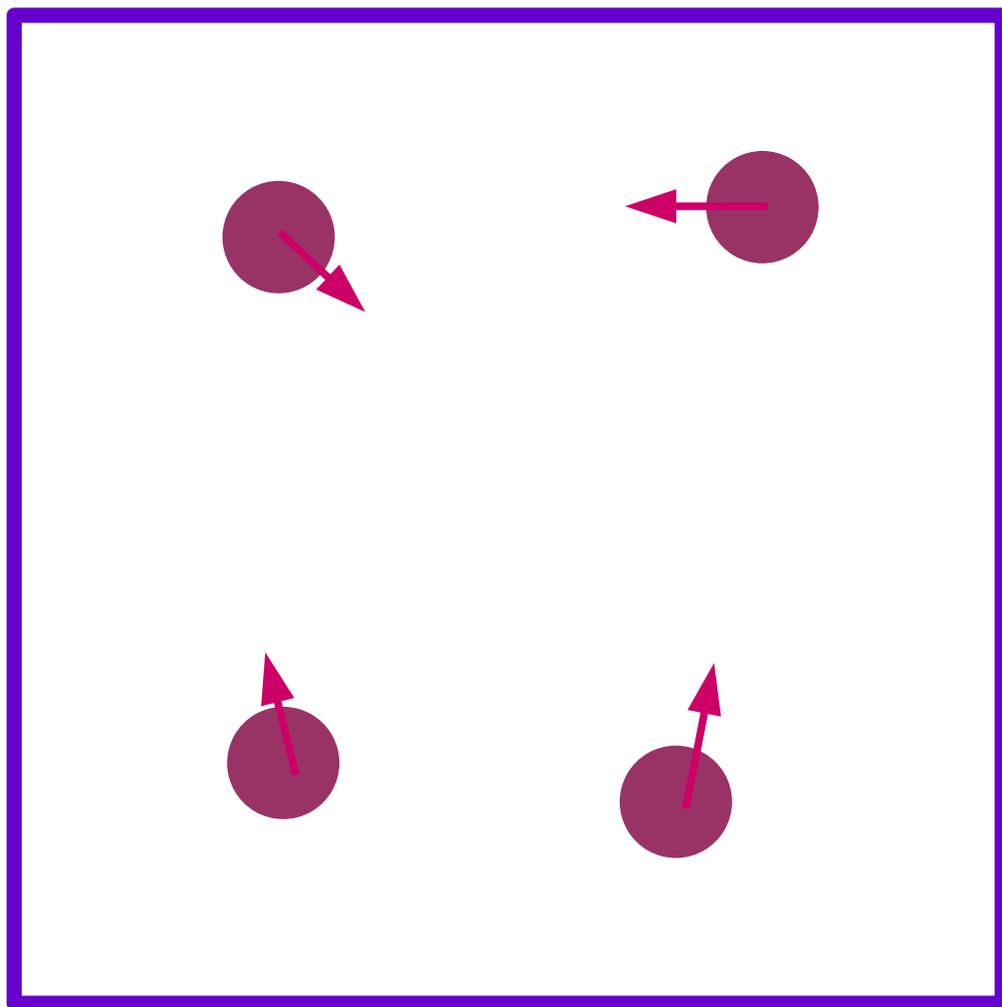
A heuristic view of the freeze-out

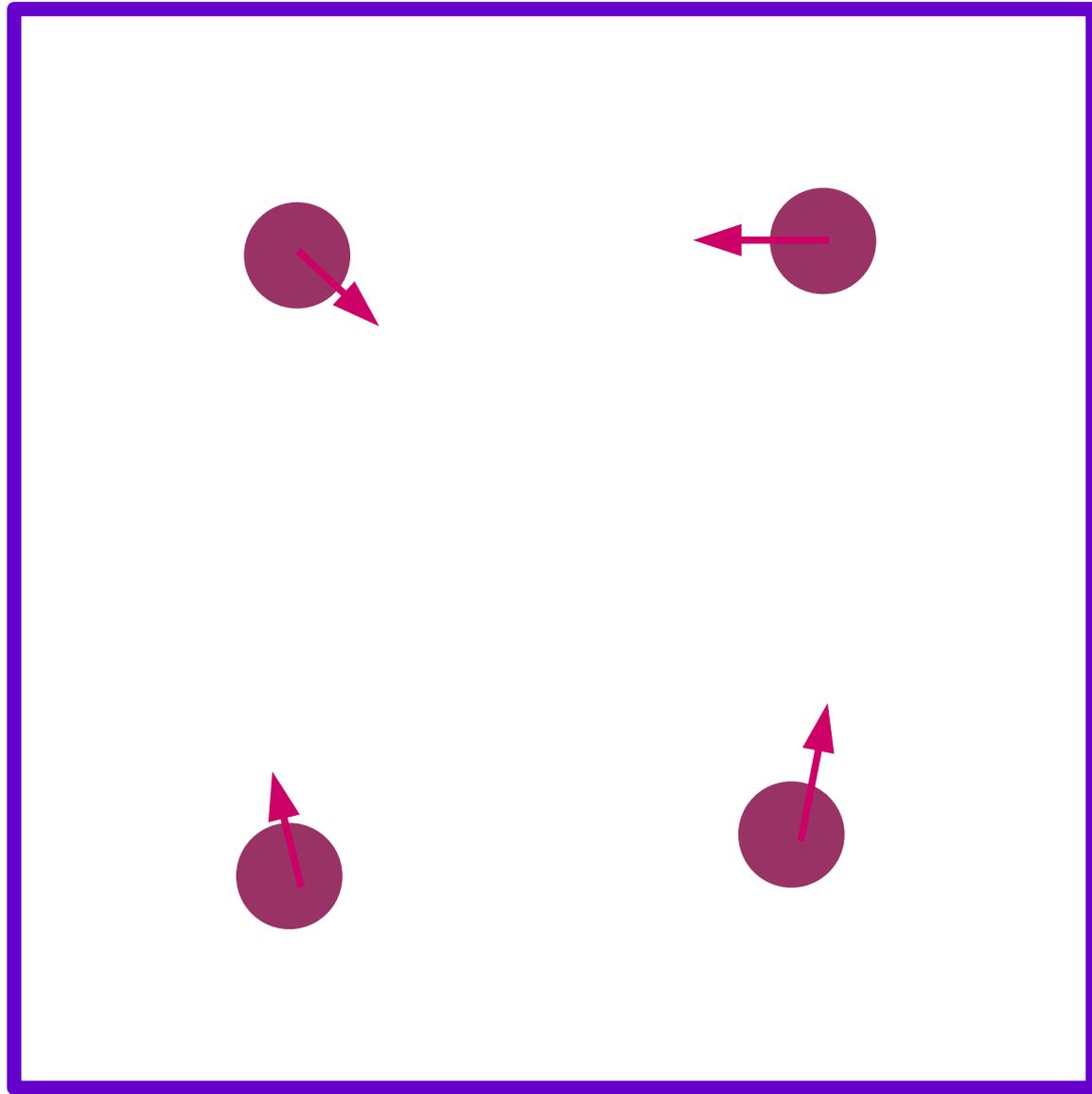
Dark matter population in an **expanding** Universe





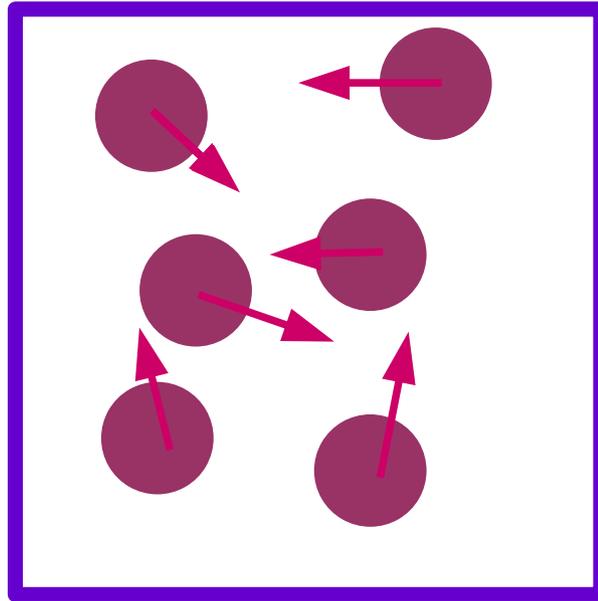




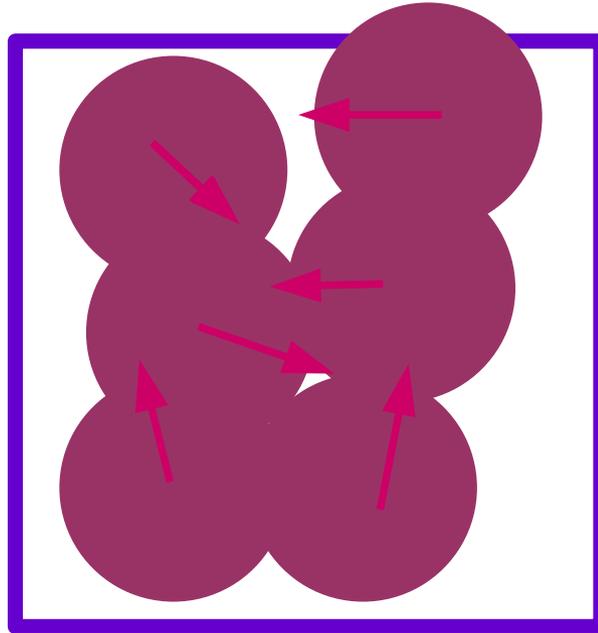


Dark matter particles can no longer annihilate.
The number of dark matter particles “freezes-out”

The *relic abundance* of dark matter particles depends on their annihilation cross section and on their velocity

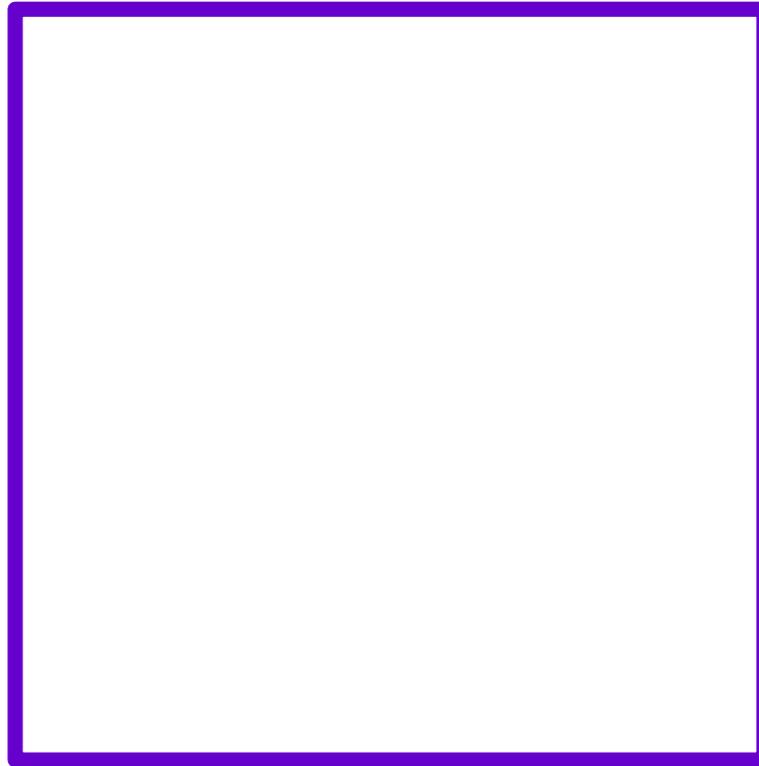


The *relic abundance* of dark matter particles depends on their annihilation cross section...



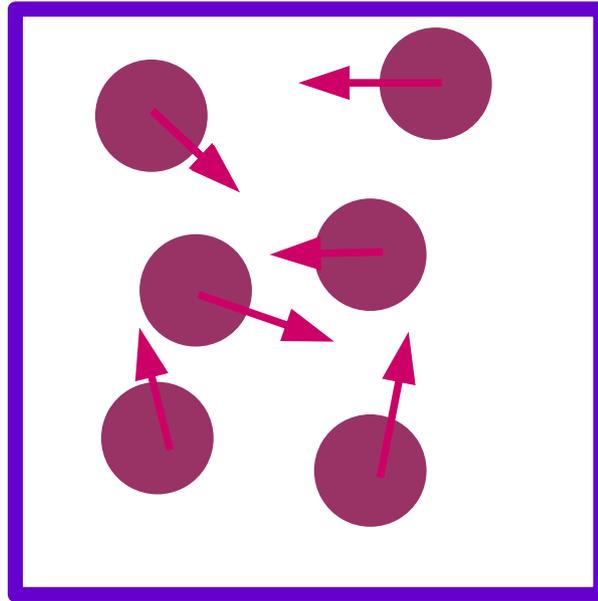
Large annihilation cross section \rightarrow Small relic abundance
Small annihilation cross section \rightarrow Large relic abundance

The *relic abundance* of dark matter particles depends on their annihilation cross section...

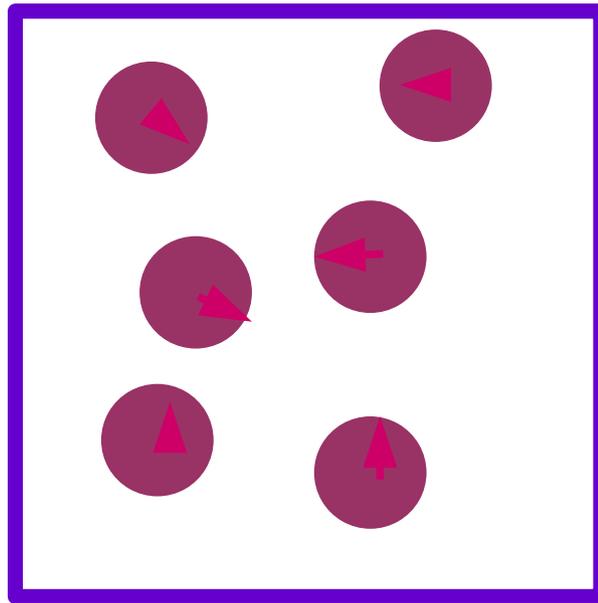


Large annihilation cross section \rightarrow Small relic abundance
Small annihilation cross section \rightarrow Large relic abundance

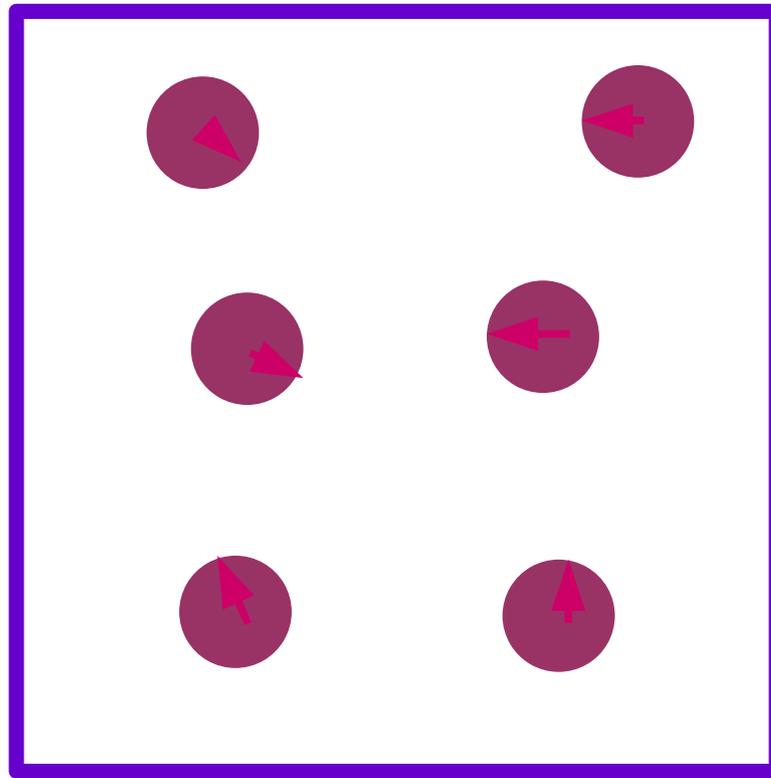
... and on their velocity



... and on their velocity



... and on their velocity



Large velocity \rightarrow Small relic abundance

Small velocity \rightarrow Large relic abundance

A heuristic view of the freeze-out

$$\Omega_{\text{DM}} h^2 \propto \frac{1}{\langle \sigma v \rangle}$$

The basic tool: the Boltzmann equation

Boltzmann equation: equation that describes the time evolution of the phase space density distribution $f(t, \vec{r}, \vec{p})$:

$$L[f] = C[f]$$

Liouville operator
(time evolution)

Collision term
(creation/destruction of particles in
phase space due to annihilations or
decays)

The basic tool: the Boltzmann equation

Boltzmann equation for the dark matter number density in an expanding Universe:

$$\frac{dn}{dt} + 3Hn = -\langle\sigma v\rangle(n^2 - n_{\text{eq}}^2)$$

(under some assumptions – see later)

- $n(t)$ number density of DM particles

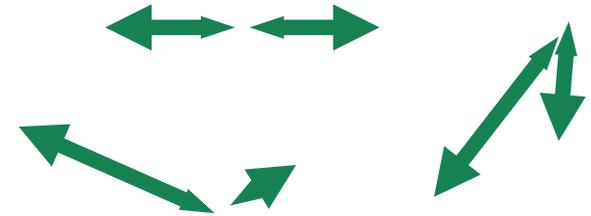
$$n(t) = \frac{g}{(2\pi)^3} \int d^3p f(t, E)$$

- $H(t) \equiv \frac{\dot{a}}{a} \rightarrow$ Hubble rate

- σ = annihilation cross-section
DM DM \rightarrow SM SM

- v = relative velocity

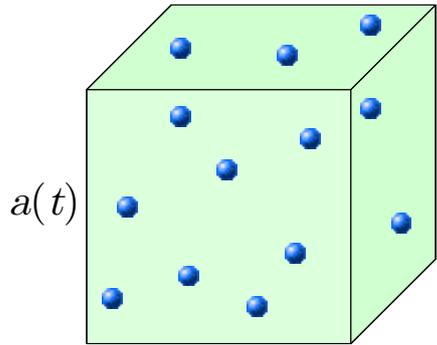
- $\langle\dots\rangle$ = thermal average



Justification

LHS

Assume that the collision term vanishes ($\sigma=0$)
 \Rightarrow number of particles conserved



$$\frac{dN(t)}{dt} = 0$$

$$N(t) = n(t)V(t) = n(t)a(t)^3$$

$$\rightsquigarrow \frac{d}{dt}(na^3) = \dot{n}a^3 + 3na^2\dot{a} = 0$$

$$\Rightarrow a^3\left(\dot{n} + 3\frac{\dot{a}}{a}n\right) = 0$$

$$\dot{n} + 3Hn = 0 \text{ when } \sigma = 0$$

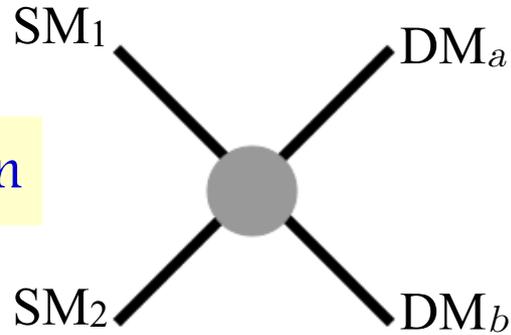
Justification

RHS

Remember:

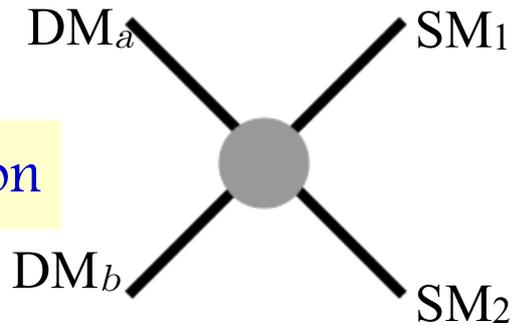
Boltzmann equation: change of n = production - destruction

production



$$\sim \int |\mathcal{M}_{12 \rightarrow ab}|^2 f_1 f_2 d(\text{phase space})$$

destruction



$$\sim \int |\mathcal{M}_{ab \rightarrow 12}|^2 f_a f_b d(\text{phase space})$$

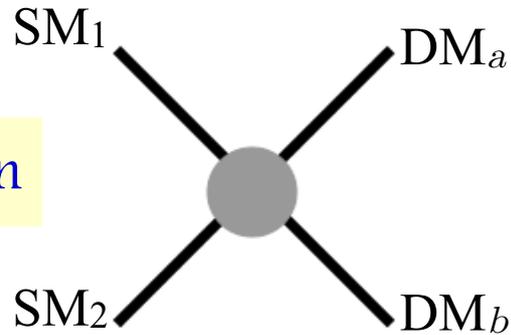
Justification

RHS

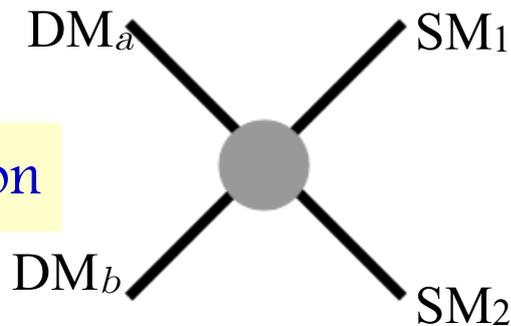
Remember:

Boltzmann equation: change of $n = \text{production} - \text{destruction}$

production



destruction



$$\sim \int |\mathcal{M}_{12 \rightarrow ab}|^2 f_1 f_2 d(\text{phase space})$$

Equal if T conserved
(CP conserved)

$$\sim \int |\mathcal{M}_{ab \rightarrow 12}|^2 f_a f_b d(\text{phase space})$$

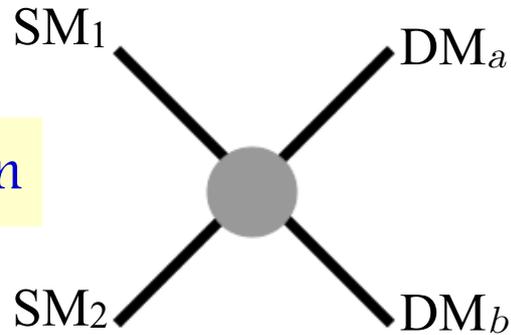
Justification

RHS

Remember:

Boltzmann equation: change of $n = \text{production} - \text{destruction}$

production

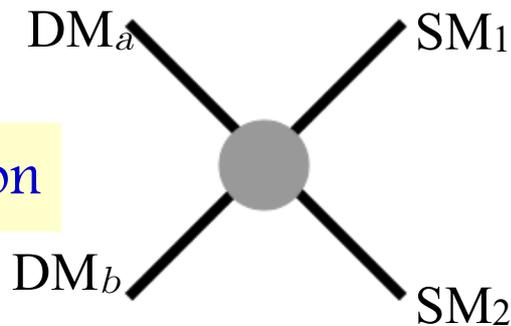


$$\sim \int |\mathcal{M}_{12 \rightarrow ab}|^2 f_1 f_2 d(\text{phase space})$$

Equal if T conserved
(CP conserved)

Assumption 1

destruction



$$\sim \int |\mathcal{M}_{ab \rightarrow 12}|^2 f_a f_b d(\text{phase space})$$

$$\text{RHS} \sim - \int |\mathcal{M}_{ab \rightarrow 12}|^2 (f_a f_b - f_1 f_2) d(\text{phase space})$$

Justification

RHS

Assume SM particles in thermal equilibrium Assumption 2

$$f_1 = f_1^{\text{eq}} = e^{-E_1/T} \quad (\text{Boltzmann distribution})$$

Justification

RHS

Assume SM particles in thermal equilibrium Assumption 2

$$f_1 = f_1^{\text{eq}} = e^{-E_1/T} \quad (\text{Boltzmann distribution})$$

$$\Rightarrow f_1 f_2 = f_1^{\text{eq}} f_2^{\text{eq}} = e^{-(E_1+E_2)/T} = e^{-(E_a+E_b)/T} = f_a^{\text{eq}} f_b^{\text{eq}}$$

$$\Rightarrow \text{RHS} \sim - \int |\mathcal{M}_{ab \rightarrow 12}|^2 (f_a f_b - f_a^{\text{eq}} f_b^{\text{eq}}) d(\text{phase space})$$

Justification

RHS

Assume SM particles in thermal equilibrium Assumption 2

$$f_1 = f_1^{\text{eq}} = e^{-E_1/T} \quad (\text{Boltzmann distribution})$$

$$\Rightarrow f_1 f_2 = f_1^{\text{eq}} f_2^{\text{eq}} = e^{-(E_1+E_2)/T} = e^{-(E_a+E_b)/T} = f_a^{\text{eq}} f_b^{\text{eq}}$$

$$\Rightarrow \text{RHS} \sim - \int |\mathcal{M}_{ab \rightarrow 12}|^2 (f_a f_b - f_a^{\text{eq}} f_b^{\text{eq}}) d(\text{phase space})$$



$$n(t) = \frac{g}{(2\pi)^3} \int d^3p f(E, t)$$

$$\sigma = \frac{1}{\text{flux}} \int |\mathcal{M}|^2 d\text{LIPS}$$

$$\text{RHS} = -\langle \sigma v \rangle (n_a n_b - n_a^{\text{eq}} n_b^{\text{eq}})$$

$$\left(\text{Full Boltzmann eq: } \frac{dn}{dt} + 3Hn = -\langle \sigma v \rangle (n^2 - n_{\text{eq}}^2) \right)$$

Solving the Boltzmann equation

Boltzmann equation:

$$\frac{dn}{dt} + \underbrace{3Hn}_{\text{Number density reduced by the expansion of the Universe}} = -\langle\sigma v\rangle(n^2 - n_{\text{eq}}^2)$$

Number density reduced by the expansion of the Universe.
Hot to tell whether the dark matter production/destruction is efficient or not?

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Number density reduced by the expansion of the Universe.
Hot to tell whether the dark matter production/destruction is efficient or not?

Define “yield”:

$$Y \equiv \frac{n}{s} = \frac{\text{number density}}{\text{entropy density}}$$

If no entropy production,

$$\frac{dS}{dt} = 0 = \frac{d}{dt}(a^3 s) = a^3(\dot{s} + 3Hs)$$
$$\rightsquigarrow \dot{s} + 3Hs = 0$$

Solving the Boltzmann equation

Boltzmann equation:

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Time evolution of the yield:

$$\frac{dY}{dt} = \frac{1}{s^2}(\dot{n}s - n\dot{s}) = \frac{1}{s^2}(-3Hns - s\langle\sigma v\rangle(n^2 - n_{\text{eq}}^2) + n3HS)$$

$$\dot{n} = -3Hn - \langle\sigma v\rangle(n^2 - n_{\text{eq}}^2)$$

$$\dot{s} = -3Hs$$

Solving the Boltzmann equation

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$$\frac{dn}{dt} + \underbrace{3Hn}_{\text{expansion}} = -\langle\sigma v\rangle(n^2 - n_{\text{eq}}^2)$$

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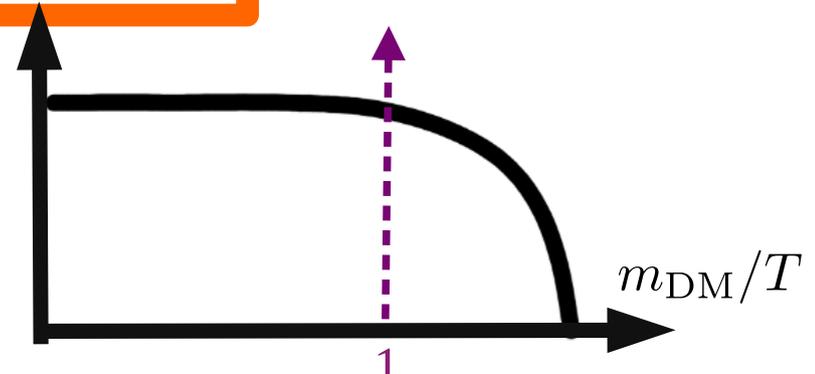
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Define “yield”:

$$Y \equiv \frac{n}{s} = \frac{\text{number density}}{\text{entropy density}}$$

$$\frac{dY}{dt} = -s\langle\sigma v\rangle(Y^2 - Y_{\text{eq}}^2)$$

$$Y_{\text{eq}} = \begin{cases} \sim \text{constant} & \text{if } T \gg m_{\text{DM}} \\ \sim \left(\frac{m_{\text{DM}}}{T}\right)^{3/2} e^{-m_{\text{DM}}/T} & \text{if } T \ll m_{\text{DM}} \end{cases}$$



Solving the Boltzmann equation

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$$\frac{dY}{dt} = -s\langle\sigma v\rangle(Y^2 - Y_{\text{eq}}^2)$$

If $\sigma=0$, then $Y = \text{constant}$

Solving the Boltzmann equation

Boltzmann equation:

$$\frac{dn}{dt} + \underbrace{3Hn}_{\text{expansion}} = -\langle\sigma v\rangle(n^2 - n_{\text{eq}}^2)$$

Number density reduced by the expansion of the Universe.
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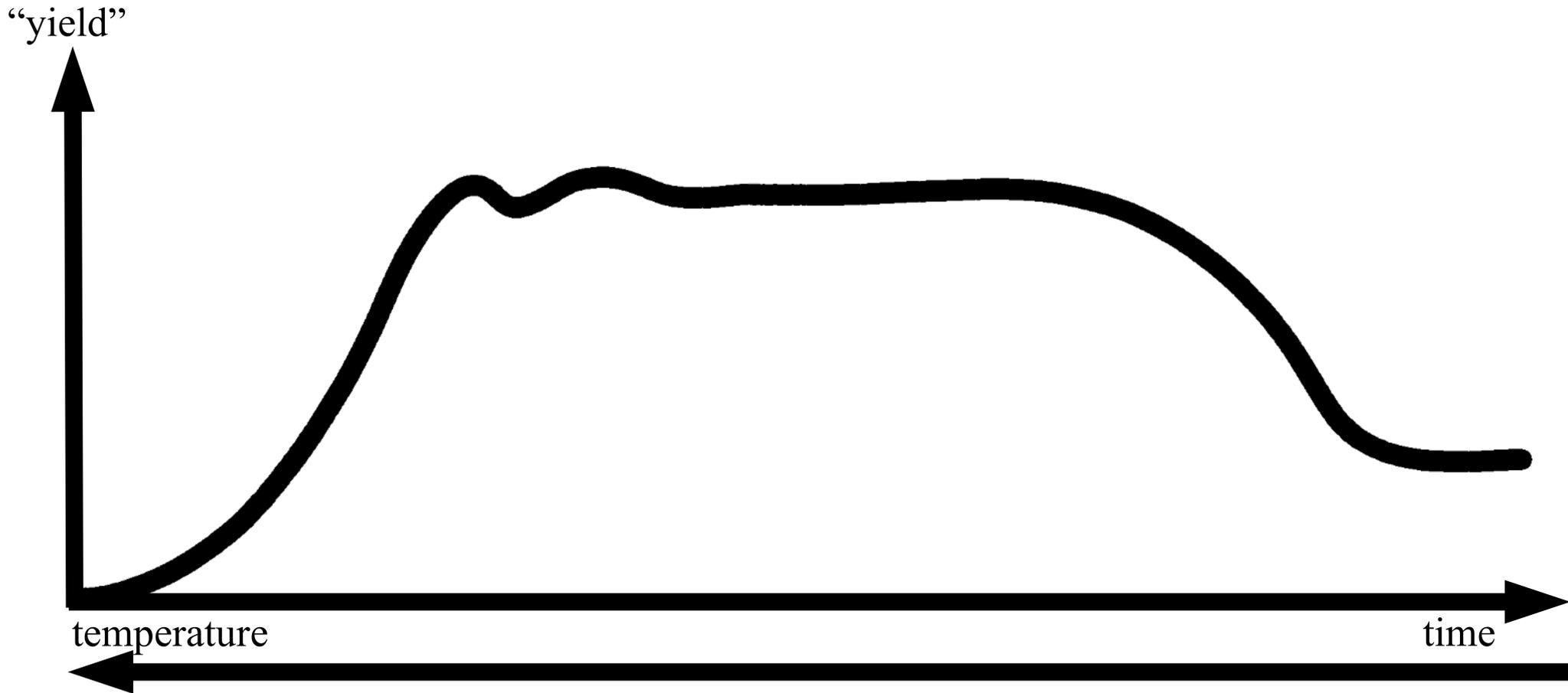
Define “yield”:

$$Y \equiv \frac{n}{s} = \frac{\text{number density}}{\text{entropy density}}$$

Define $x = \frac{m_{\text{DM}}}{T}$, $\Gamma_{\text{ann}} = n_{\text{eq}}\langle\sigma v\rangle$

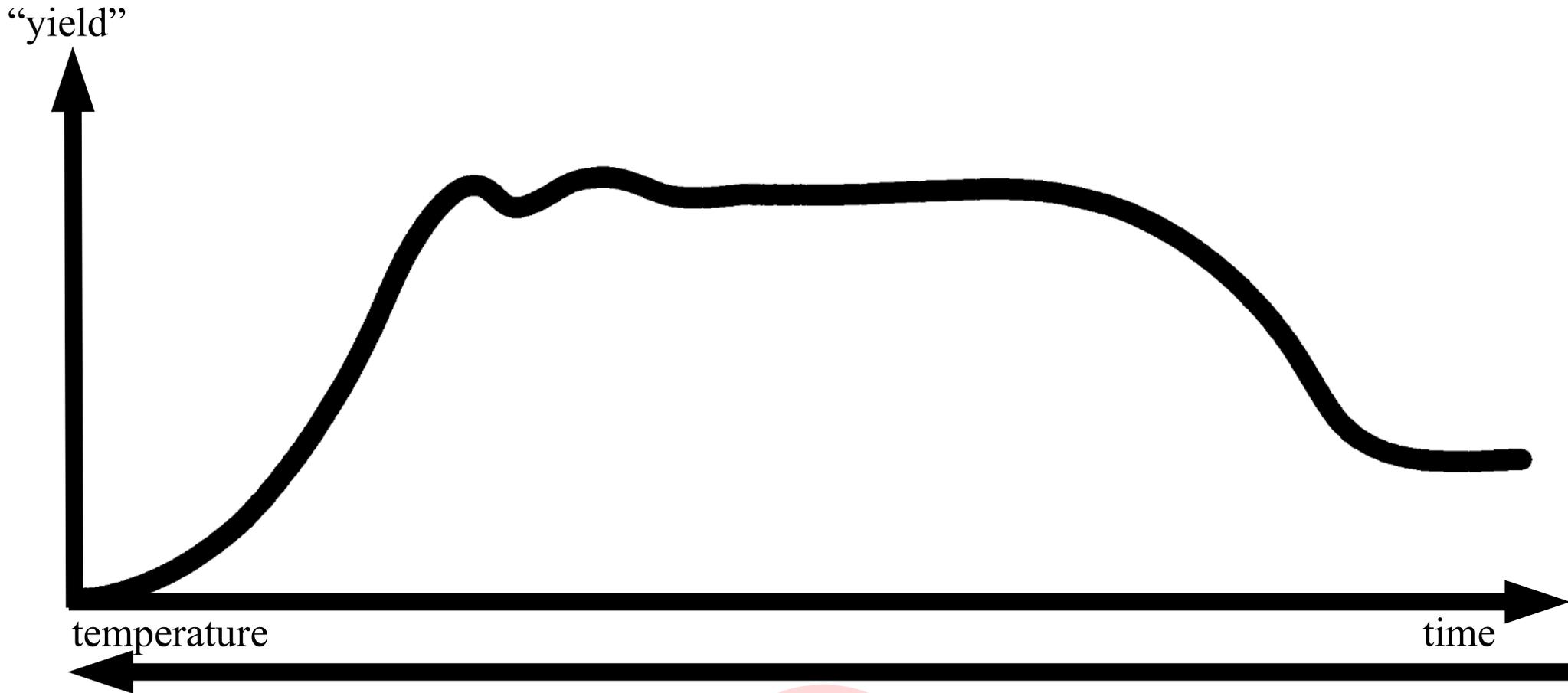
$$\frac{x}{Y_{\text{eq}}} \frac{dY}{dx} = -\frac{\Gamma_{\text{ann}}(x)}{H(x)} \left[\left(\frac{Y}{Y_{\text{eq}}} \right)^2 - 1 \right]$$

WIMP history (in a nutshell)



$$\frac{x}{Y_{\text{eq}}} \frac{dY}{dx} = - \frac{\Gamma_{\text{ann}}(x)}{H(x)} \left[\left(\frac{Y}{Y_{\text{eq}}} \right)^2 - 1 \right]$$

WIMP history (in a nutshell)



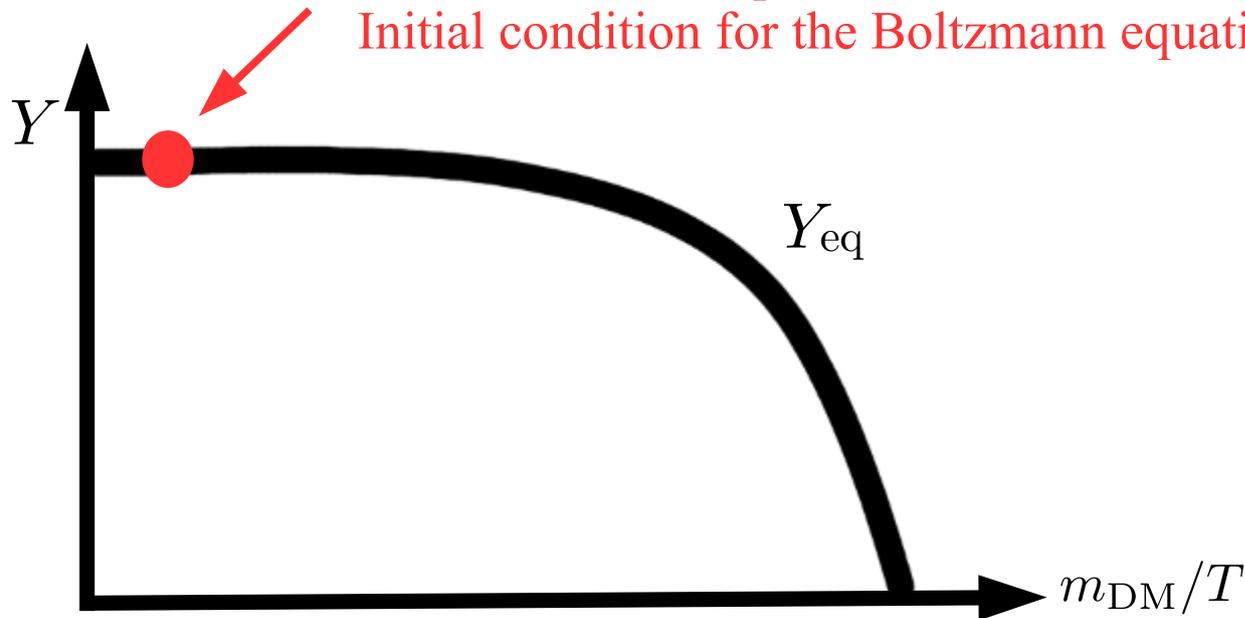
$$\frac{x}{Y_{\text{eq}}} \frac{dY}{dx} = - \frac{\Gamma_{\text{ann}}(x)}{H(x)} \left[\left(\frac{Y}{Y_{\text{eq}}} \right)^2 - 1 \right]$$

Qualitative behavior of the solution

1) Solution at very early times ($x \ll 1$, or $T \gg m_{\text{DM}}$)

$$\frac{x}{Y_{\text{eq}}} \frac{dY}{dx} = - \frac{\Gamma_{\text{ann}}(x)}{H(x)} \left[\left(\frac{Y}{Y_{\text{eq}}} \right)^2 - 1 \right]$$

Assume that at early times the DM reached thermal equilibrium.
Initial condition for the Boltzmann equation

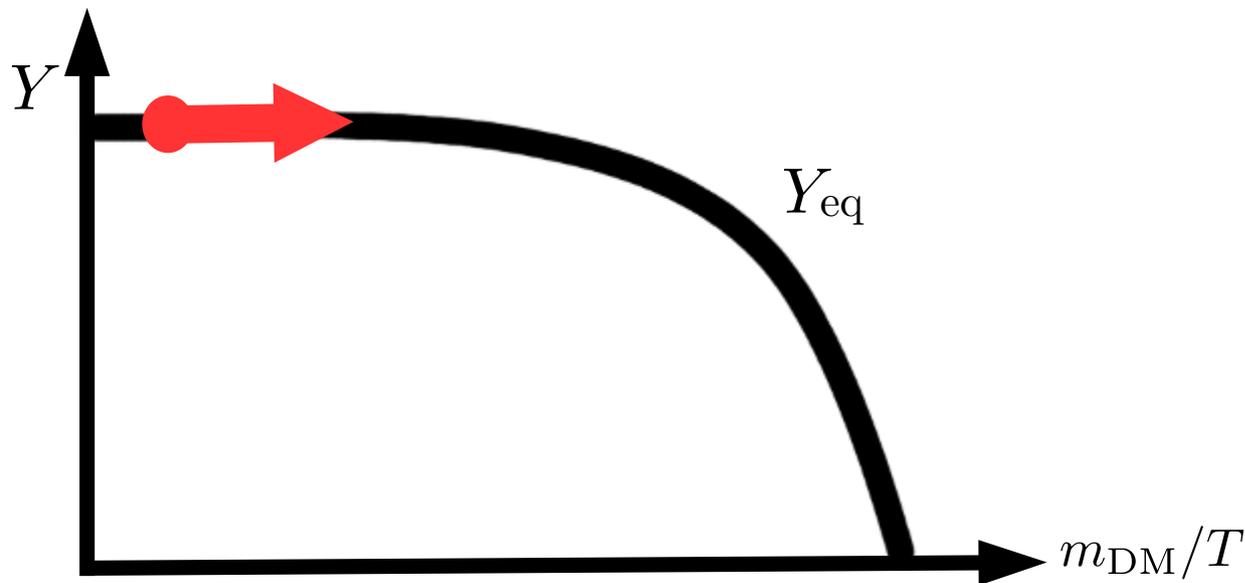


Qualitative behavior of the solution

1) Solution at very early times ($x \ll 1$, or $T \gg m_{\text{DM}}$)

$$\frac{x}{Y_{\text{eq}}} \frac{dY}{dx} = - \frac{\Gamma_{\text{ann}}(x)}{H(x)} \left[\left(\frac{Y}{Y_{\text{eq}}} \right)^2 - 1 \right] \simeq 0$$

The yield follows the equilibrium distribution

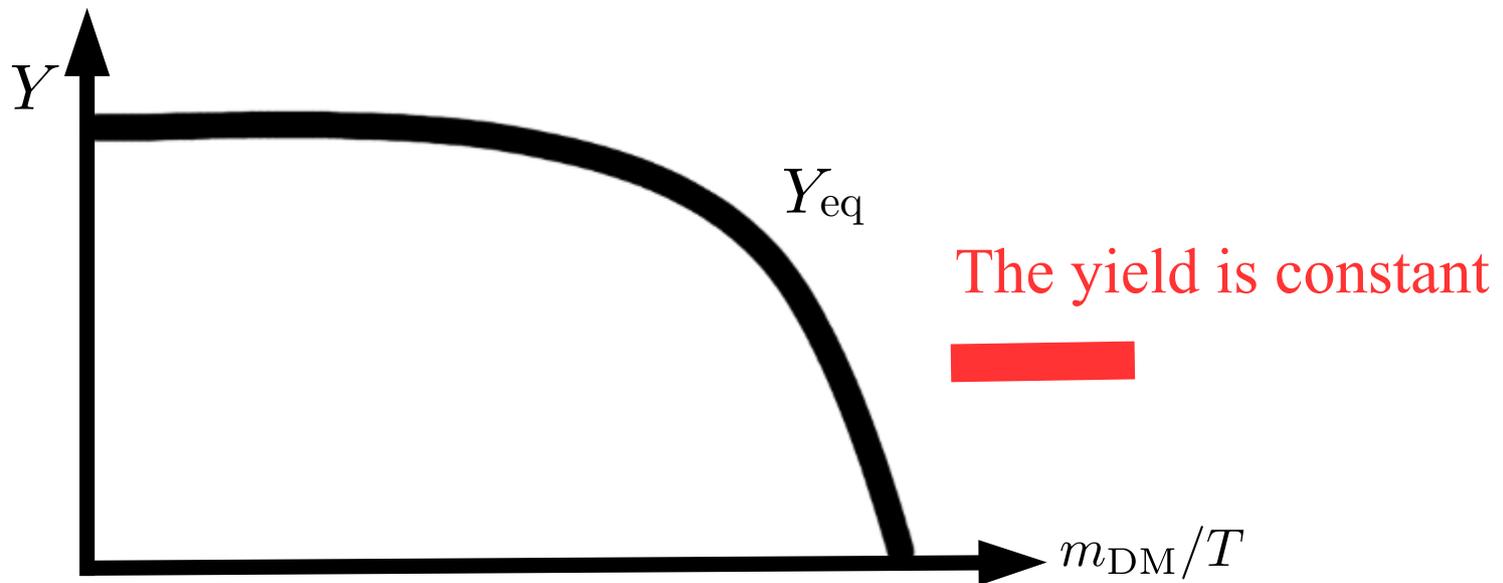


Qualitative behavior of the solution

2) Solution at very early times ($x \gg 1$, or $T \ll m_{\text{DM}}$)

$$\frac{x}{Y_{\text{eq}}} \frac{dY}{dx} = - \frac{\Gamma_{\text{ann}}(x)}{H(x)} \left[\left(\frac{Y}{Y_{\text{eq}}} \right)^2 - 1 \right] \simeq 0$$

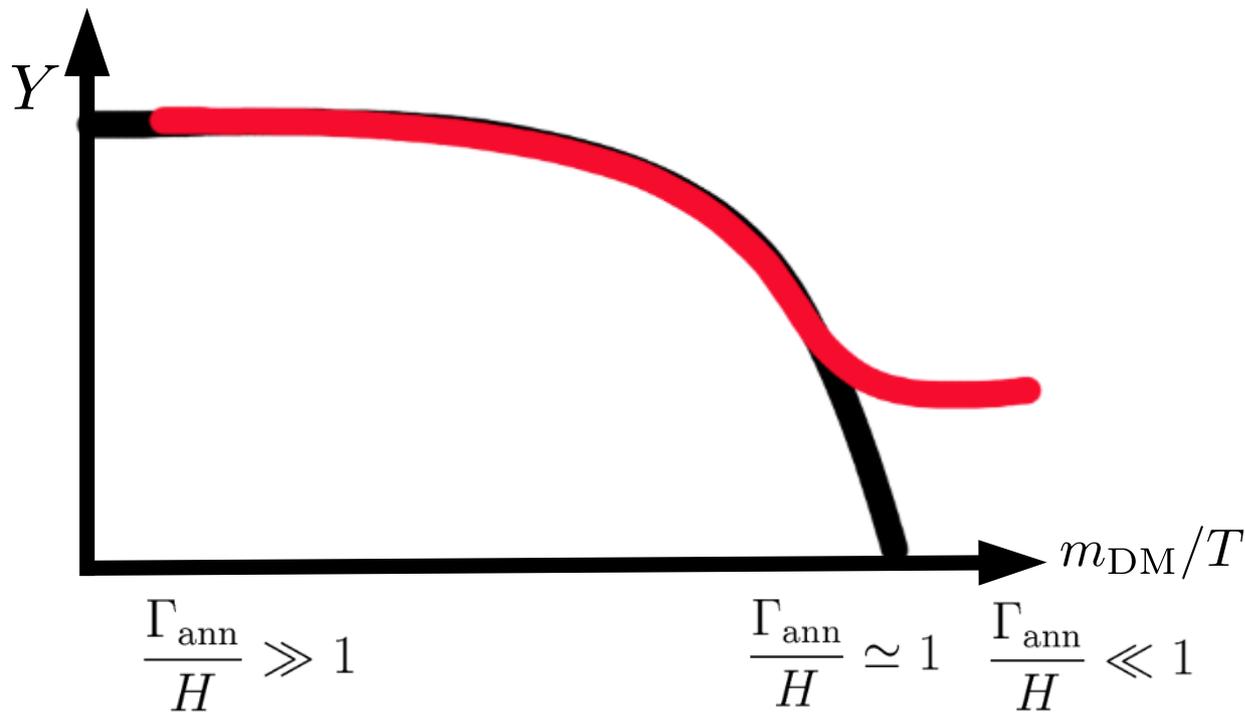
$$\Gamma_{\text{ann}} = n_{\text{eq}} \langle \sigma v \rangle \text{ small (compared to } H)$$



Qualitative behavior of the solution

3) Extrapolation between the two regimes

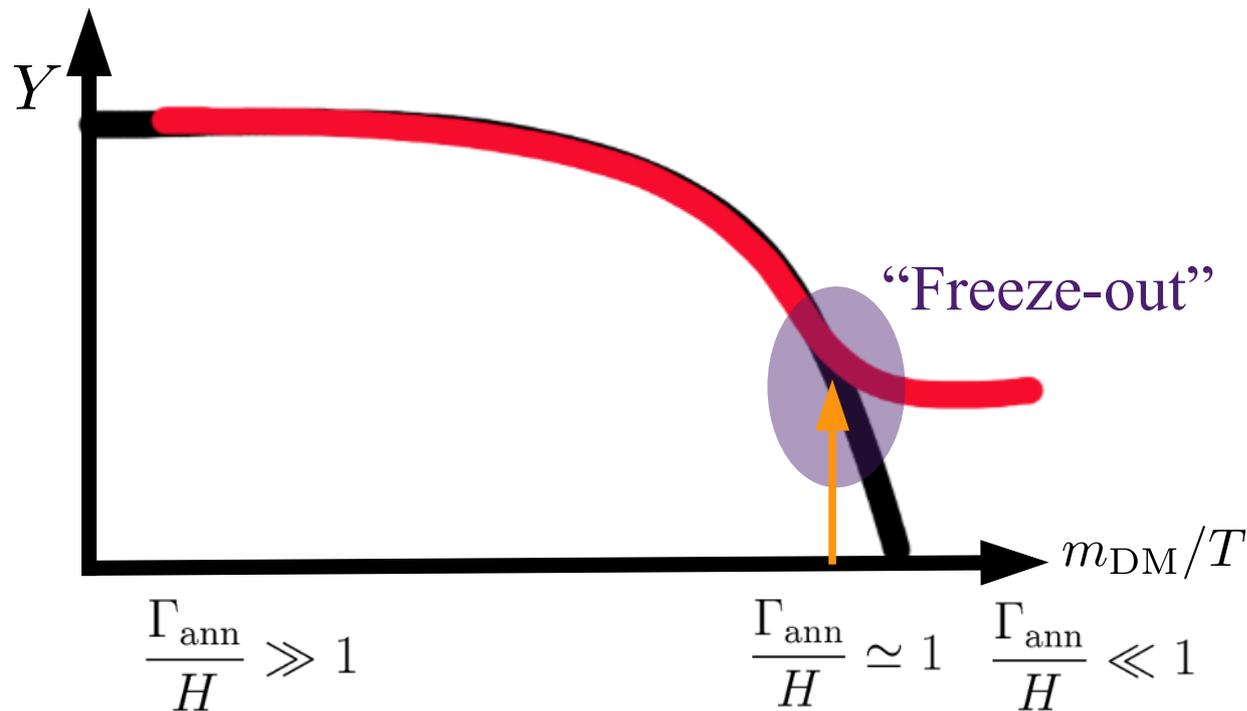
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Qualitative behavior of the solution

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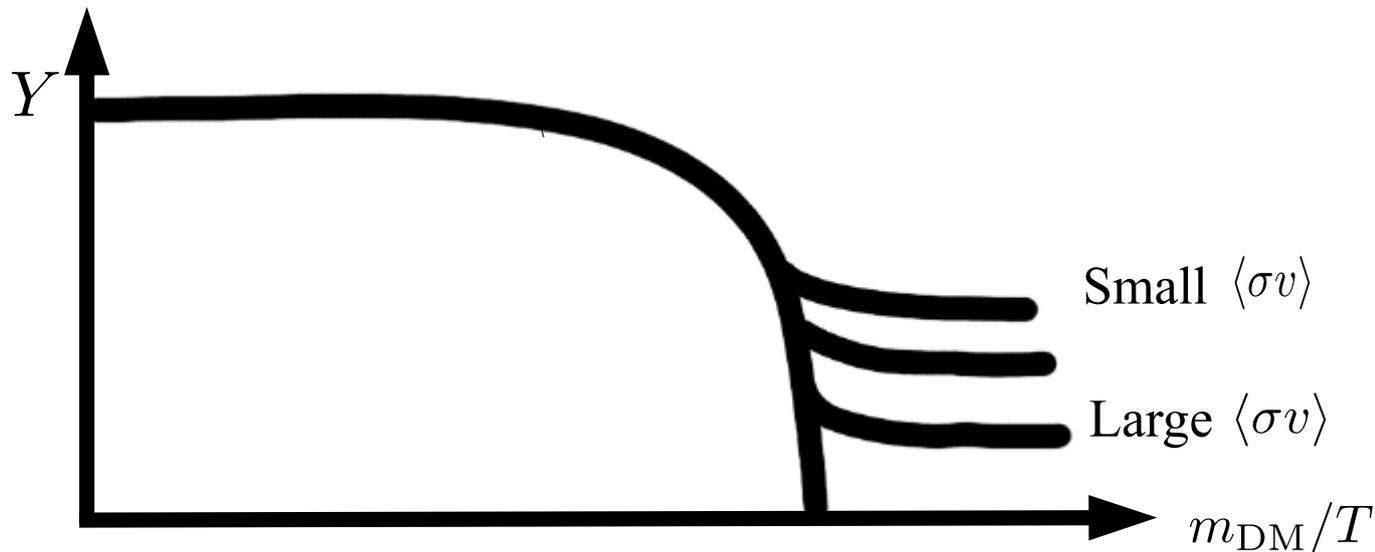
$$\frac{x}{Y_{\text{eq}}} \frac{dY}{dx} = -\frac{\Gamma_{\text{ann}}(x)}{H(x)} \left[\left(\frac{Y}{Y_{\text{eq}}} \right)^2 - 1 \right] \simeq 0$$



Number density of WIMPs at freeze-out

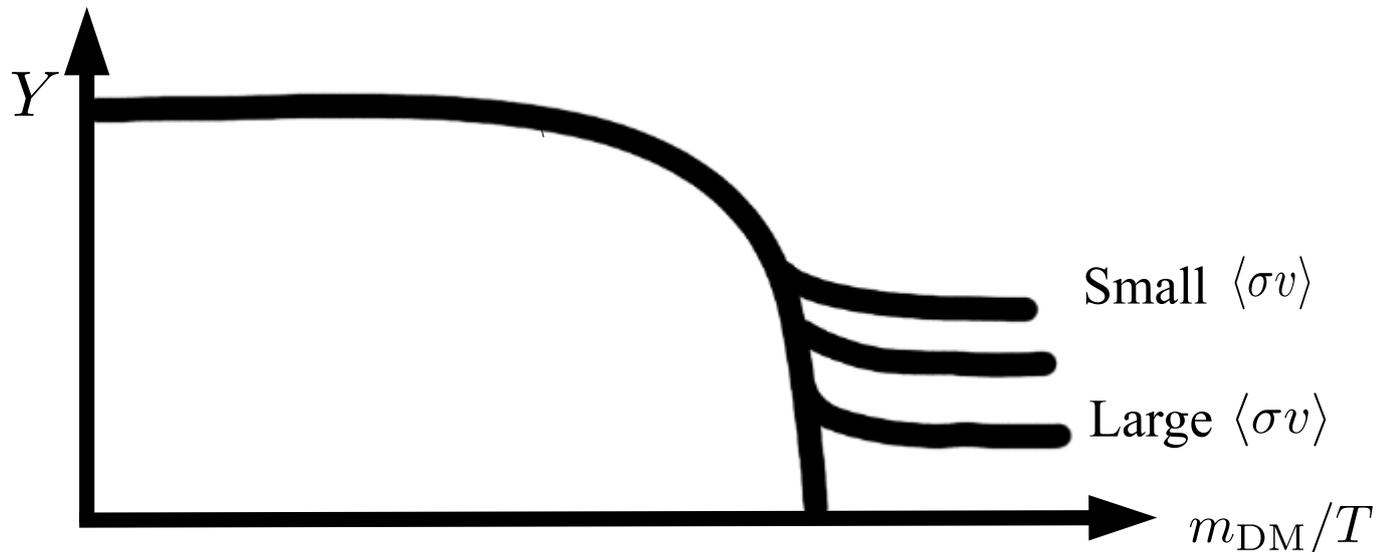
$$n_{\text{eq}}(T_{\text{fo}}) = \frac{H(T_{\text{fo}})}{\langle \sigma v \rangle \Big|_{\text{fo}}}$$

IMPORTANT: the number density of WIMPs at freeze-out is inversely proportional to the annihilation cross section



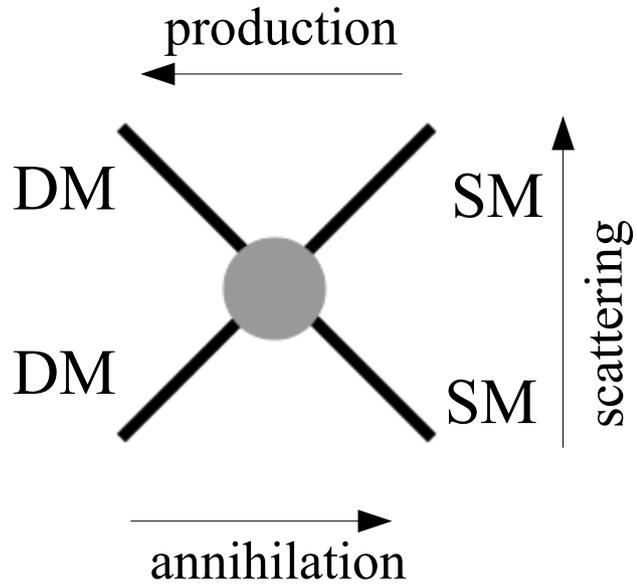
Density parameter of WIMPs today

$$\Omega_{\text{DM}} h^2 \simeq \frac{3 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}}{\langle \sigma v \rangle \Big|_{\text{fo}}}$$



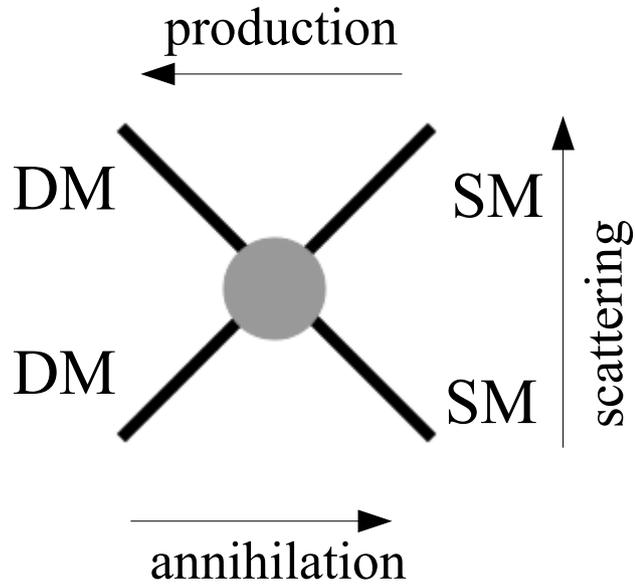
Main results from this part

WIMP dark matter



Main results from this part

WIMP dark matter

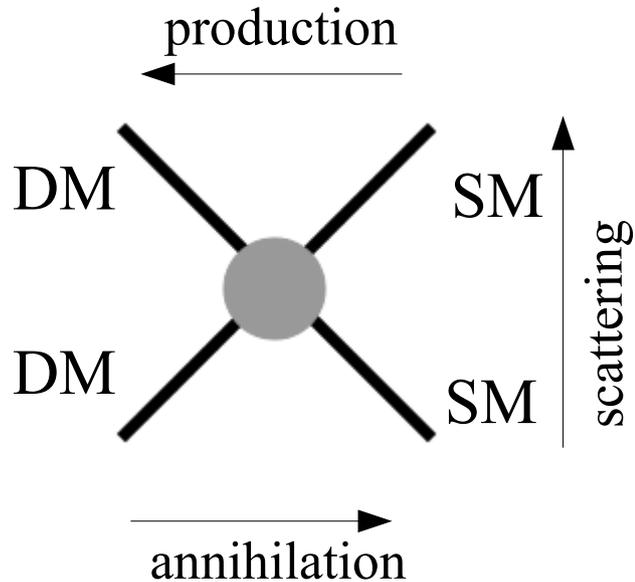


Relic abundance of DM particles

$$\Omega h^2 \simeq \frac{3 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}}{\langle \sigma v \rangle}$$

Main results from this part

WIMP dark matter



Relic abundance of DM particles

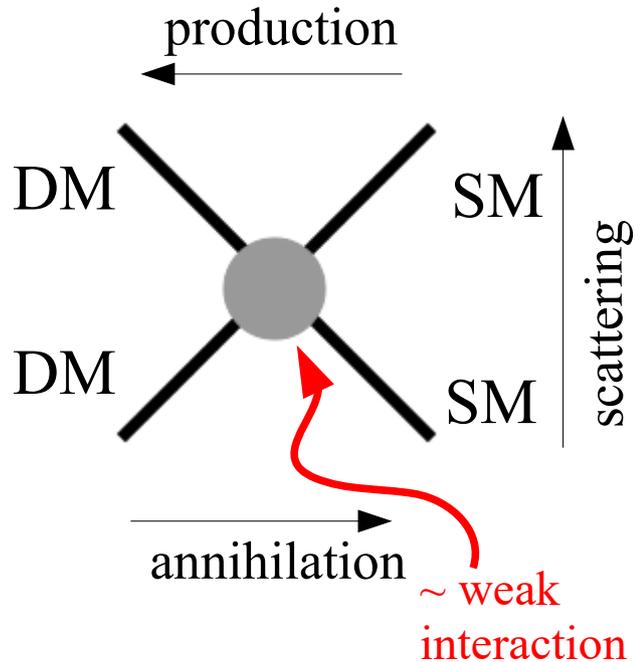
$$\Omega h^2 \simeq \frac{3 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}}{\langle \sigma v \rangle}$$

Correct DM abundance $\Omega h^2 = 0.12$ if

$$\langle \sigma v \rangle \simeq 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1} = 1 \text{ pb} \cdot c$$

Main results from this part

WIMP dark matter



Relic abundance of DM particles

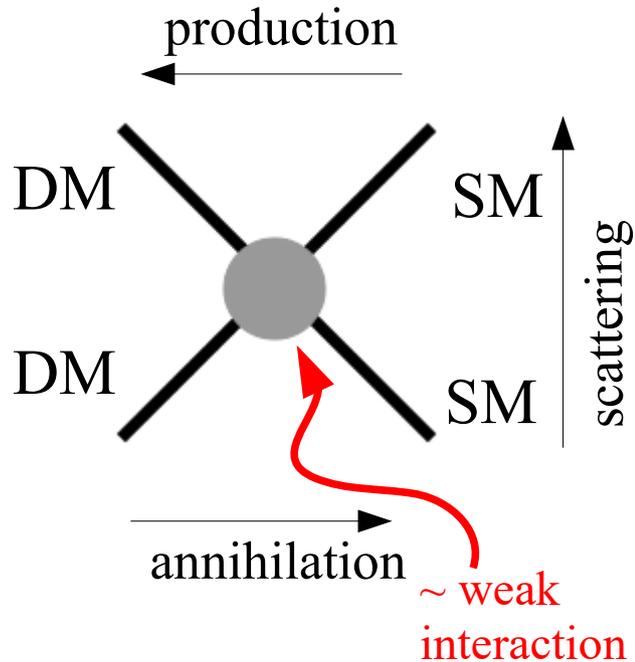
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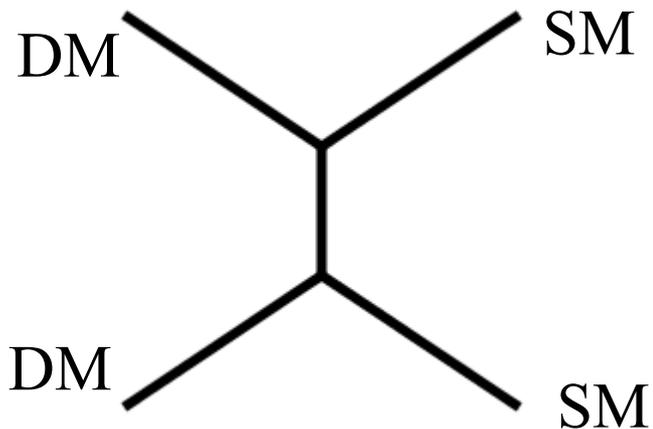


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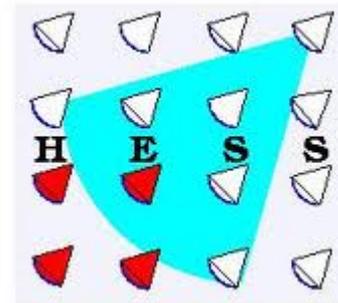
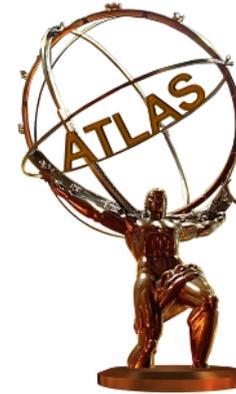
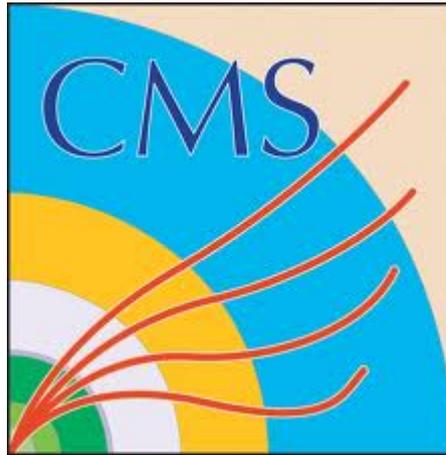
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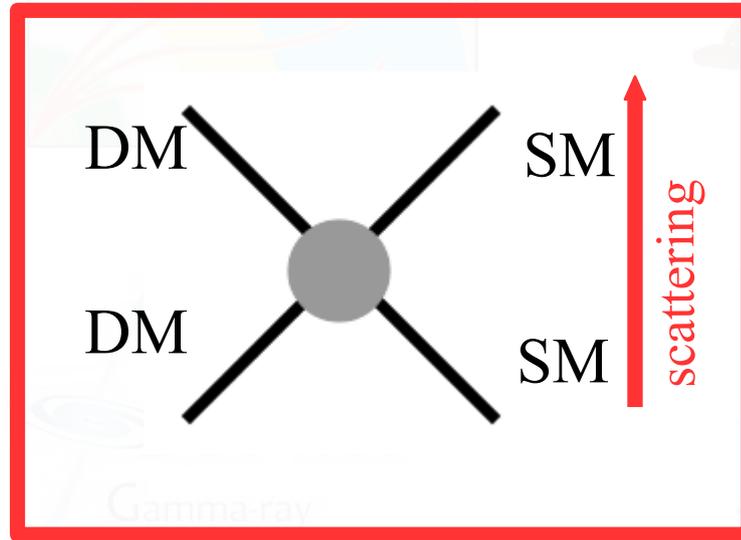


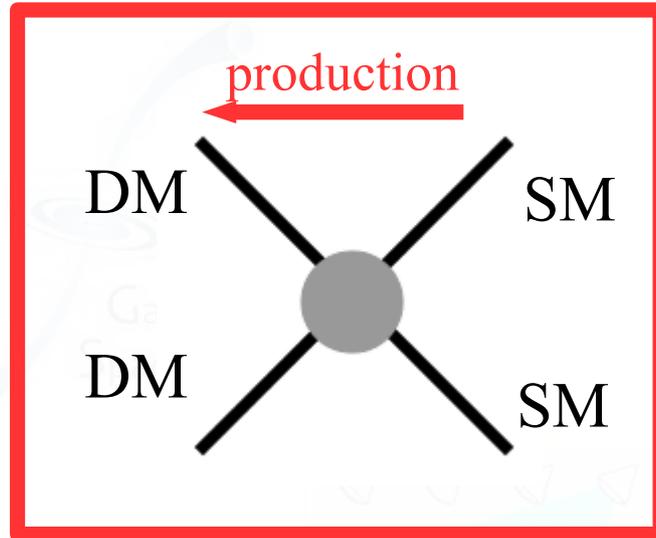
$$\sigma \sim \frac{g^4}{m_{\text{DM}}^2} = 1 \text{ pb}$$

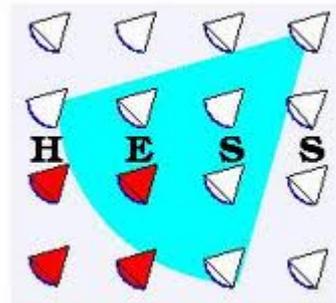
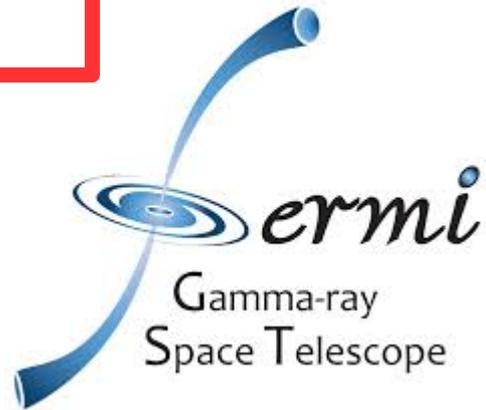
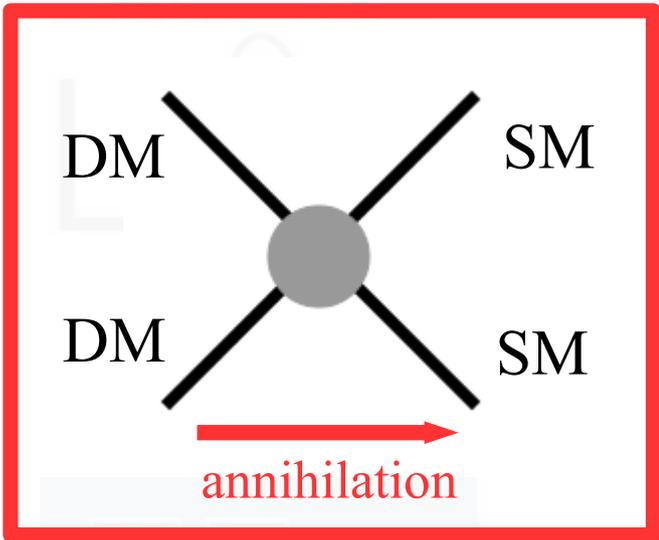
$$m_{\text{DM}} \sim 10 \text{ GeV} - 1 \text{ TeV}$$

(provided $g \sim g_{\text{weak}} \sim 0.1$)

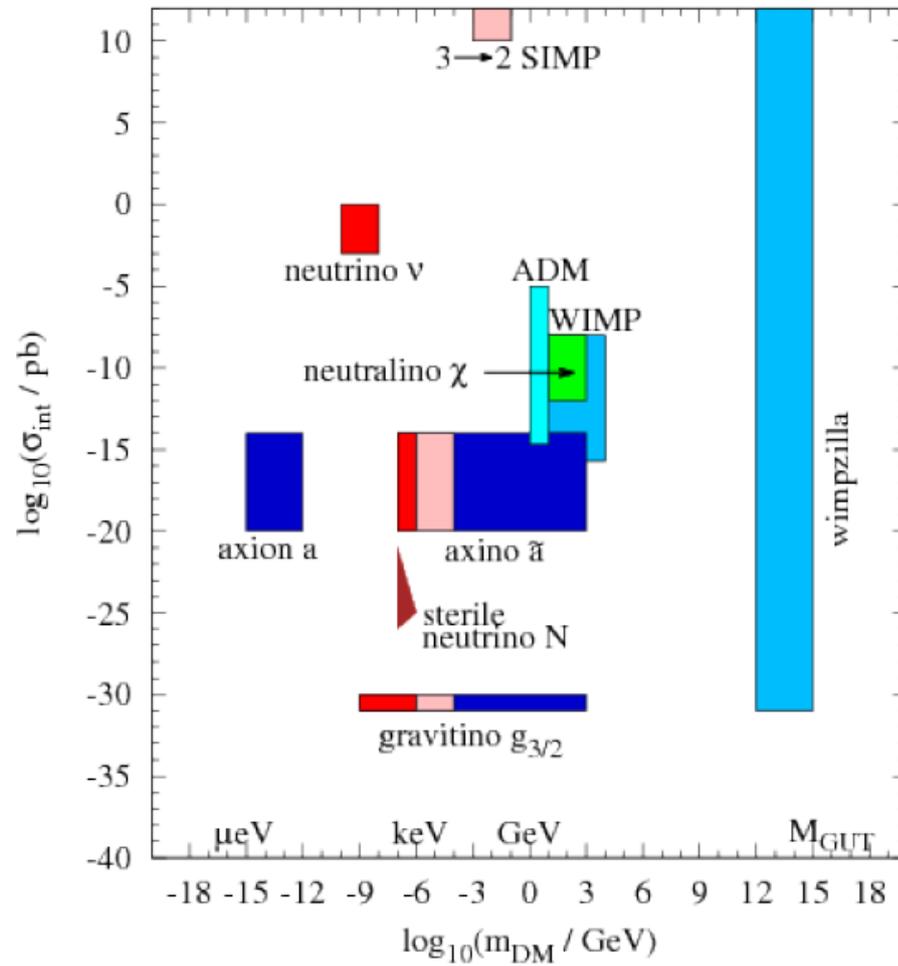




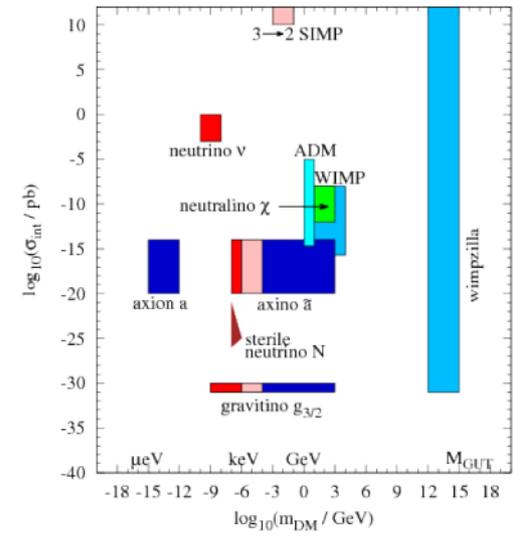
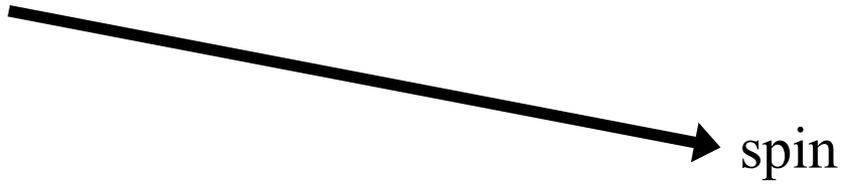




The WIMP zoo



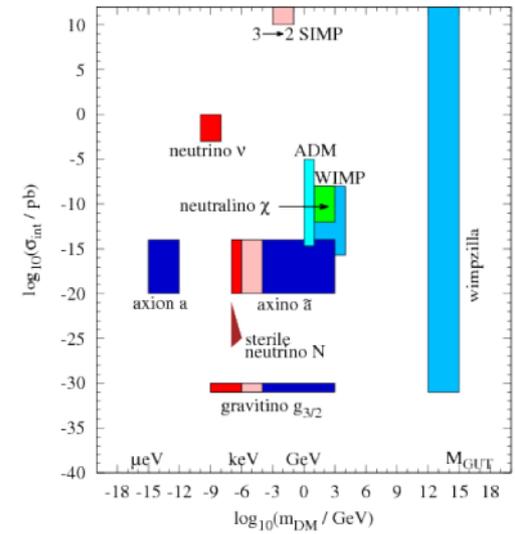
The WIMP zoo



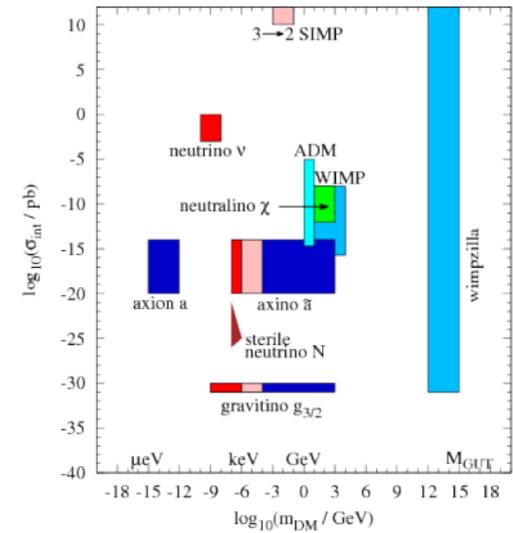
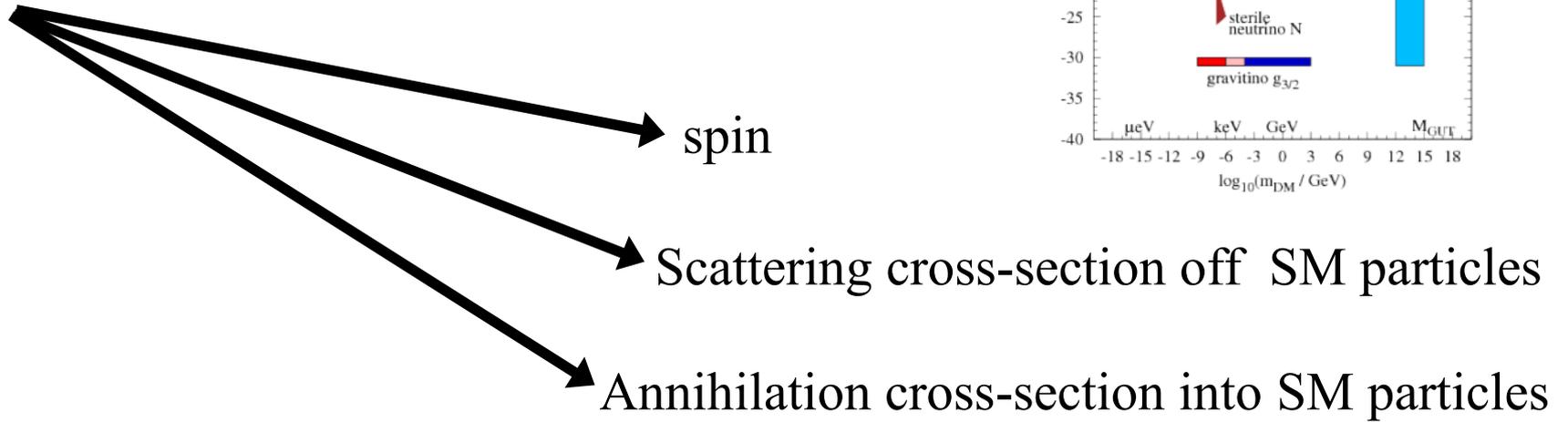
The WIMP zoo

spin

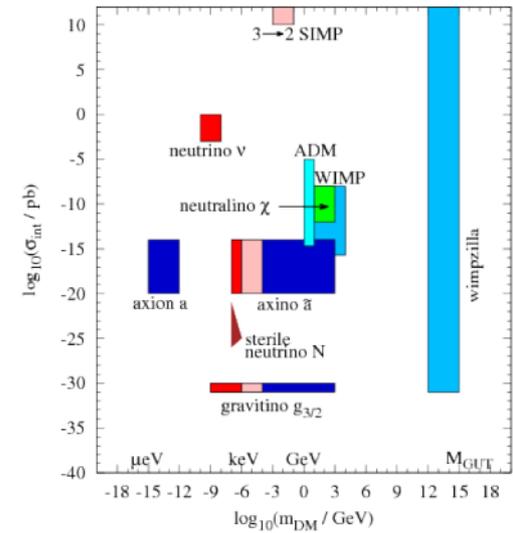
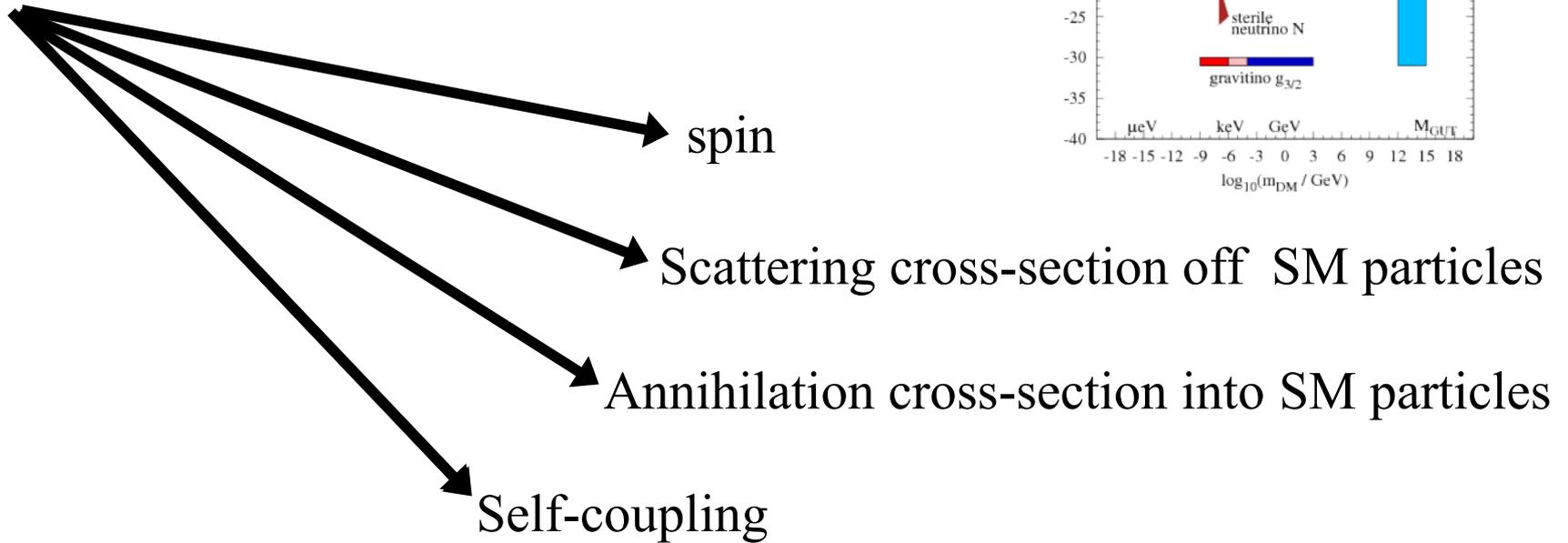
Scattering cross-section off SM particles



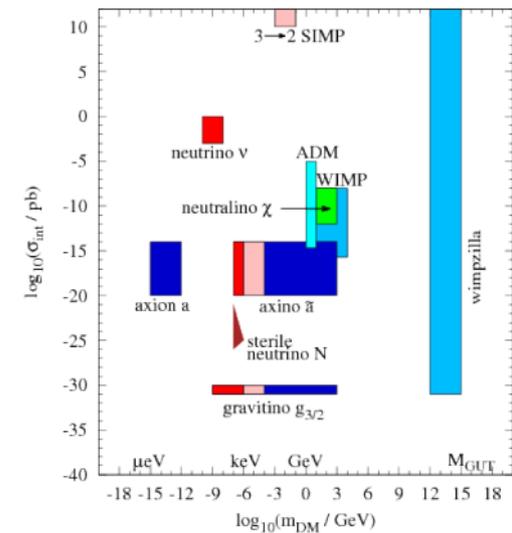
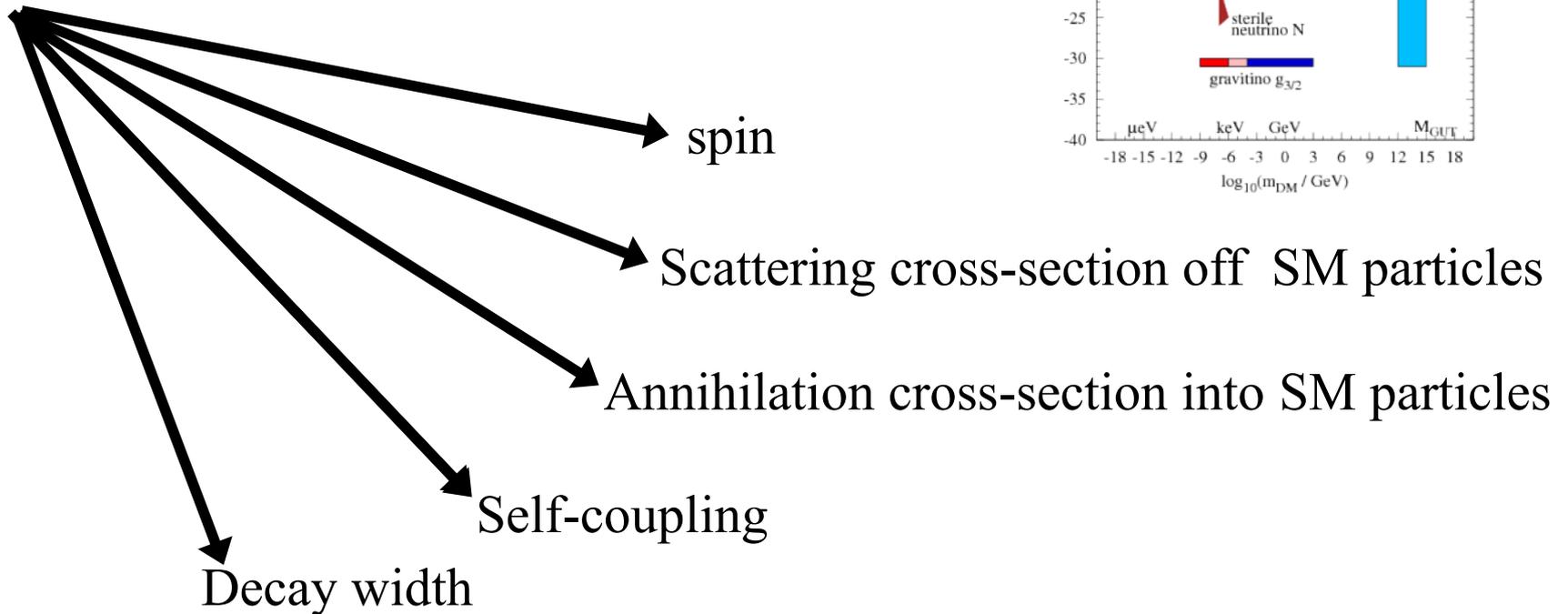
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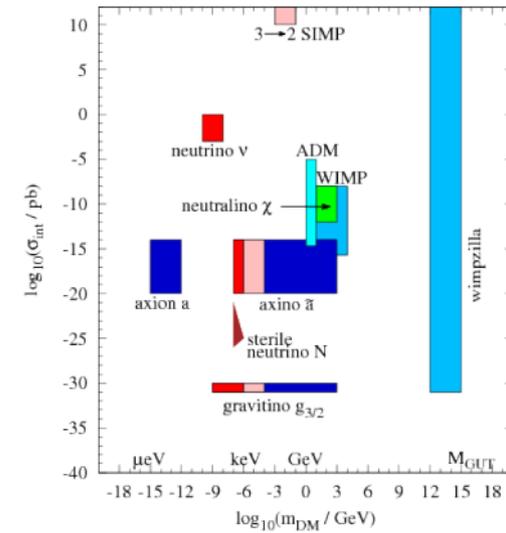
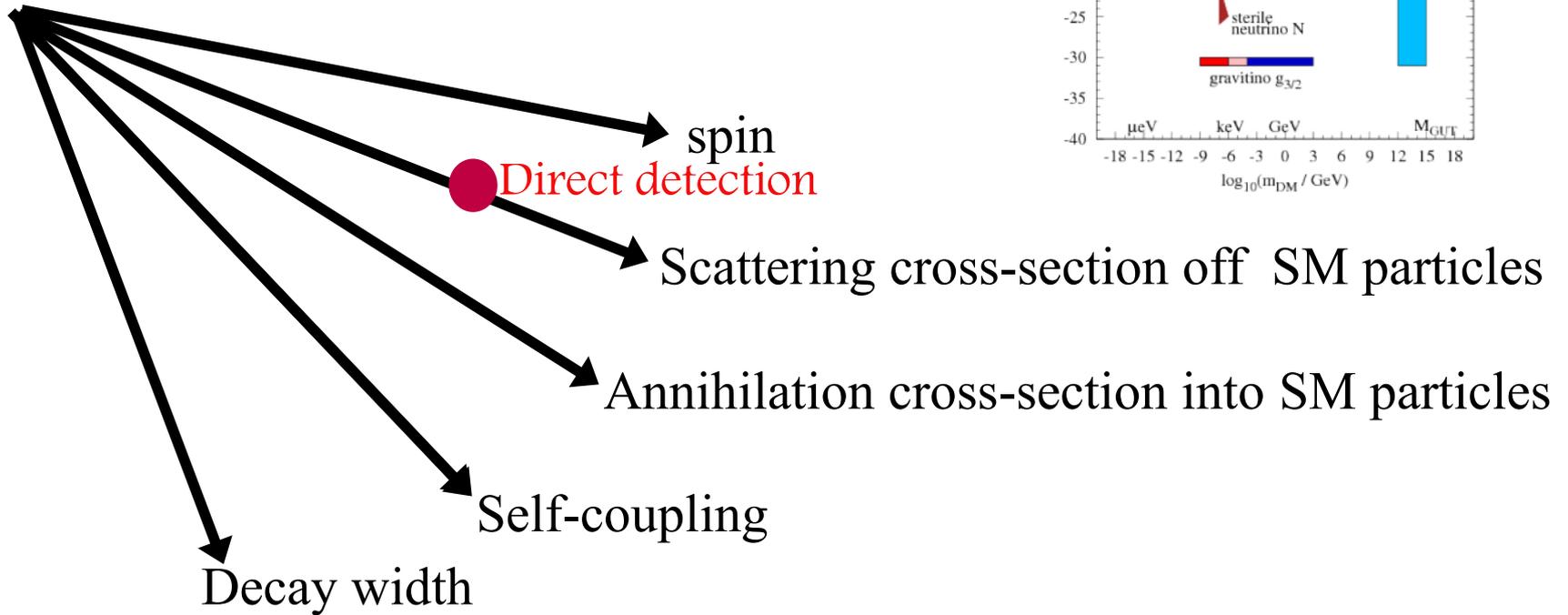
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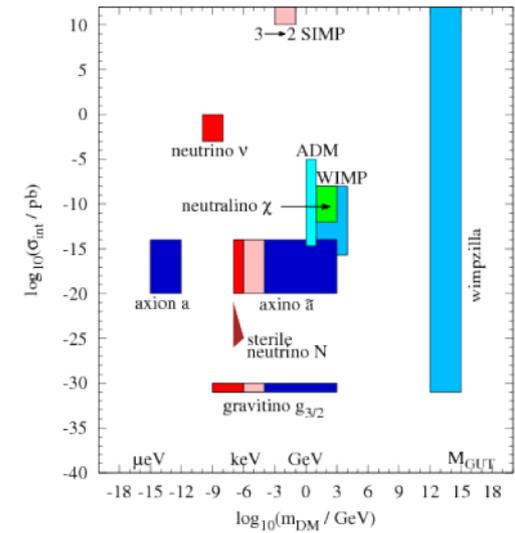
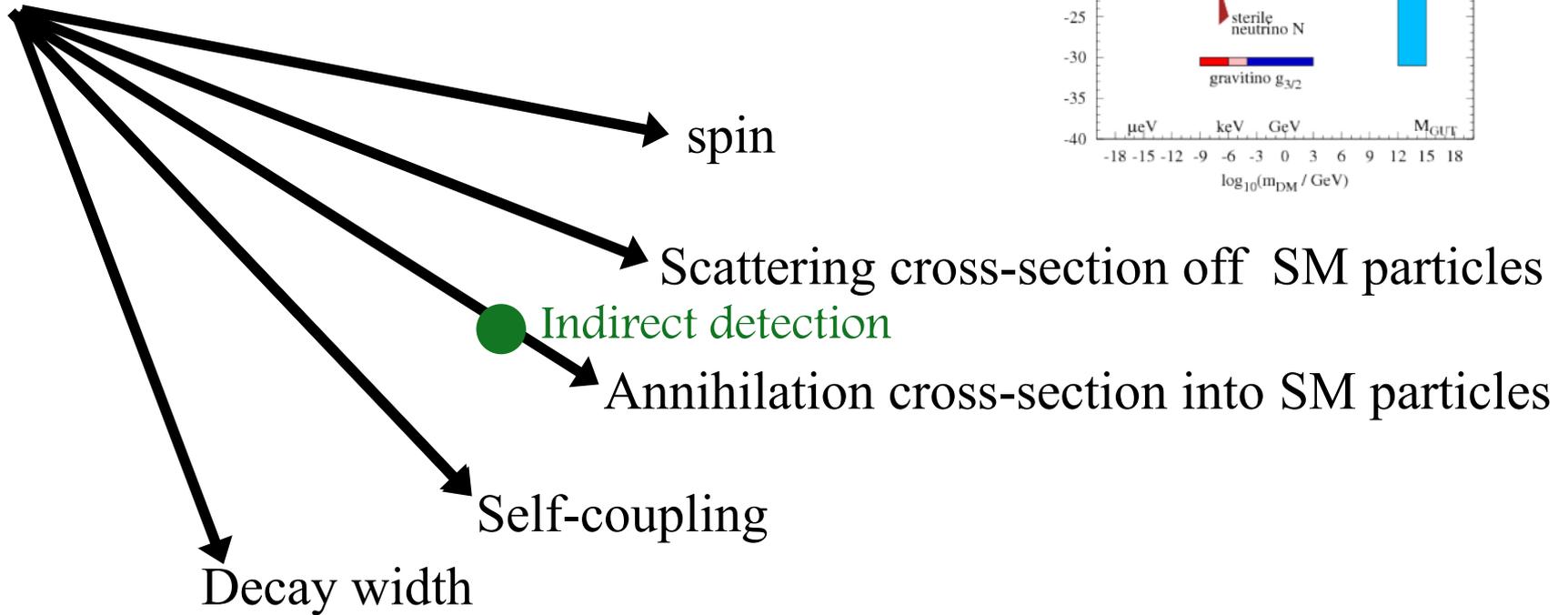
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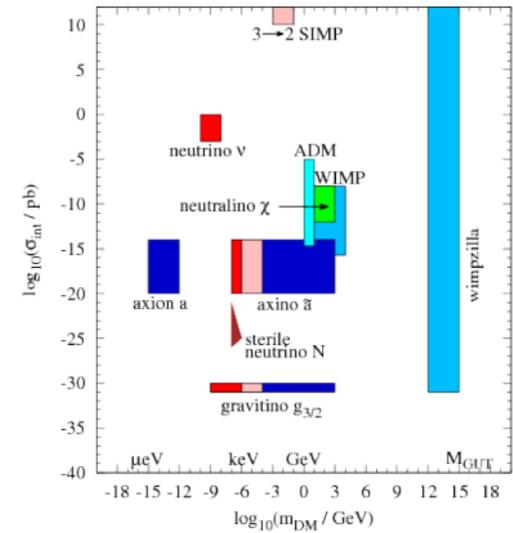
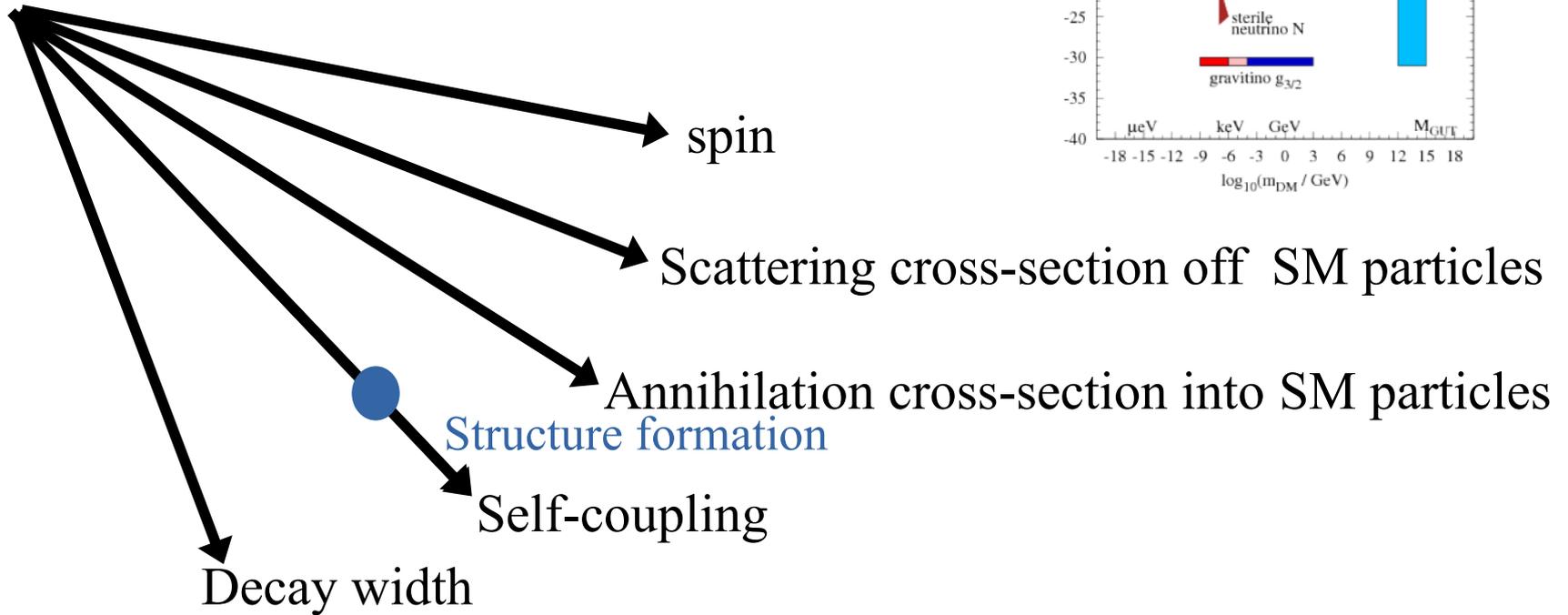
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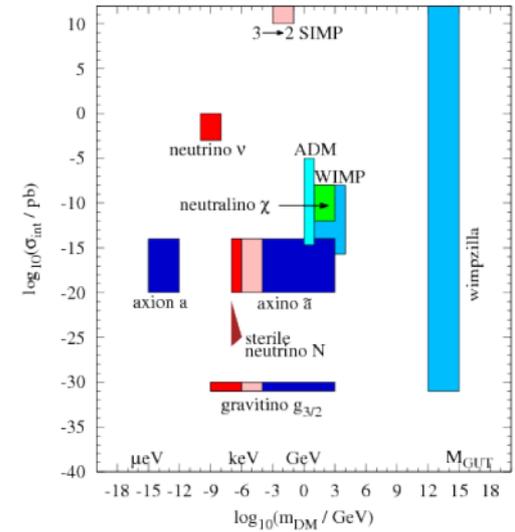
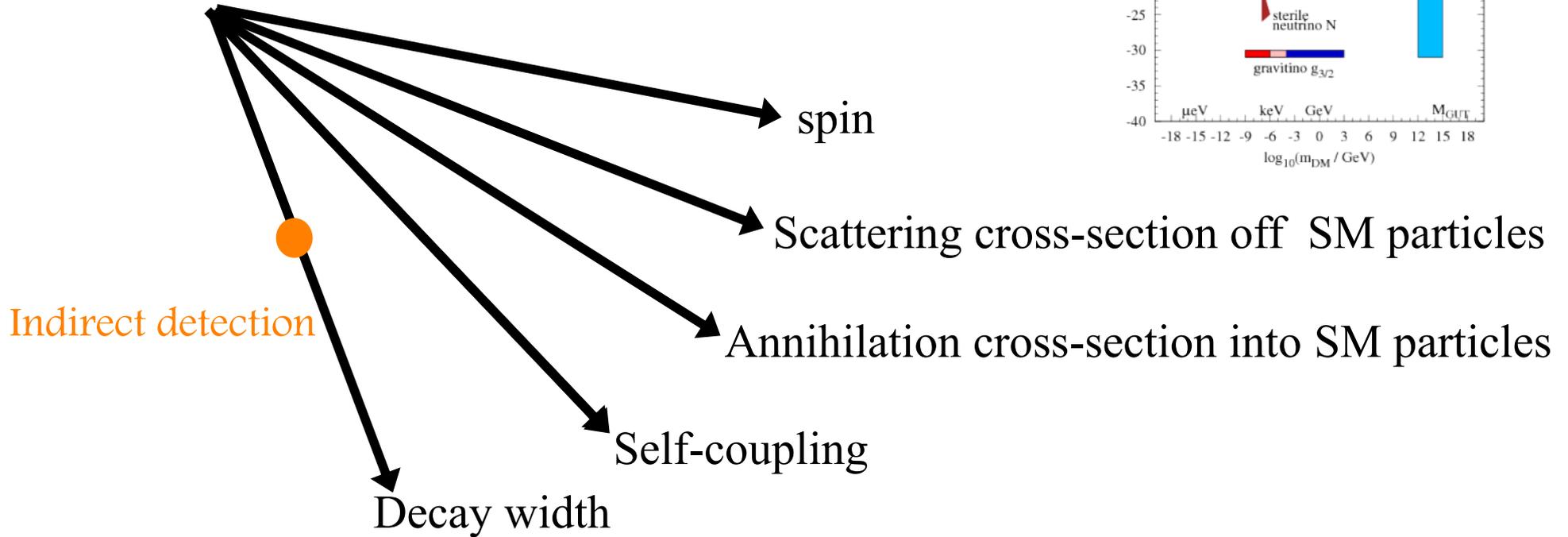
The WIMP zoo



The WIMP zoo

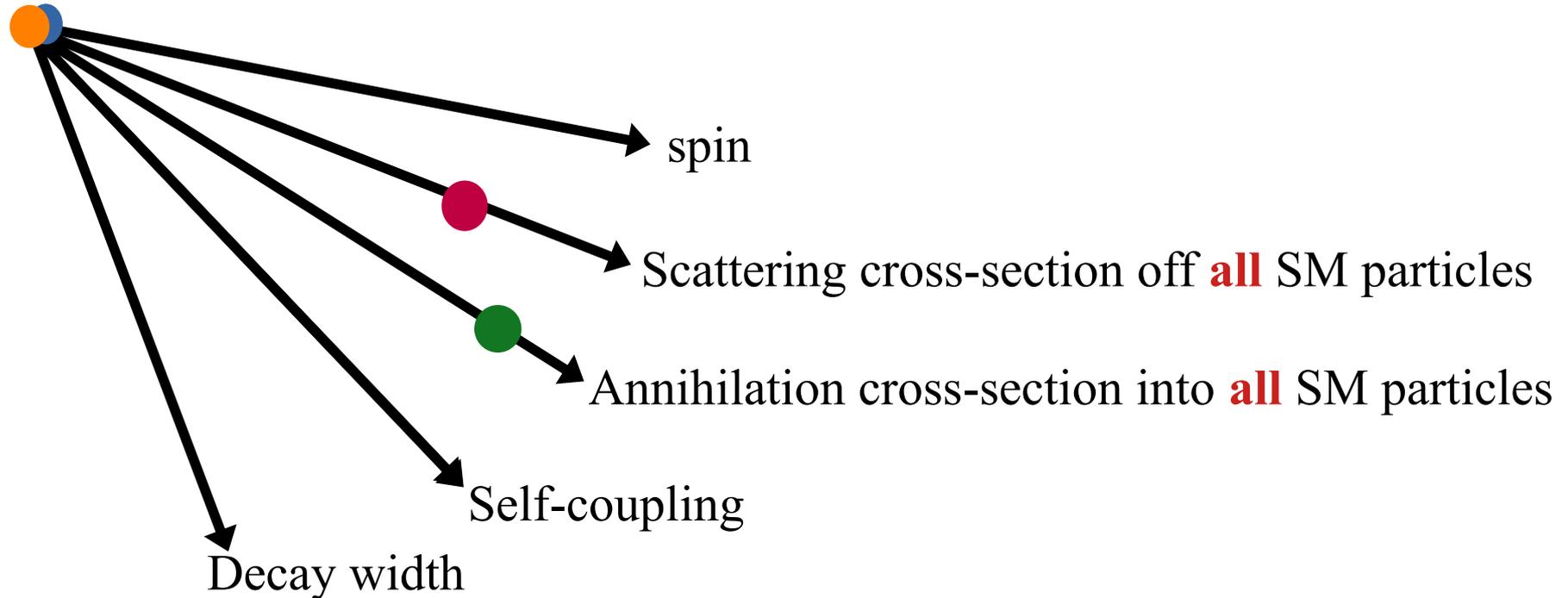


The WIMP zoo



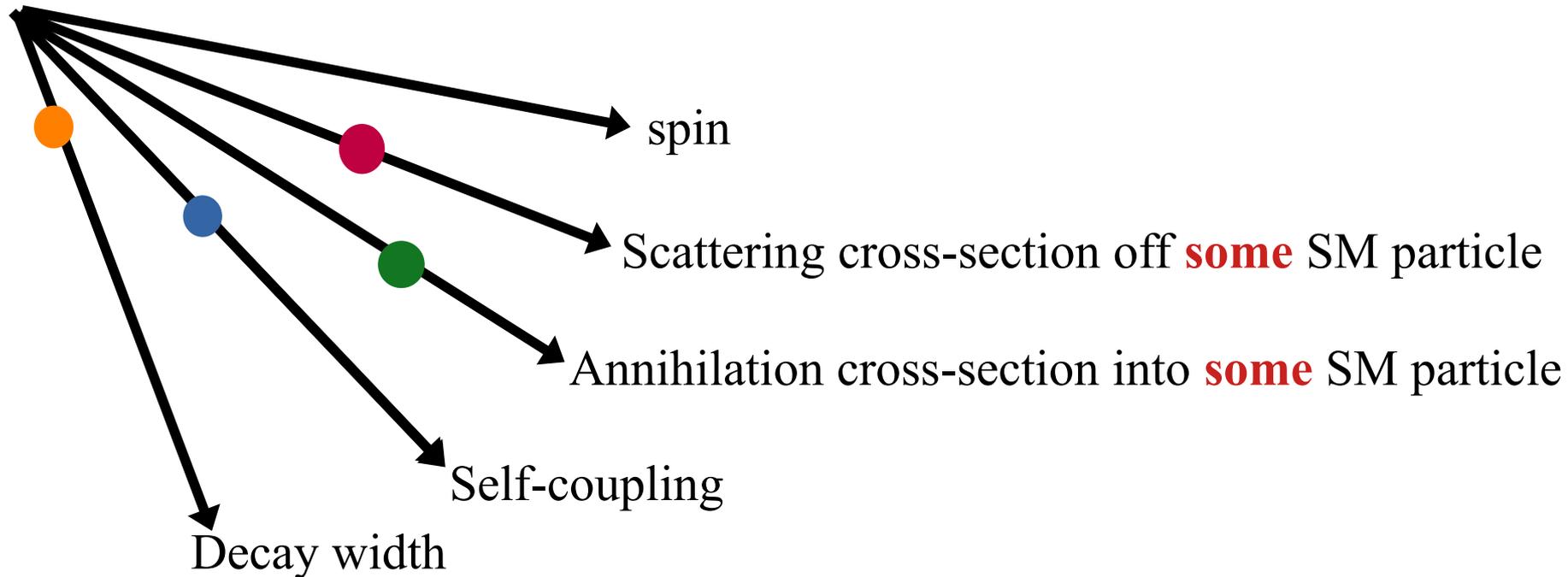
The WIMP zoo

Traditional dark matter searches optimized to detect the lightest neutralino of the Minimal Supersymmetric Standard Model.



The WIMP zoo

Traditional dark matter searches optimized to detect the lightest neutralino of the Minimal Supersymmetric Standard Model.

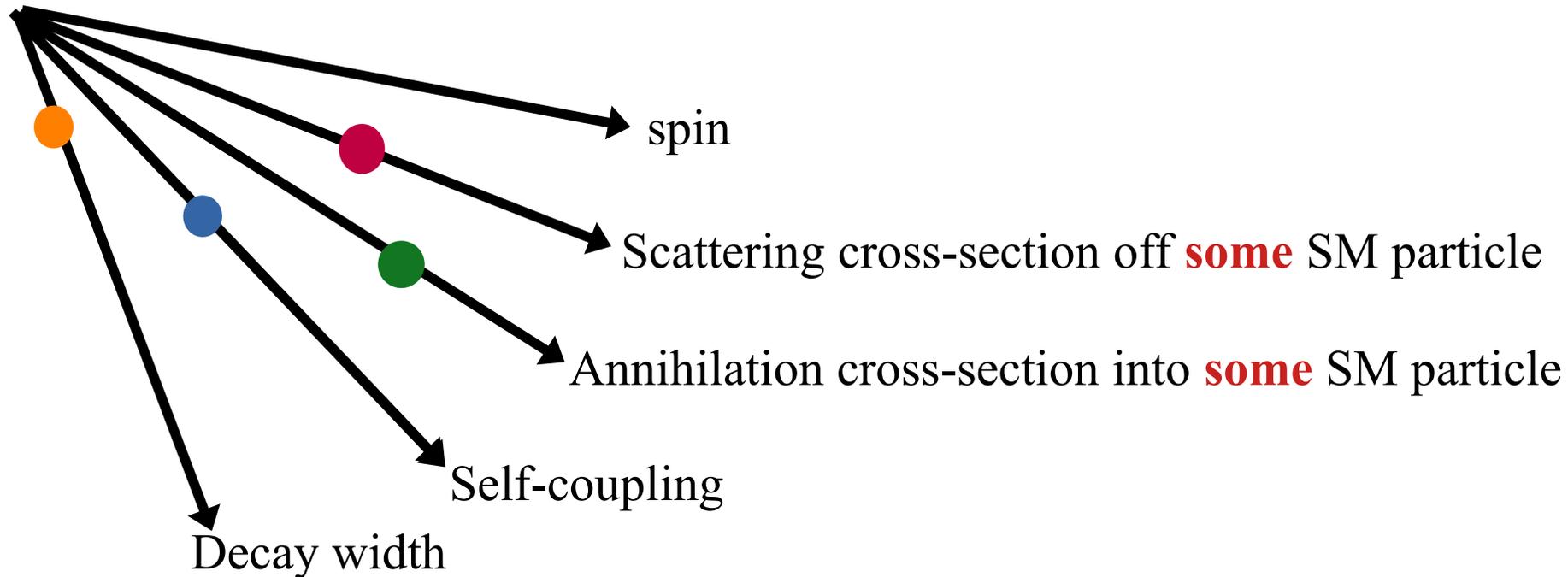


Modern approach:

- Be agnostic about the model.
- Identify distinct DM signals that allow to explore as much parameter space as possible.

The WIMP zoo

Traditional dark matter searches optimized to detect the lightest neutralino of the Minimal Supersymmetric Standard Model.

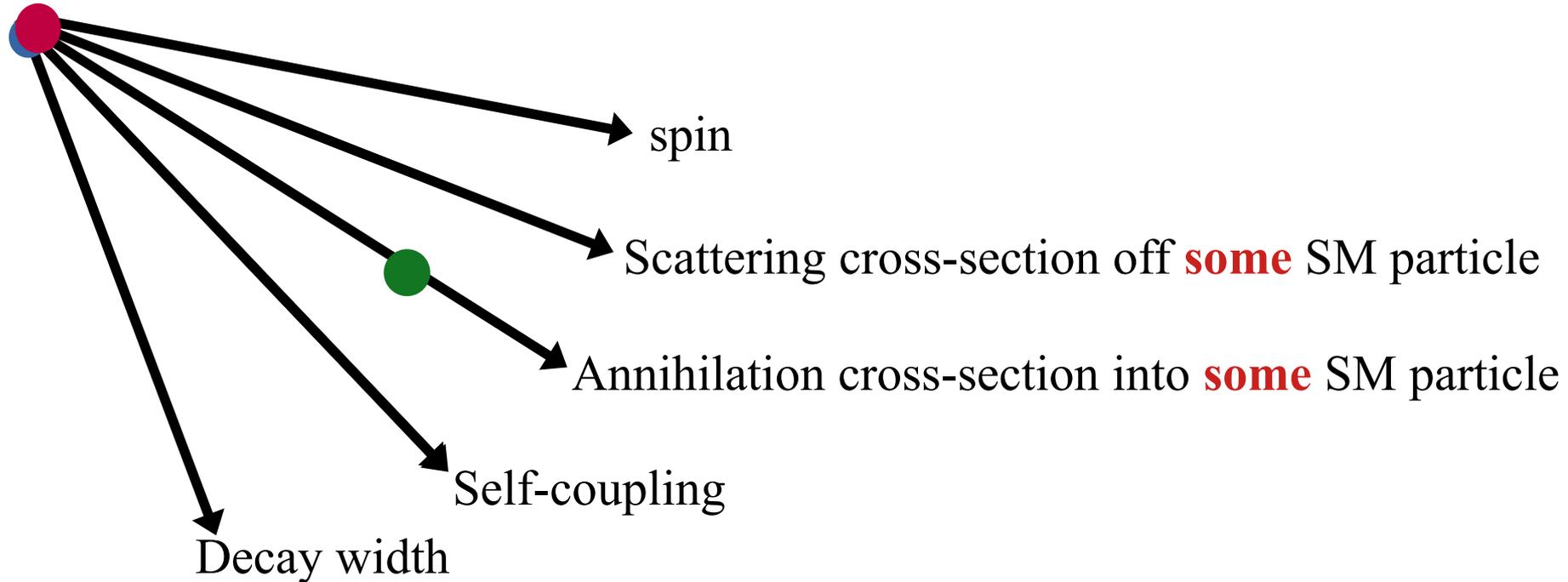


Modern approach:

- Be agnostic about the model.
- Identify distinct DM signals that allow to explore as much parameter space as possible.

No stone must be left unturned!

Probing the annihilation cross-section

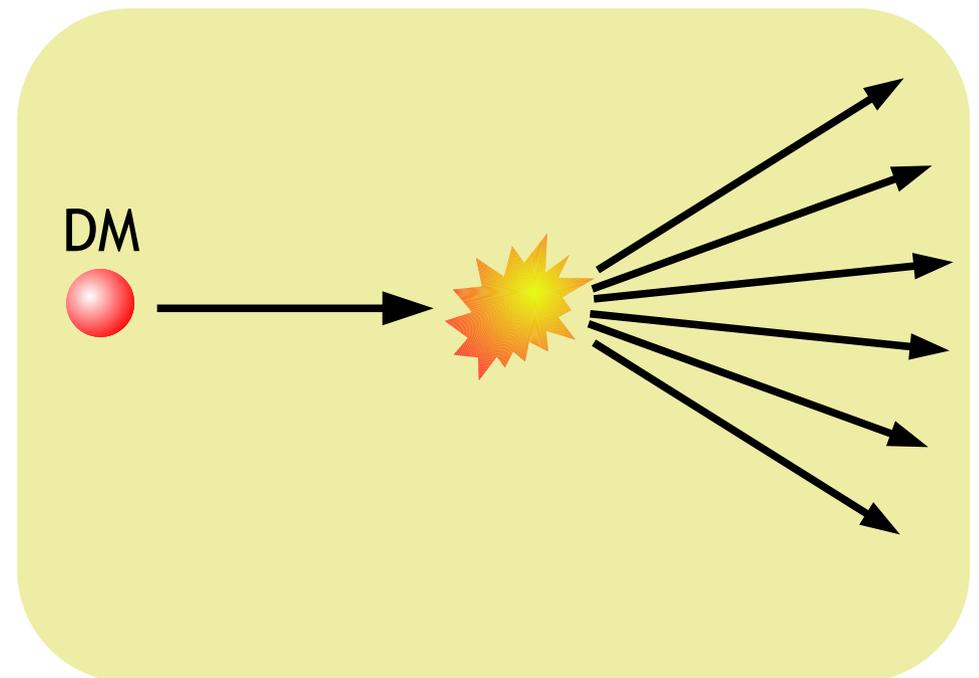
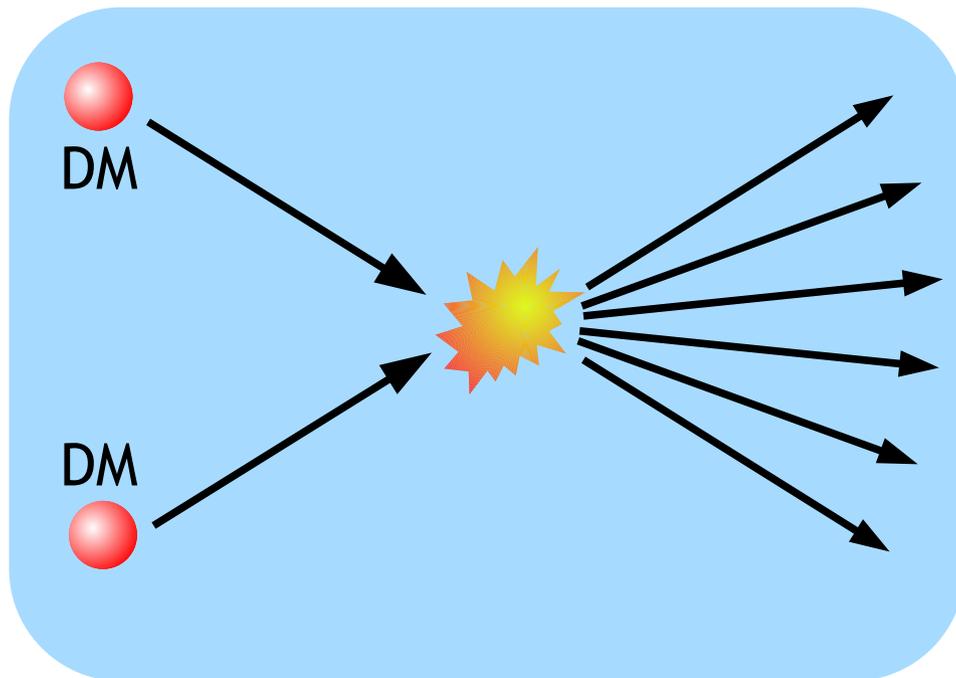


Indirect Dark Matter Searches

Indirect dark matter searches

General idea:

1) Dark matter particles annihilate or decay producing a flux of stable particles: photons, electrons, protons, positrons, antiprotons, (anti-)neutrinos or anti-nuclei



Indirect dark matter searches

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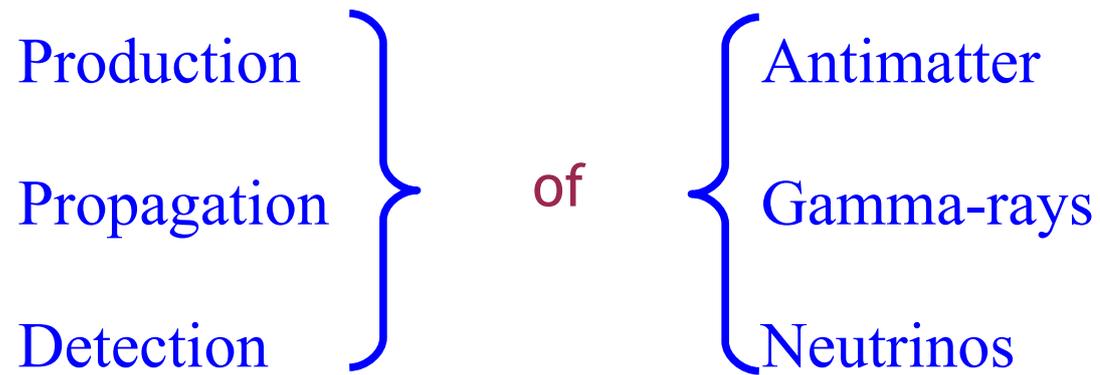
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Indirect dark matter searches

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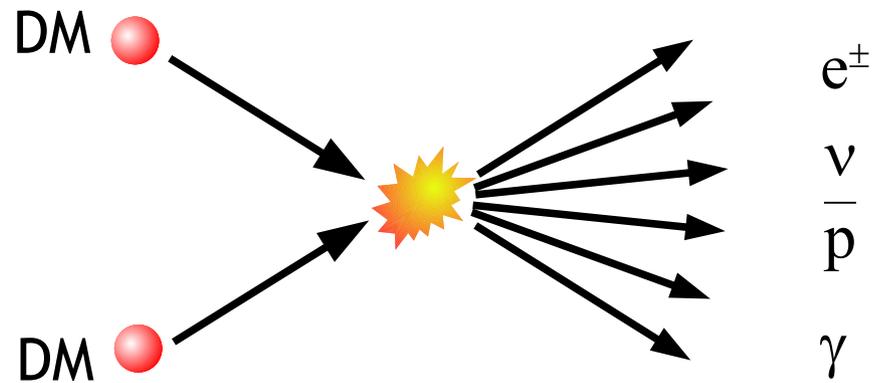
- 1) Dark matter particles annihilate or decay producing a flux of stable particles: photons, electrons, protons, positrons, antiprotons, (anti-)neutrinos or anti-nuclei.
- 2) These particles propagate through the galaxy and through the Solar System. Some of them will reach the Earth.
- 3) The products of the dark matter annihilations or decays are detected **together with other particles produced in astrophysical processes** (for example, cosmic ray collisions with nuclei in the interstellar medium). The existence of dark matter can then be inferred if there is a significant excess in the fluxes compared to the expected astrophysical backgrounds.

Indirect dark matter searches



Production

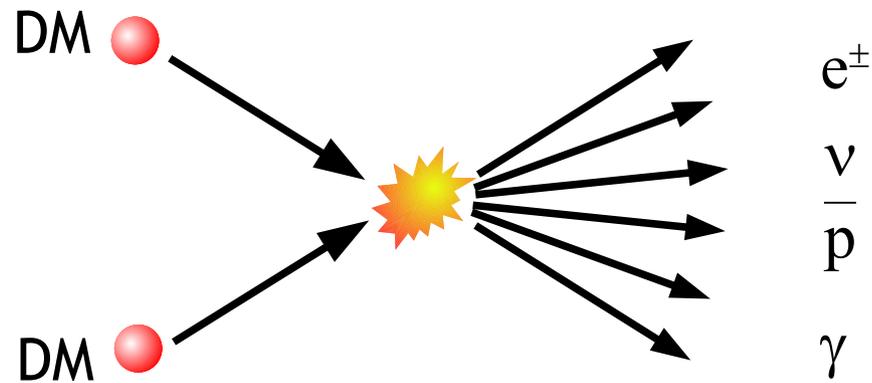
Production of SM particles in DM annihilation



Number of particles of the type “i” produced at the position r per unit time and unit volume:

$$Q(T, \vec{r}) = \frac{1}{2} \frac{\rho_\chi^2(\vec{r})}{m_\chi^2} \sum_i (\sigma v)_i \frac{dN^i}{dT}$$

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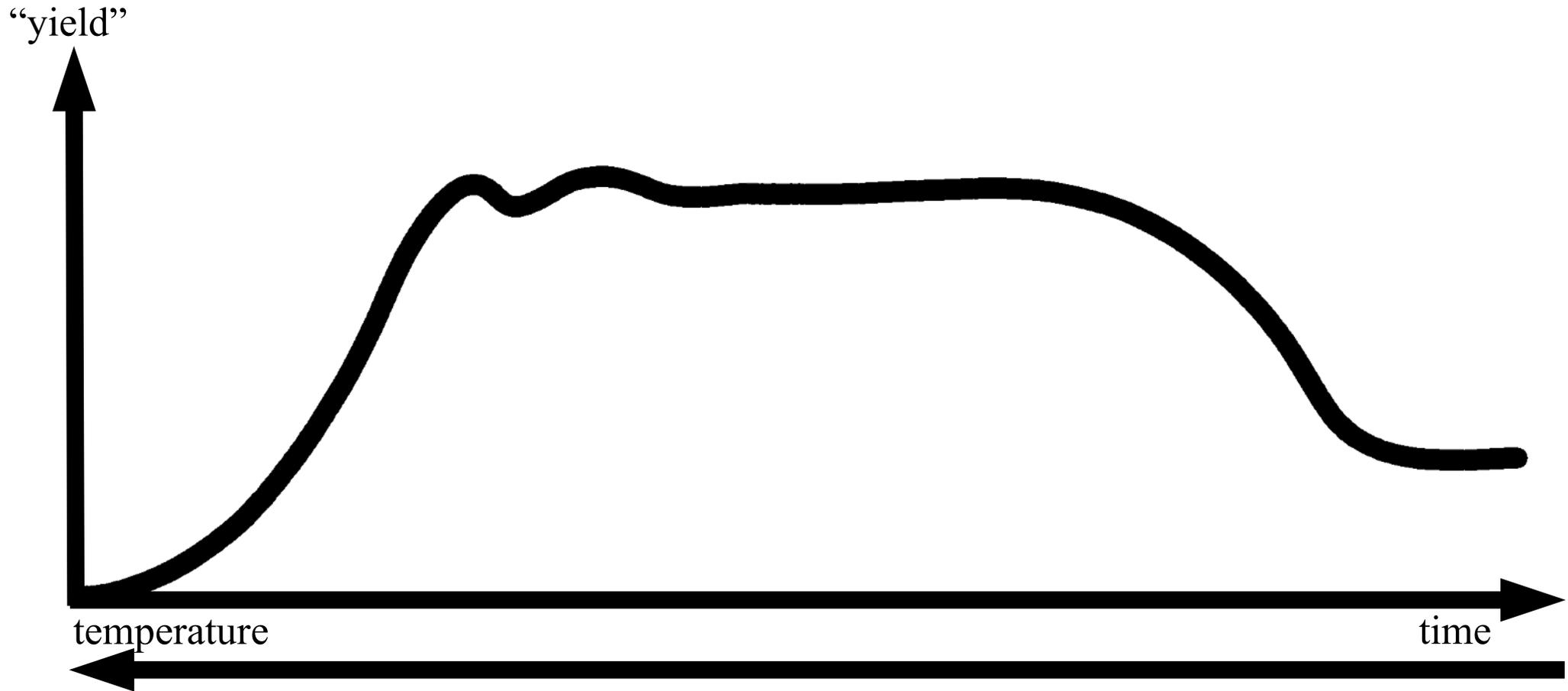


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DM density distribution in the MW

Dark matter distribution

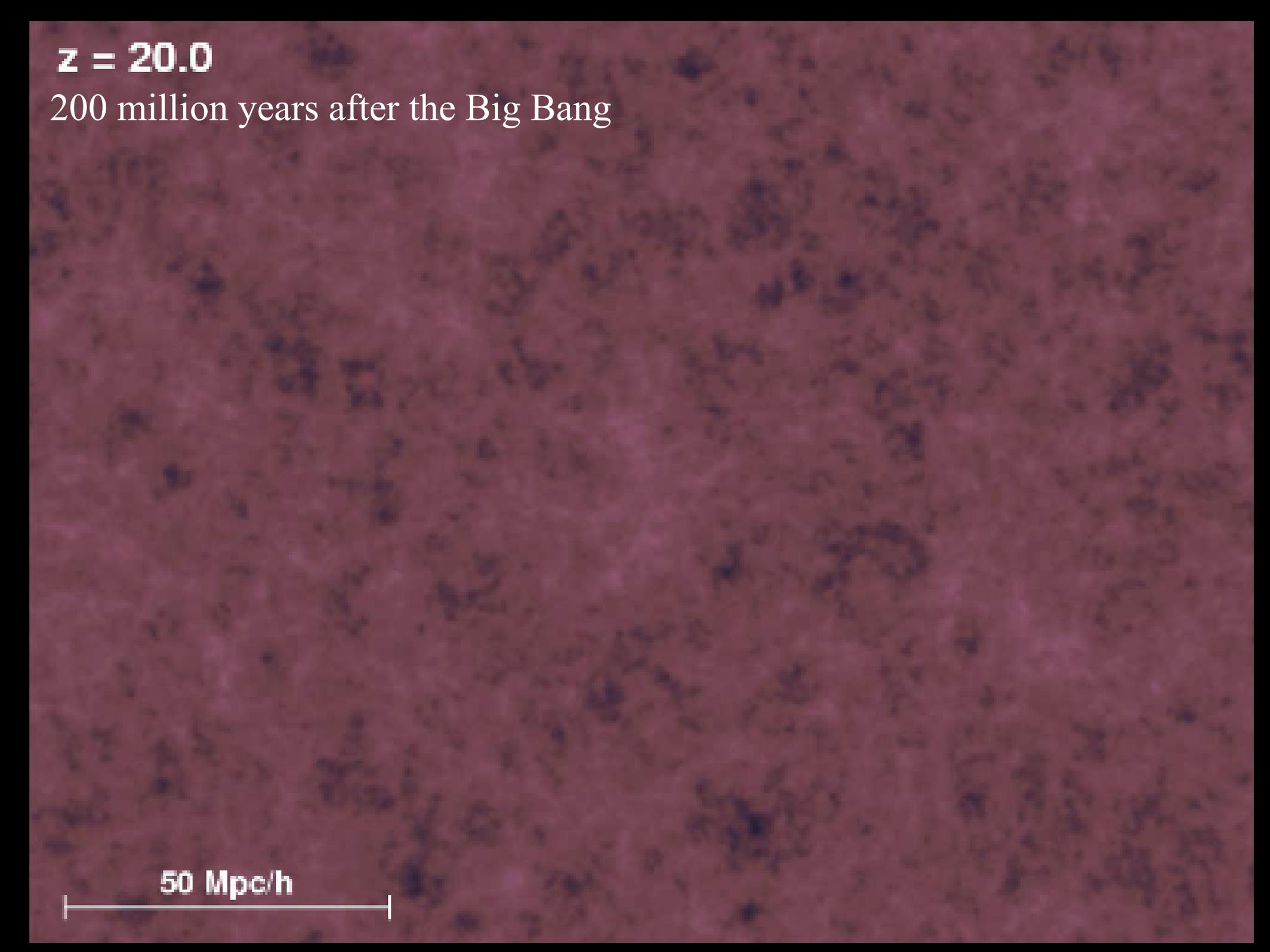


The universe at $T \sim 1 \text{ GeV}$

$z = 20.0$

200 million years after the Big Bang

50 Mpc/h

The image displays a vast field of small, faint galaxies, characteristic of a high-redshift universe. The galaxies are distributed across the frame, with some appearing as distinct, slightly elongated structures and others as more diffuse, cloud-like patches. The overall color palette is a mix of dark blues, purples, and greys, with some brighter, more prominent spots. The background is a dark, textured field of these galaxies, creating a sense of depth and density. In the bottom left corner, there is a white horizontal line with vertical end caps, labeled "50 Mpc/h", which serves as a scale bar for the simulation.

$z = 0.0$

50 Mpc/h



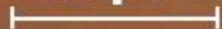
Volker Springel
Max-Planck-Institute
for Astrophysics



z=0.0

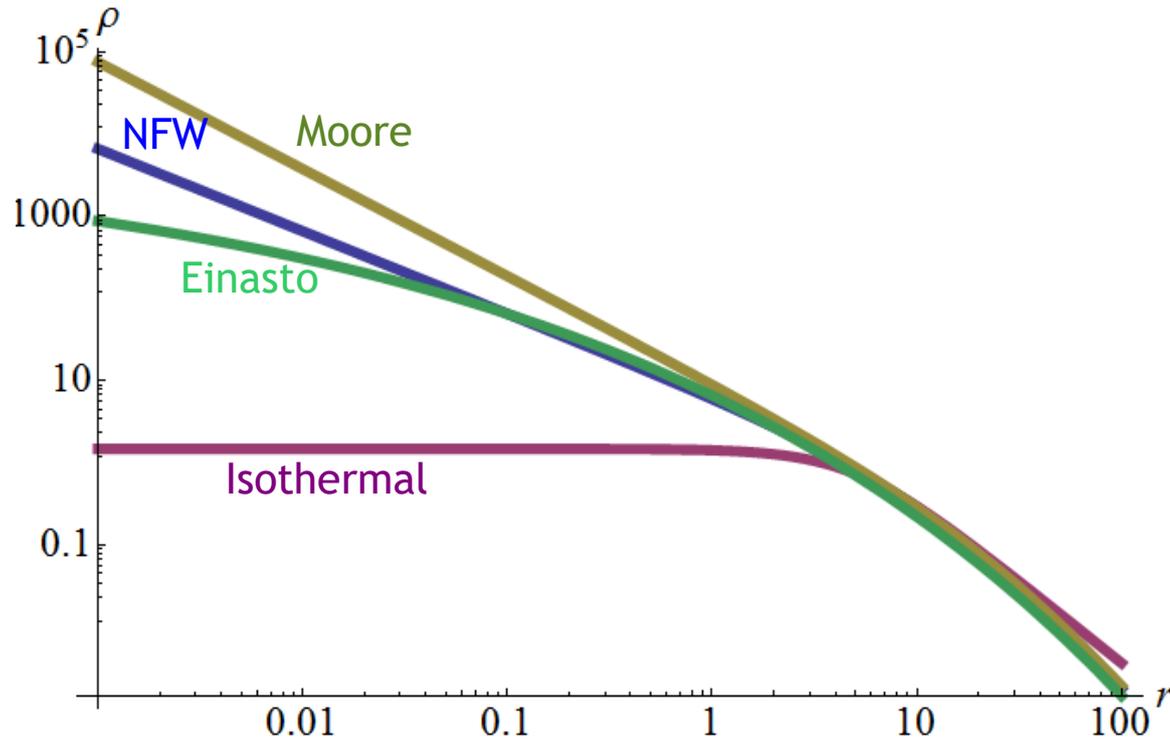
Distance Sun to Milky Way Center ~ 8.5 kpc

8 kpc



Density distribution of dark matter particles:

- Assume spherical symmetry (in a first approximation).
- Radial distribution:



NFW, Isothermal, Moore

$$\rho(r) = \frac{\rho_0}{(r/r_c)^\gamma [1 + (r/r_c)^\alpha]^{(\beta-\gamma)/\alpha}}$$

Halo model	α	β	γ	r_c (kpc)
Navarro, Frenk, White	1	3	1	20
Isothermal	2	2	0	3.5
Moore	1.5	3	1.5	28

Einasto

$$\rho(r) = \rho_0 \exp \left[-\frac{2}{\alpha} \left(\left(\frac{r}{r_s} \right)^\alpha - 1 \right) \right]$$

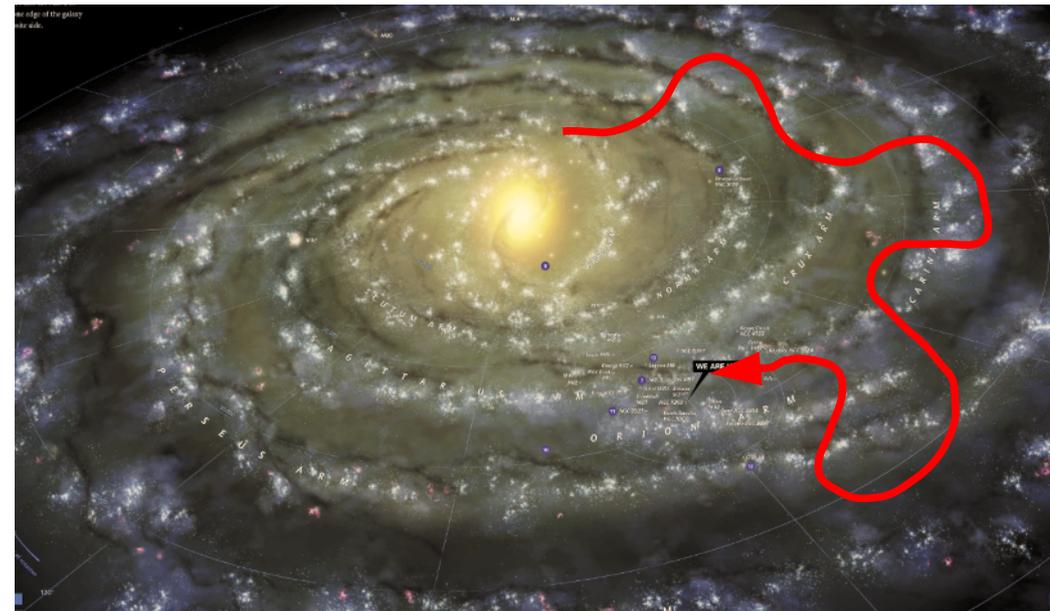
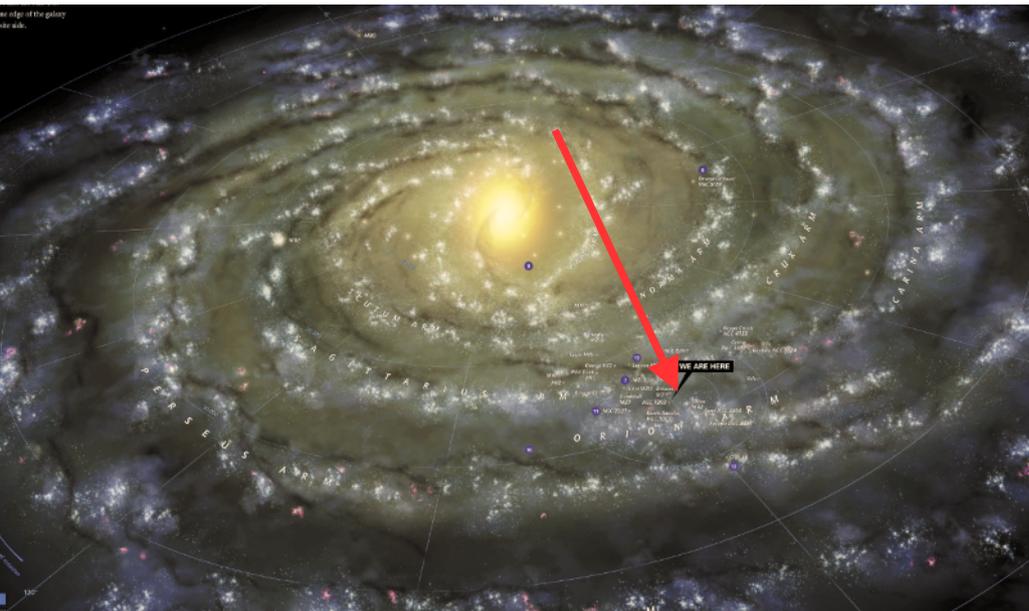
$$\alpha = 0.17, r_s = 20 \text{ kpc}$$

- Normalized such that the local DM density is $\rho(r=8.5 \text{ kpc}) = 0.38 \text{ GeV/cm}^3$

Propagation

Propagation of SM particles in the Galaxy

Neutral particles propagate in straight lines practically without losing energy. Charged particles, on the other hand, propagate in a complicated way through the tangled magnetic field of our Galaxy.

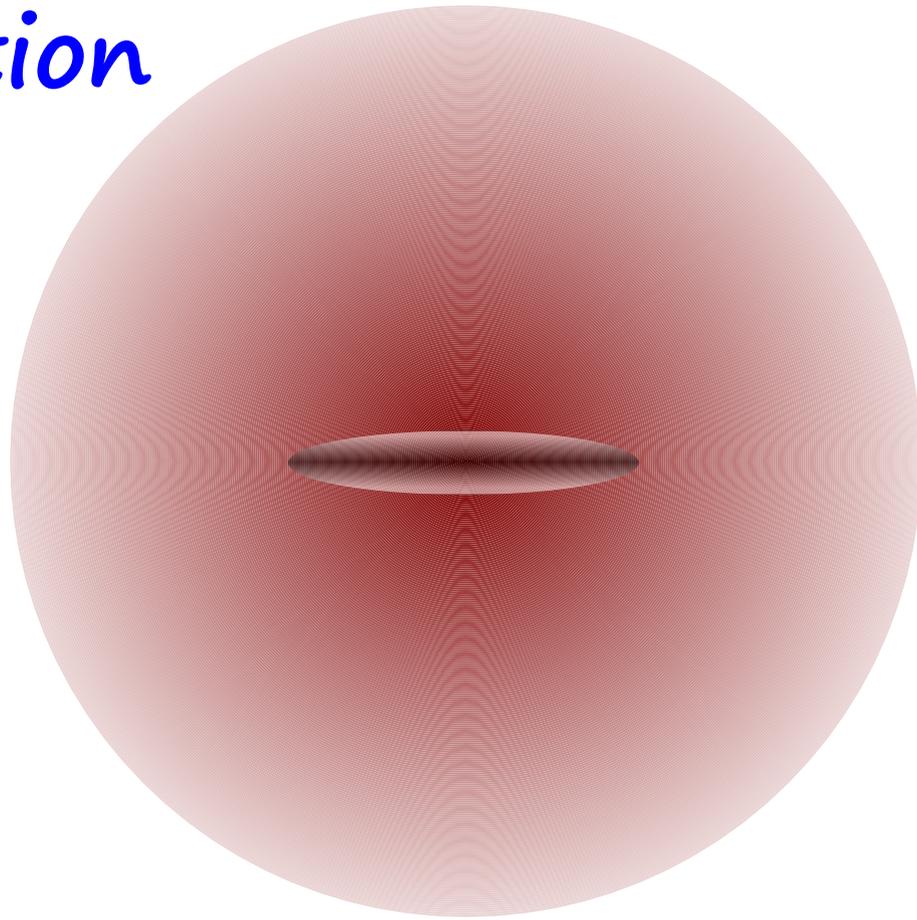


Charged particles

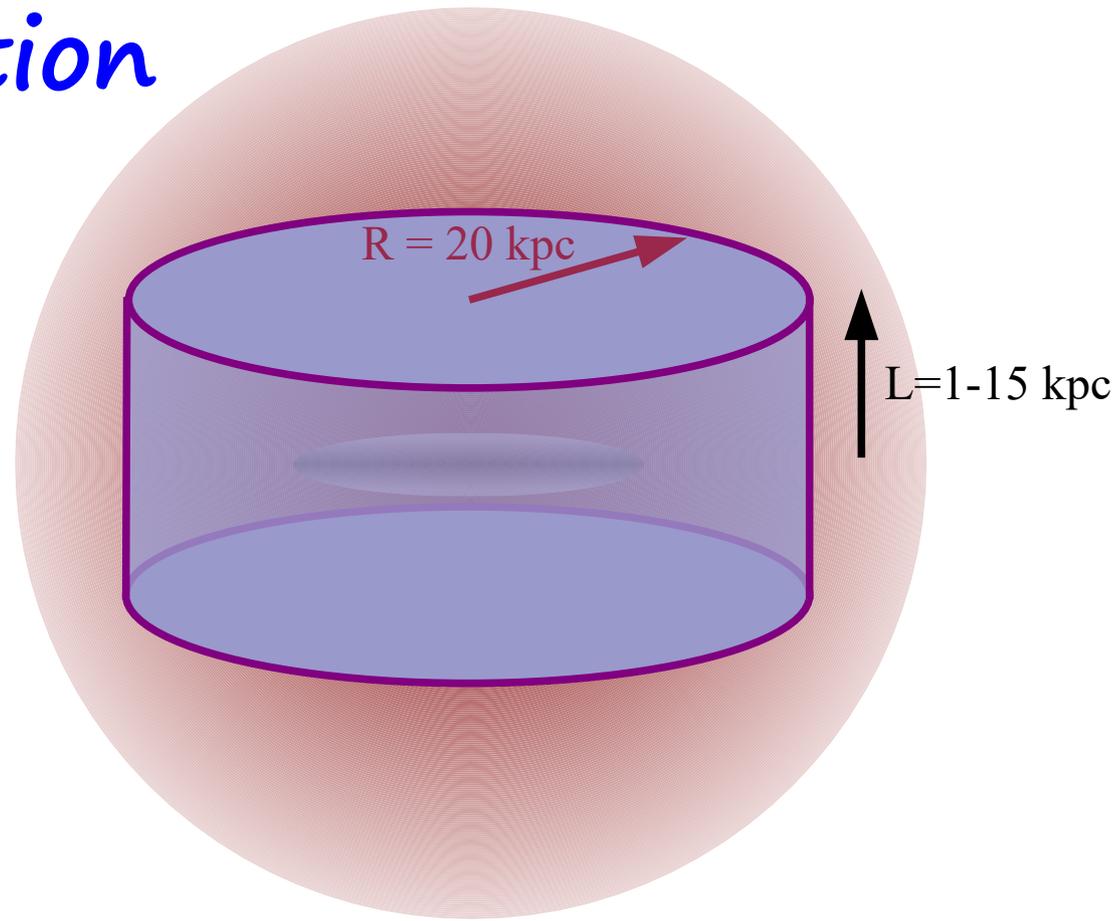
Propagation



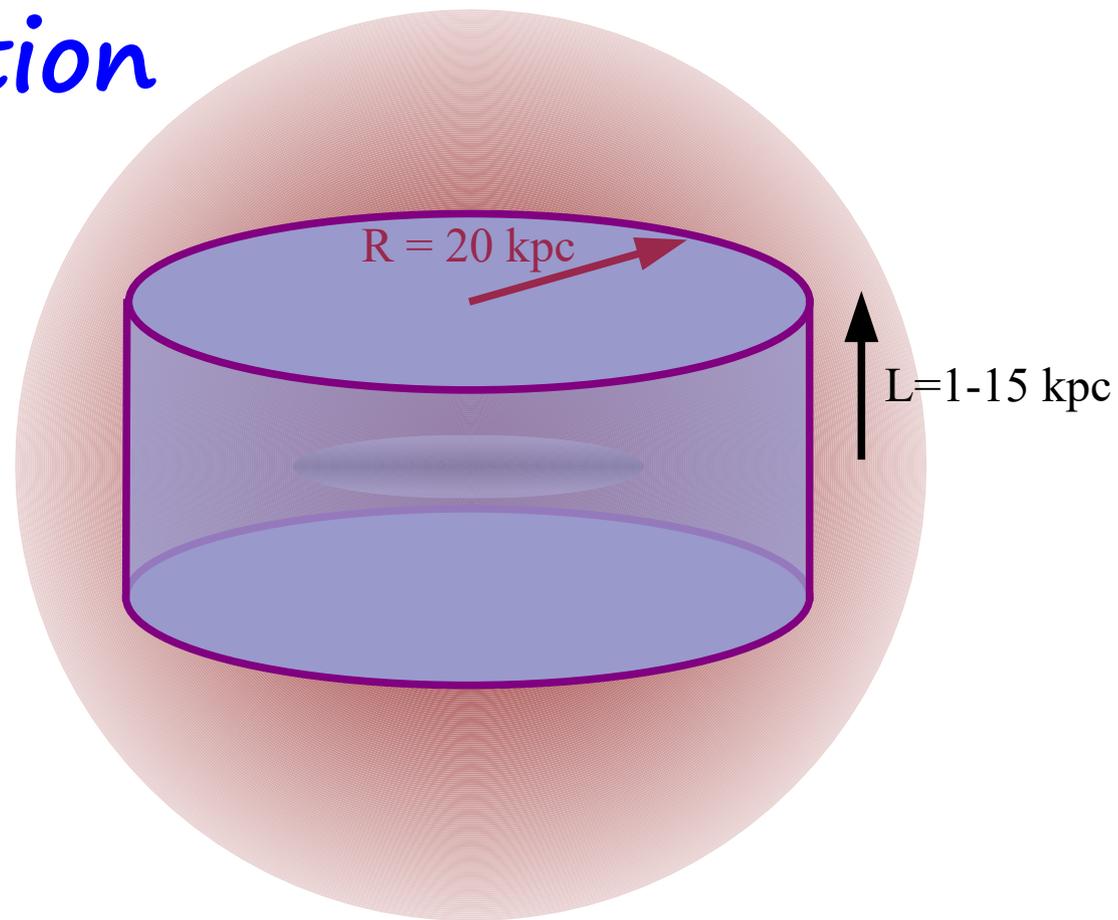
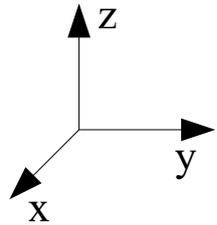
Propagation



Propagation



Propagation



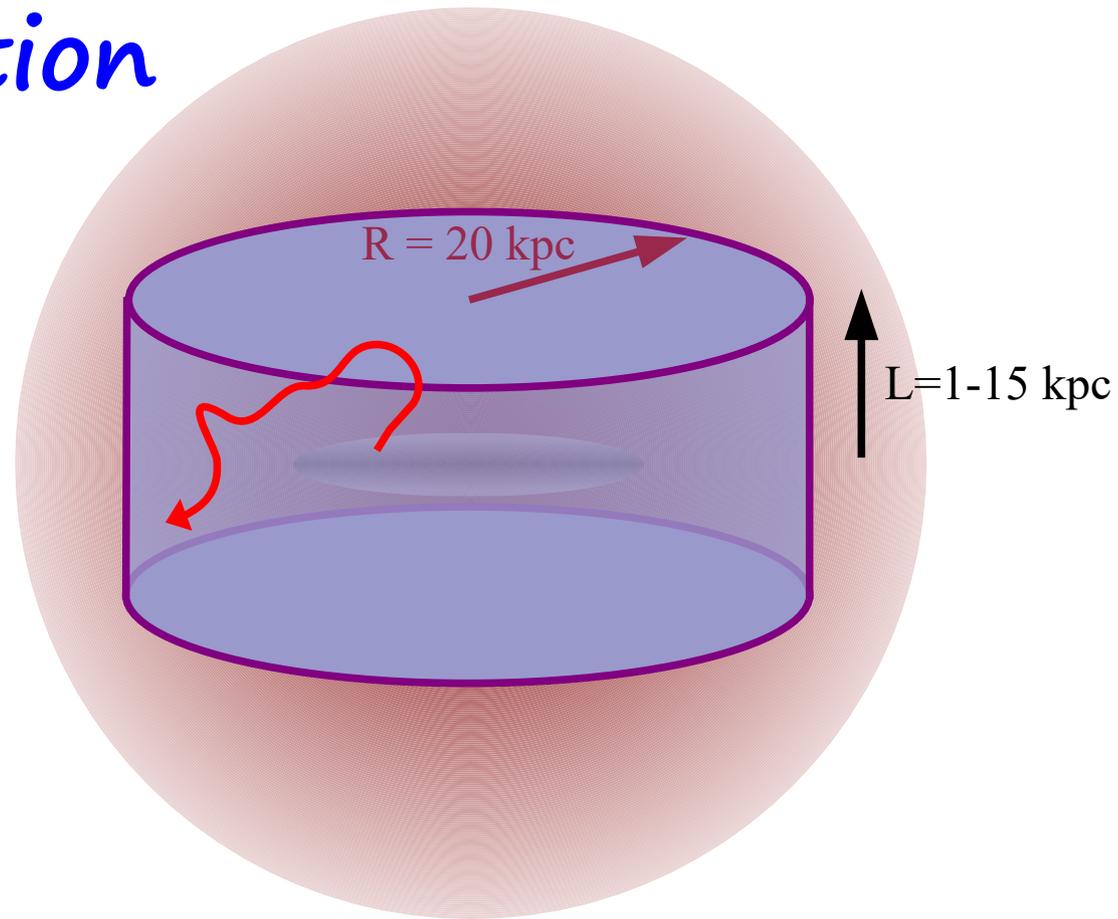
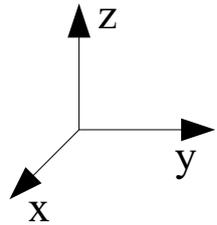
$$0 = \frac{\partial f}{\partial t} = \nabla \cdot [K(T, \vec{r}) \nabla f] + \frac{\partial}{\partial T} [b(T, \vec{r}) f] - \nabla \cdot [\vec{V}_c(\vec{r}) f] - 2h\delta(z)\Gamma_{\text{ann}}f + Q(T, \vec{r}) .$$

f : number density of antiparticles per unit kinetic energy

interstellar antimatter flux:

$$\Phi^{\text{IS}}(T) = \frac{dN}{dt dS dT d\Omega} = \frac{v}{4\pi} f(T)$$

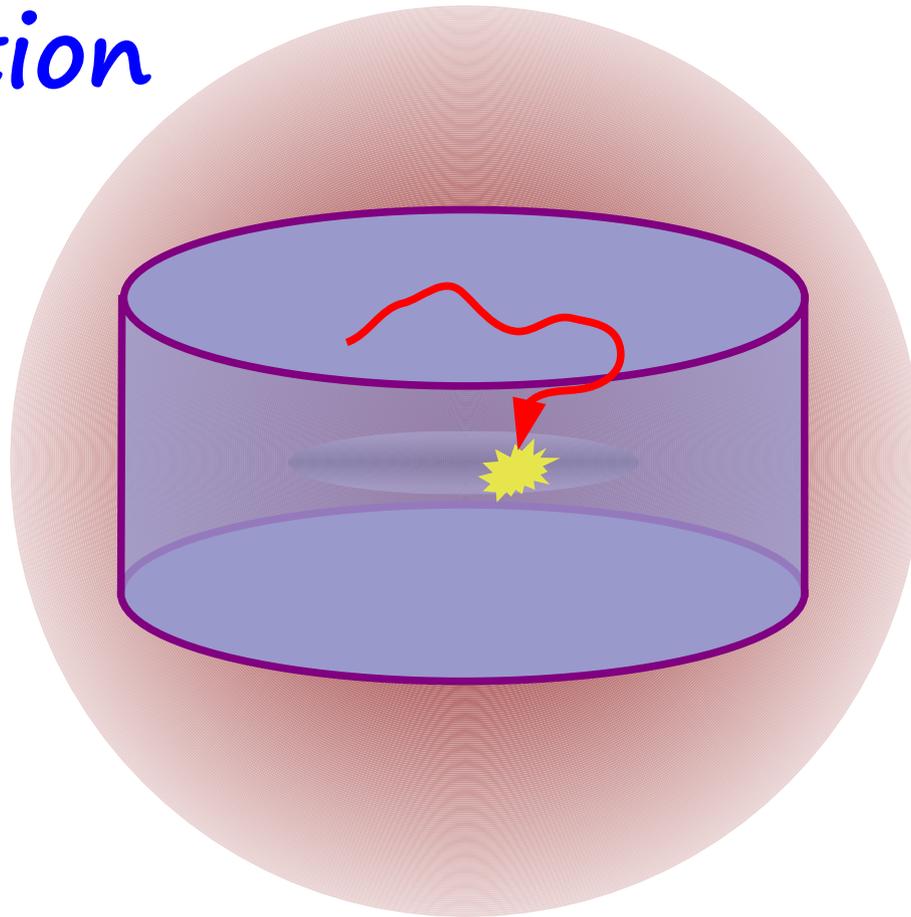
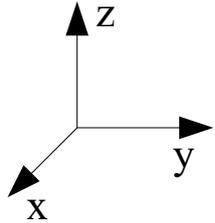
Propagation



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Source term $Q(T, \vec{r}) = \frac{1}{2} \frac{\rho^2(\vec{r})}{m_{\text{DM}}^2} \langle \sigma v \rangle \frac{dN}{dT}$ dark matter annihilation

Propagation



$$0 = \frac{\partial f}{\partial t} = \nabla \cdot [K(T, \vec{r}) \nabla f] + \frac{\partial}{\partial T} [b(T, \vec{r}) f] - \nabla \cdot [\vec{V}_e(\vec{r}) f] - 2h\delta(z)\Gamma_{\text{ann}}f - Q(T, \vec{r}) .$$

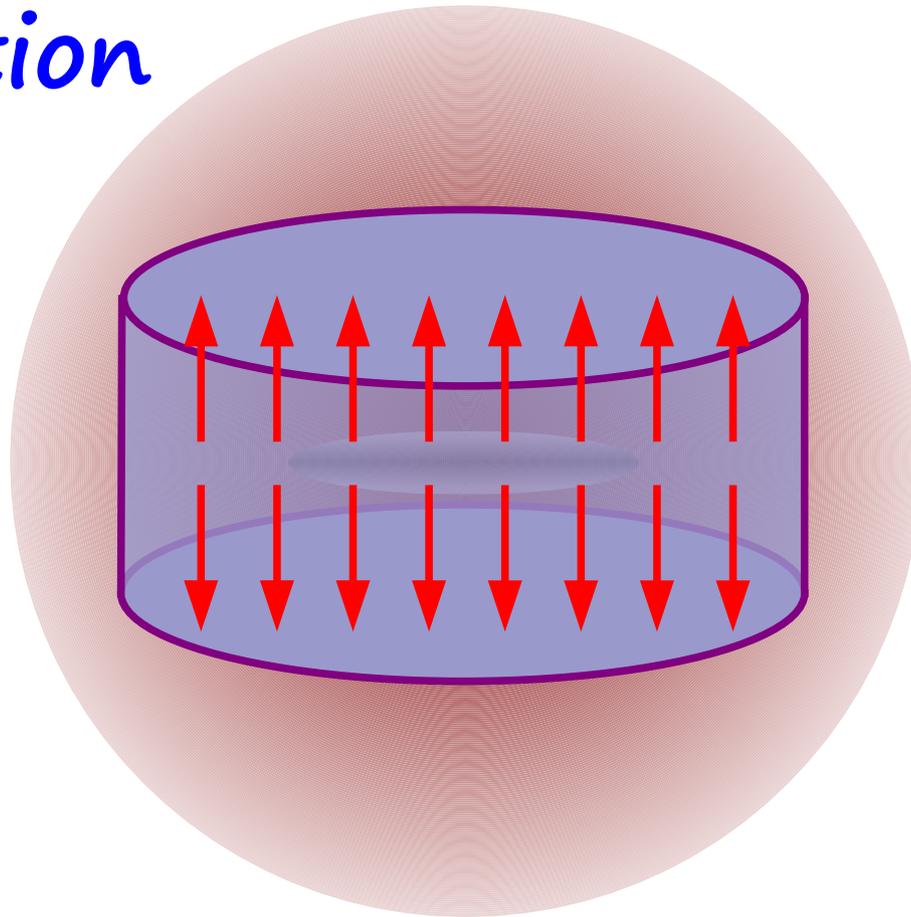
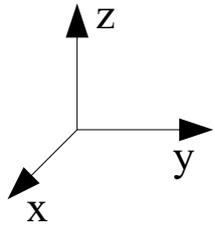
Annihilation term

Negligible for positrons.
For antiprotons,

$$\Gamma_{\text{ann}} = (n_{\text{H}} + 4^{2/3}n_{\text{He}})\sigma_{\bar{p}p}^{\text{ann}}v_{\bar{p}} .$$

$$\sigma_{\bar{p}p}^{\text{ann}}(T) = \begin{cases} 661 (1 + 0.0115 T^{-0.774} - 0.948 T^{0.0151}) \text{ mbarn} , & T < 15.5 \text{ GeV} , \\ 36 T^{-0.5} \text{ mbarn} , & T \geq 15.5 \text{ GeV} , \end{cases}$$

Propagation



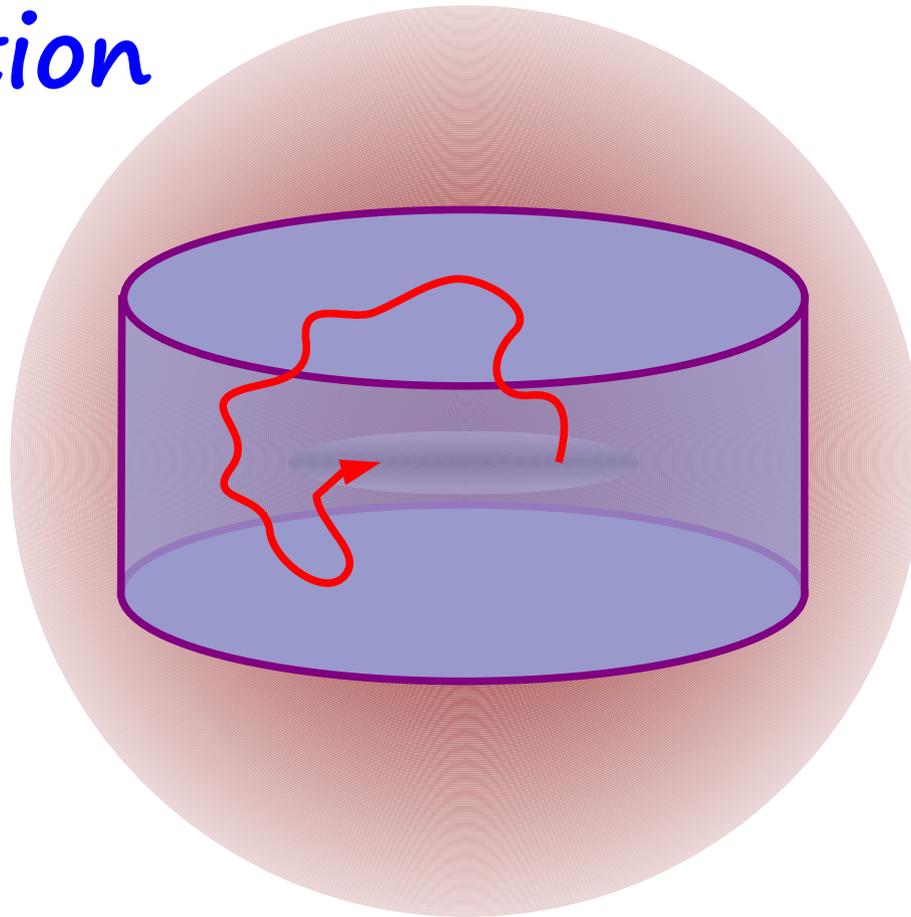
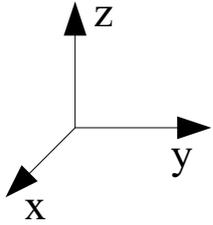
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Convection term

- Due to the Milky Way galactic wind.
- Drifts particles away from the Galactic disk.
- **Difficult to model.** Assume:

$$\vec{V}_c(\vec{r}) = V_c \text{sign}(z) \vec{k}$$

Propagation



$$0 = \frac{\partial f}{\partial t} = \nabla \cdot [K(T, \vec{r}) \nabla f] - \frac{\partial}{\partial T} [b(T, \vec{r}) f] - \nabla \cdot [\vec{V}_c(\vec{r}) f] - 2h\delta(z)\Gamma_{\text{ann}}f + Q(T, \vec{r}) .$$

Energy loss term

- Due to inverse Compton scattering on the interstellar radiation field (starlight, thermal radiation of dust, CMB) and synchrotron radiation.
- Negligible for antiprotons and antideuterons
- Can be modelled

- Energy loss due to Inverse Compton scattering: $e^+\gamma \rightarrow e^+\gamma$

$$b_{\text{ICS}}(E_e, \vec{r}) = \int_0^\infty d\epsilon \int_\epsilon^{E_\gamma^{\text{max}}} dE_\gamma (E_\gamma - \epsilon) \frac{d\sigma^{\text{IC}}(E_e, \epsilon)}{dE_\gamma} f_{\text{ISRF}}(\epsilon, \vec{r})$$

Number density
of photons in ISRF

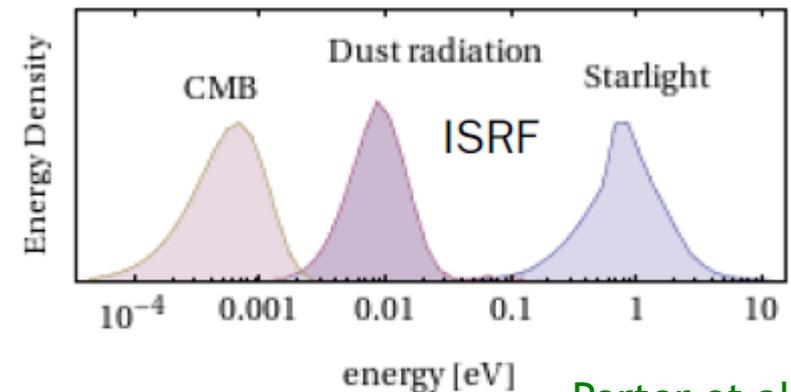
$$\frac{d\sigma^{\text{IC}}(E_e, \epsilon)}{dE_\gamma} = \frac{3}{4} \frac{\sigma_T}{\gamma_e^2 \epsilon} \times \left[2q \ln q + 1 + q - 2q^2 + \frac{1}{2} \frac{(q\Gamma)^2}{1 + q\Gamma} (1 - q) \right]$$

$\gamma_e = E_e/m_e \propto$ Lorentz factor.

$\Gamma_e = 4 \gamma_e \epsilon/m_e$

$q = E_\gamma/\Gamma(E_e - E_\gamma)$

$\sigma_T = 0.67$ barn \propto Compton scattering cross section
in the Thomson limit.



Porter et al.

- Energy loss due to synchrotron radiation:

$$b_{\text{sync}}(E_e, \vec{r}) = \frac{4}{3} \sigma_T \gamma_e^2 \frac{B^2}{2}$$

$$B = 6 \mu G \exp(-|z|/5 \text{ kpc} - r/20 \text{ kpc})$$

Approximately $b(E) = \frac{E^2}{E_0 \tau_E}$, with $E_0 = 1$ GeV and $\tau_E = 10^{16}$ s

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$\gamma_e = E_e/m_e \propto$ Lorentz

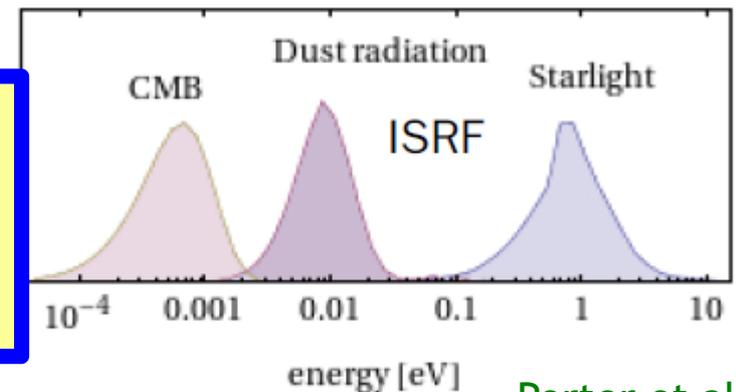
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Not very well known, though...



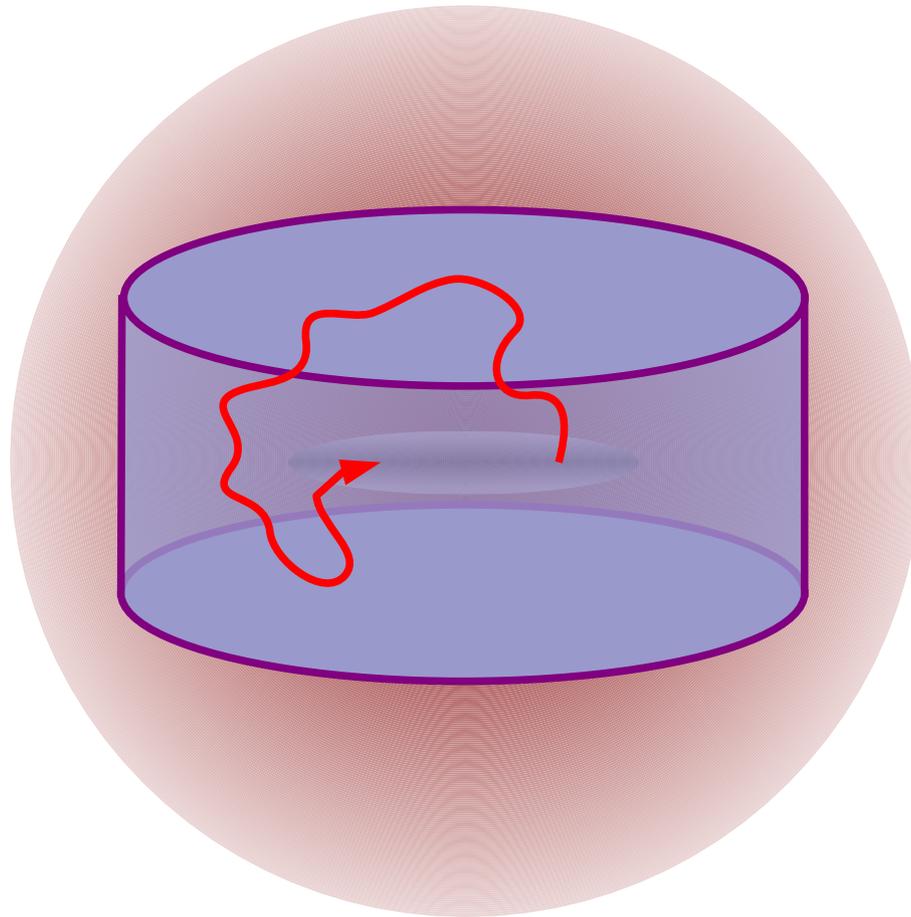
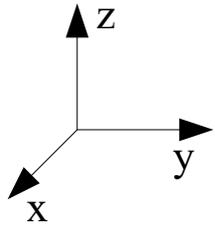
Porter et al.

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Diffusion term

- Due to the tangled magnetic field of the Galaxy.
- **Difficult to model.** Assume

$$K(T) = K_0 \beta \mathcal{R}^\delta$$

$$\left(\begin{array}{l} \beta = \text{velocity} \\ P = \text{rigidity} \end{array} \right)$$

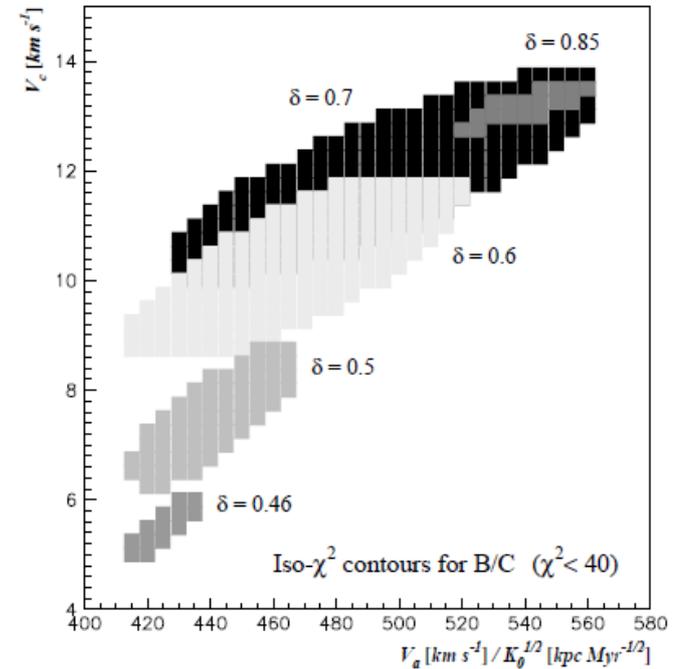
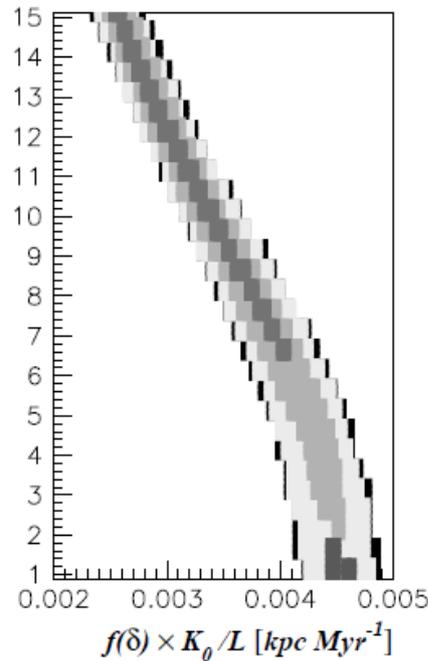
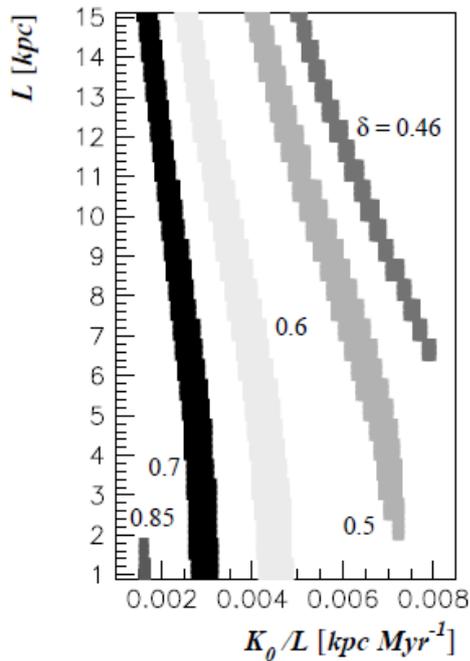
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$$K(T) = K_0 \beta \mathcal{R}^\delta$$

$$\vec{V}_c(\vec{r}) = V_c \text{sign}(z) \vec{k}$$

K_0 , δ , V_c (as well as L) must be determined with measurements of other cosmic ray species (mainly B/C ratio).

Iso- χ^2 contours for B/C ($\chi^2 < 40$)



Model	δ	K_0 (kpc ² /Myr)	L (kpc)	V_c (km/s)
MIN	0.85	0.0016	1	13.5
MED	0.70	0.0112	4	12
MAX	0.46	0.0765	15	5

Maurin, Donato, Taillet, Salati '01



M80

M14

8
Draconis
NGC 5129

M92

9

3
KIC ARM

NORMA ARM

CRUX ARM

CARINA ARM

SCUTUM ARM

M71

M4

Alphei Cluster
NGC 4755

30,000

Bottlefly
M52

NGC 6397

Carina
NGC 3392

Keyhole
NGC 3324

SAGITTARIUS ARM

Eagle
M16

13
Lagoon
M8

WE ARE HERE

M10
Wild Duck
M10

George
M73

M2

Orion
M97

Trifid
M20

Antares
M79

Bumblebee
M27

NGC 7293

Orion
M42

NGC 2269

Booby

NGC 2837

11
NGC 7027

North America
NGC 7000

Orion
M43

Orion
M48

Orion
M49

O R I O N

10

6,000 light years

12
Orion
M45

ARM

M

A

R

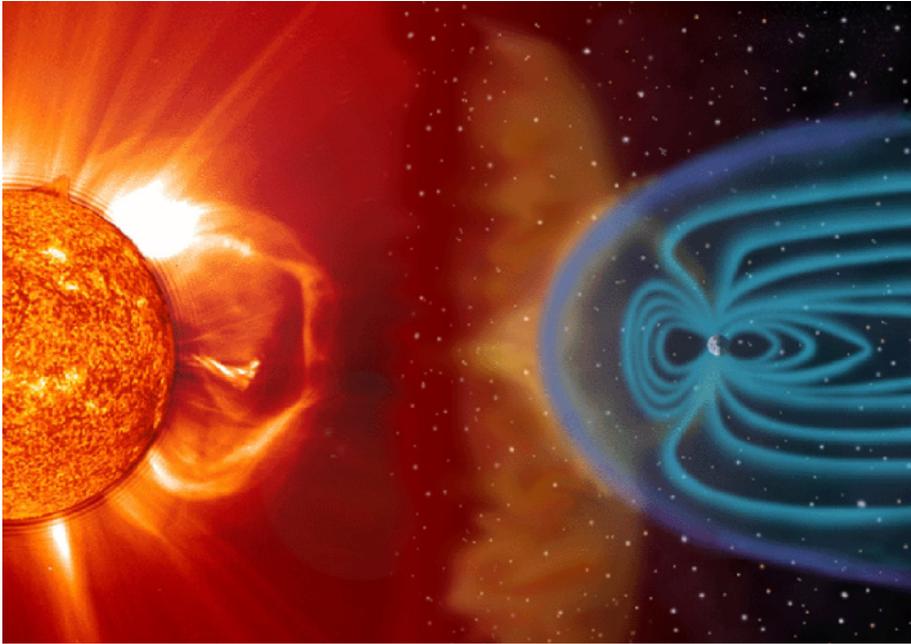
N

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Propagation *inside* the Solar System



In the “force field approximation”, the flux at the top of the atmosphere (TOA) is related to the interstellar flux (IS) by

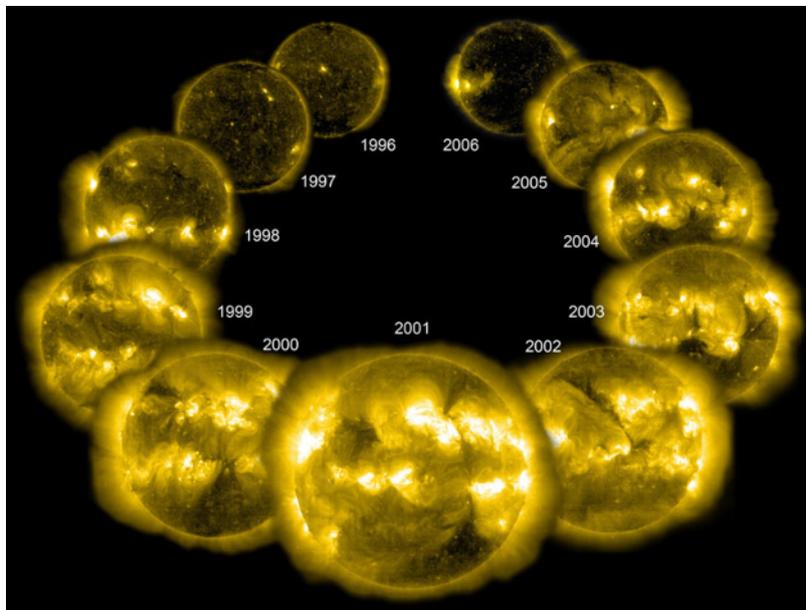
$$\Phi_{e^\pm}^{\text{TOA}}(E_{\text{TOA}}) = \frac{E_{\text{TOA}}^2}{E_{\text{IS}}^2} \Phi_{e^\pm}^{\text{IS}}(E_{\text{IS}})$$

$$E_{\text{IS}} = E_{\text{TOA}} + \phi_F$$

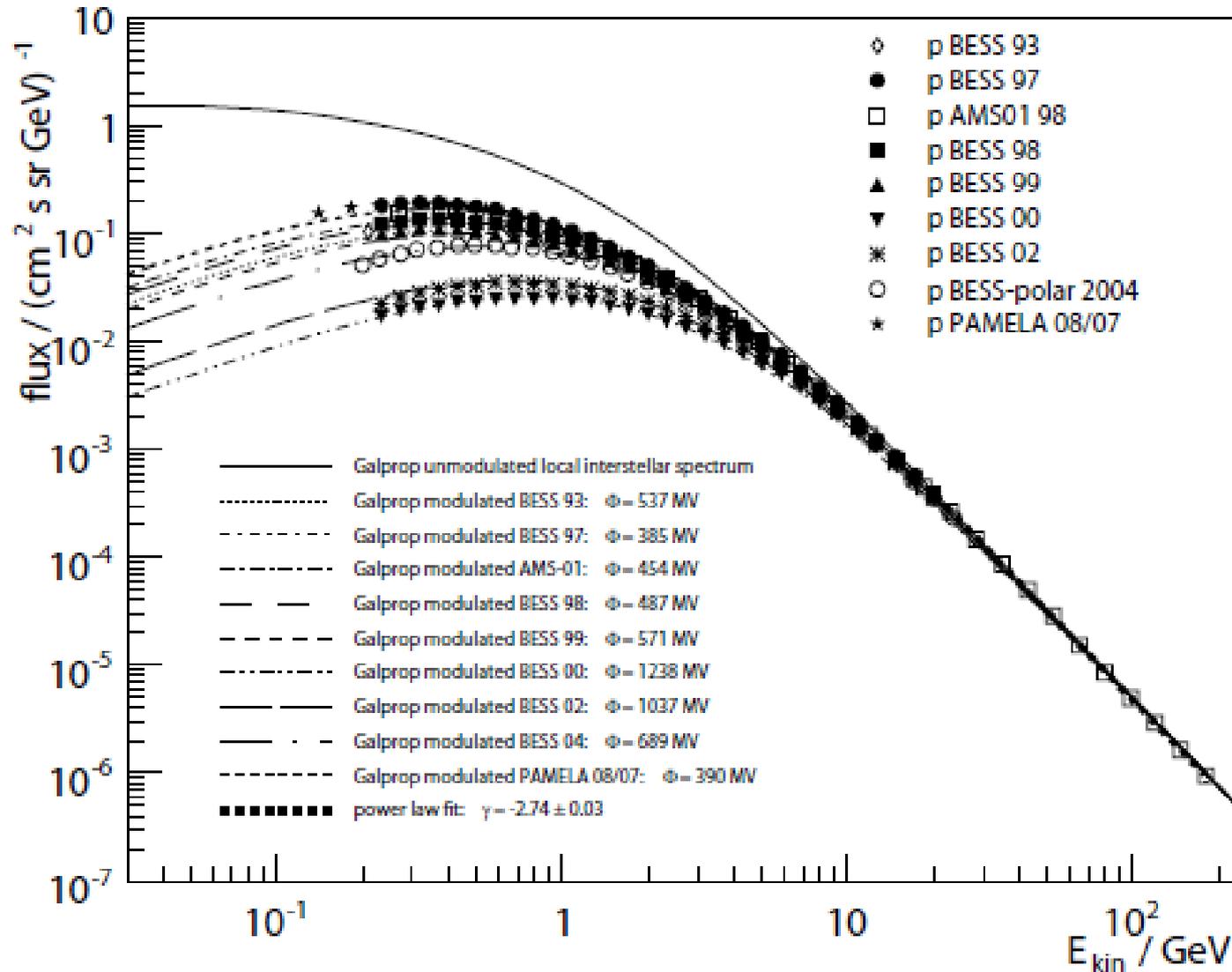


solar modulation parameter

$$\phi_F = 500 \text{ MV} - 1.3 \text{ GV}$$



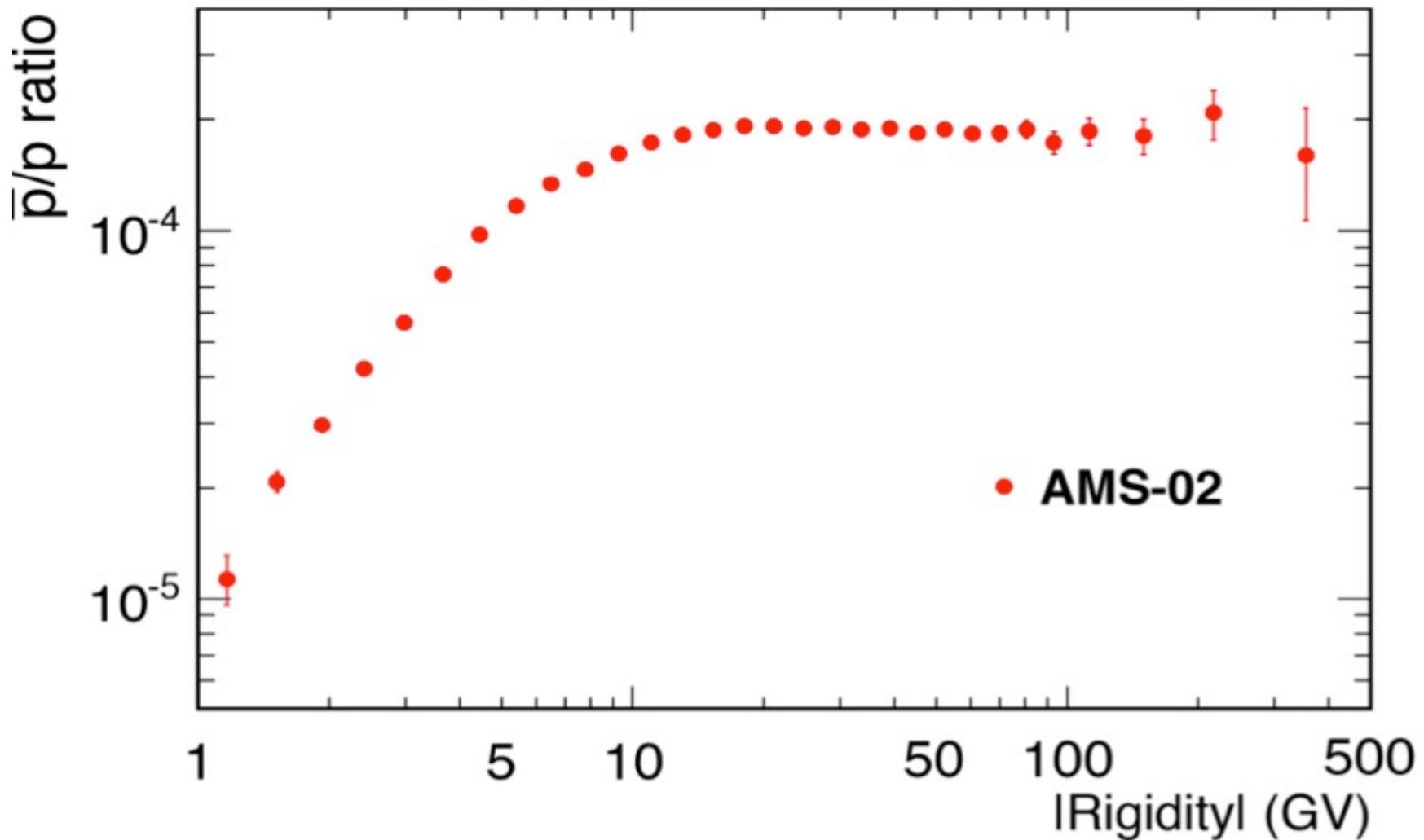
Cosmic ray **proton** spectrum as measured by BESS, AMS-01 and PAMELA



Gast, Schael '09

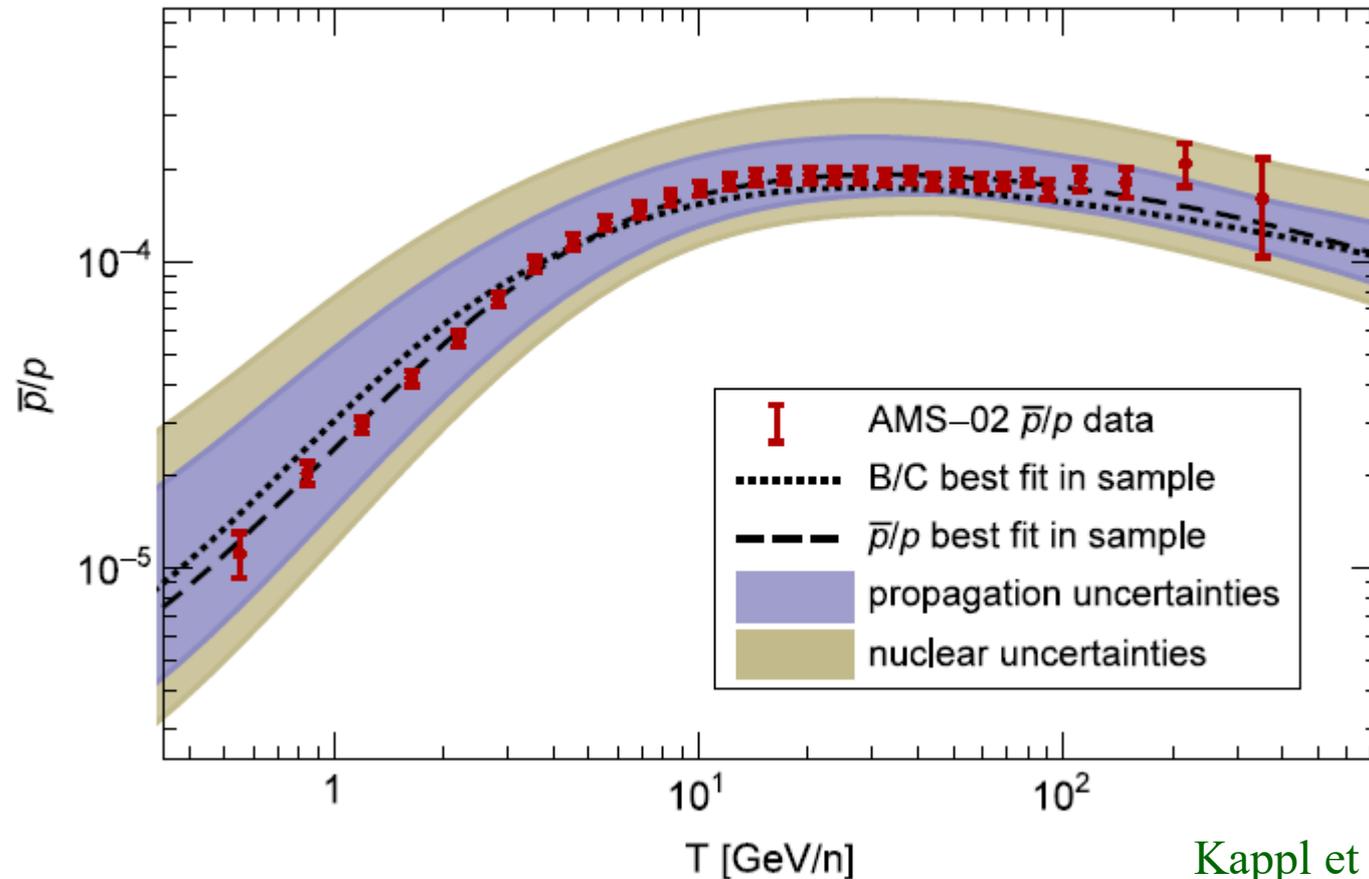
Experimental results

AMS \bar{p}/p results



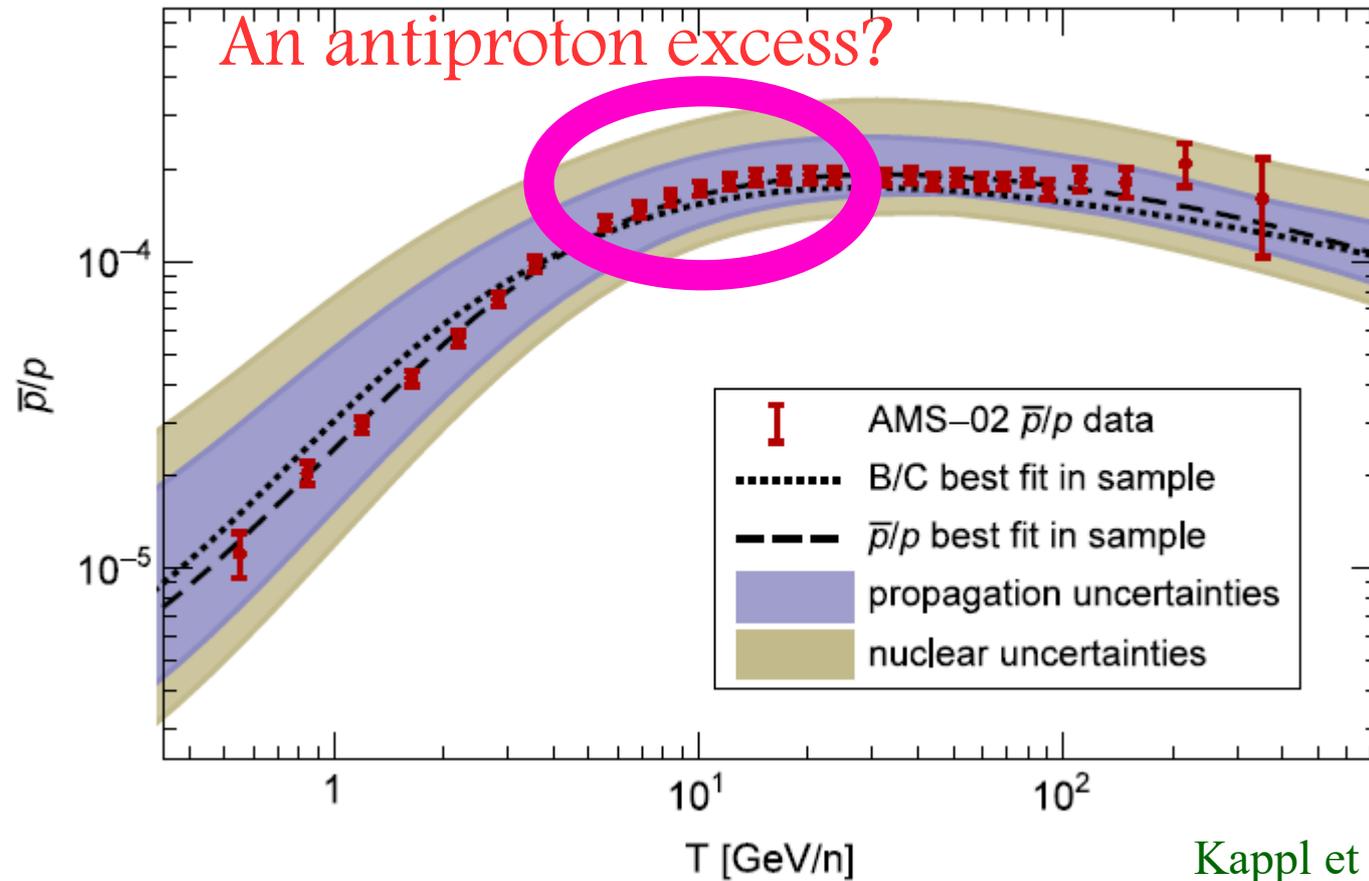
AMS-02 coll'15

Experimental results



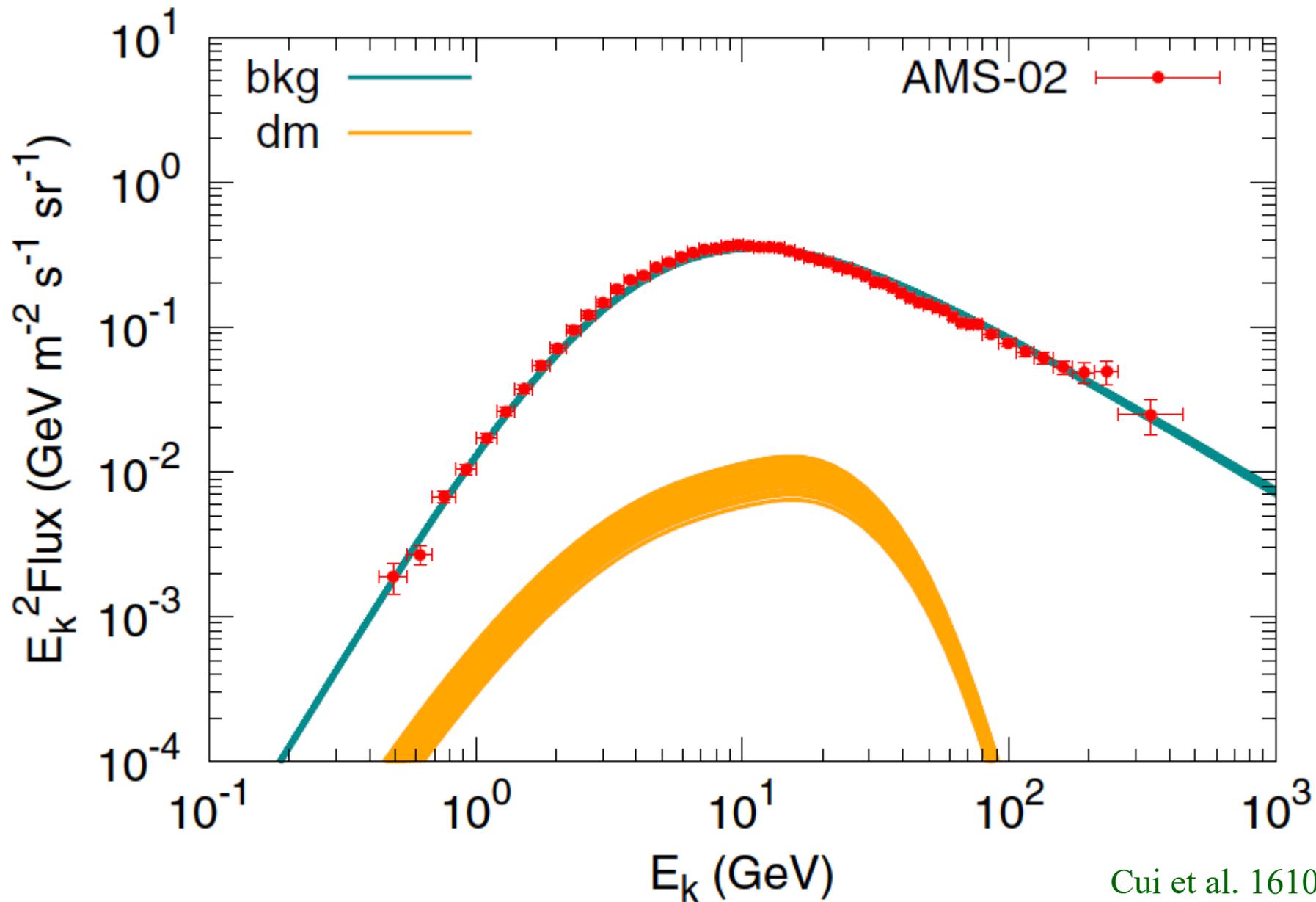
Good qualitative agreement between the measurements and the theoretical predictions from collisions of cosmic rays on the interstellar medium $p p \rightarrow \bar{p} X$

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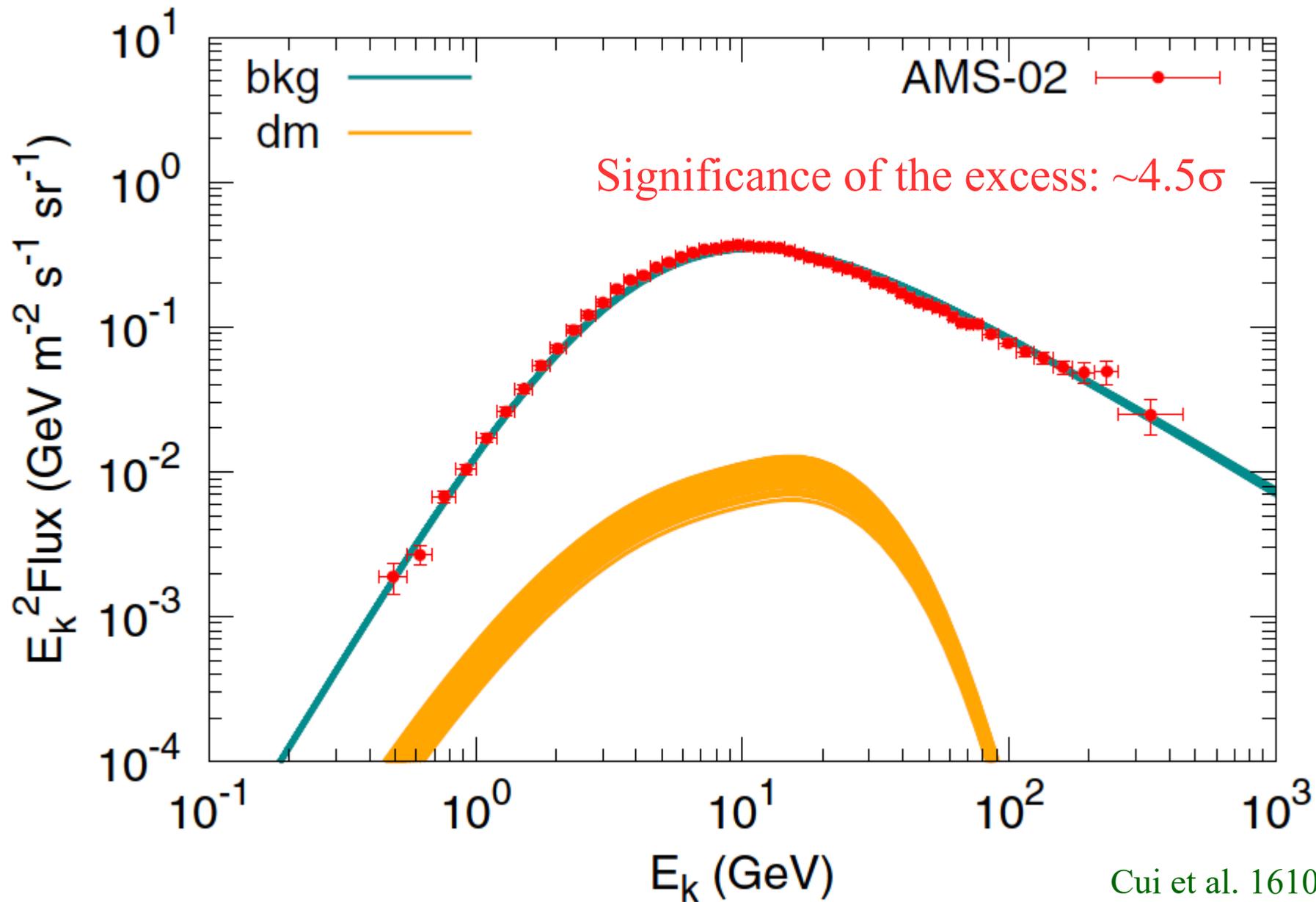
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An antiproton excess??



Cui et al. 1610.03840
Cuoco et al. 1610.03071

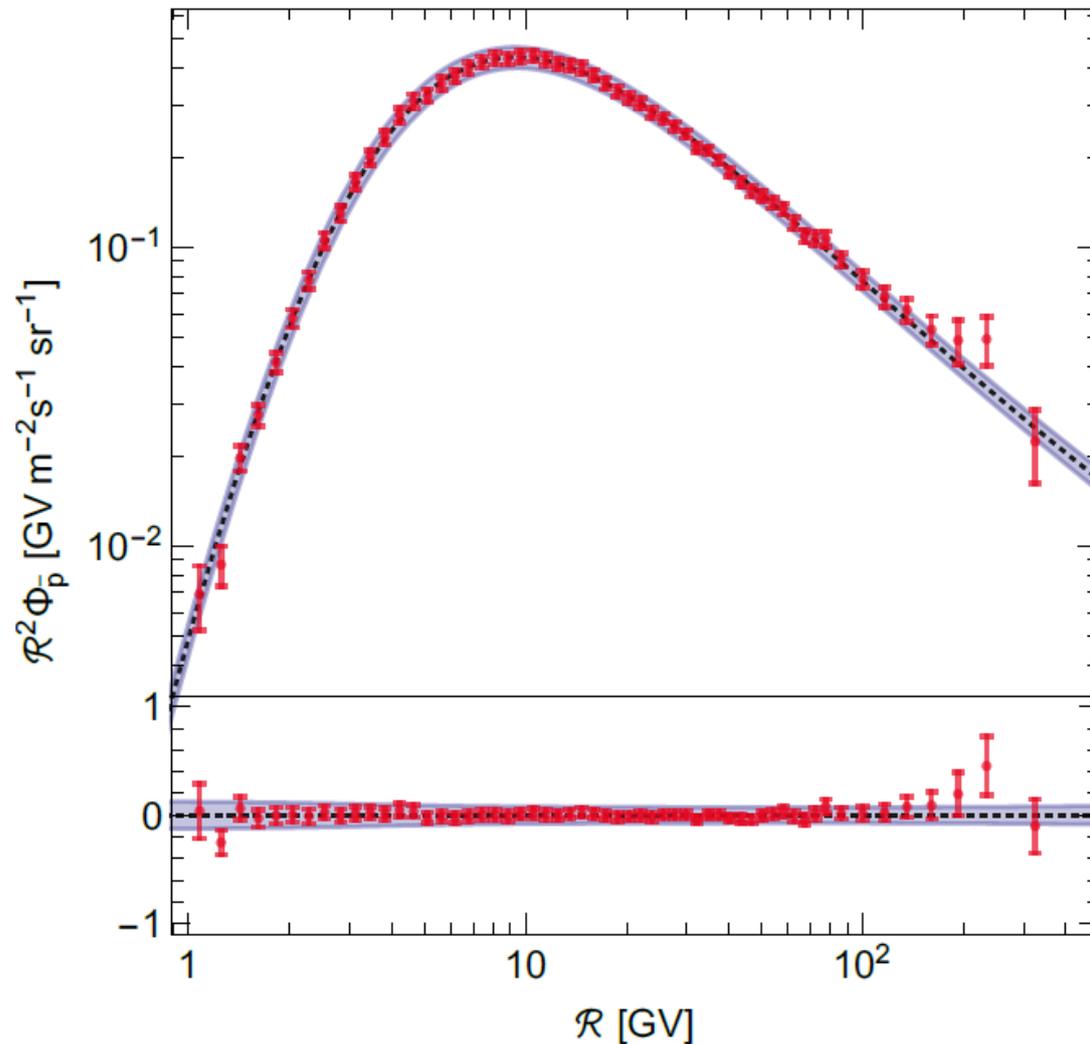
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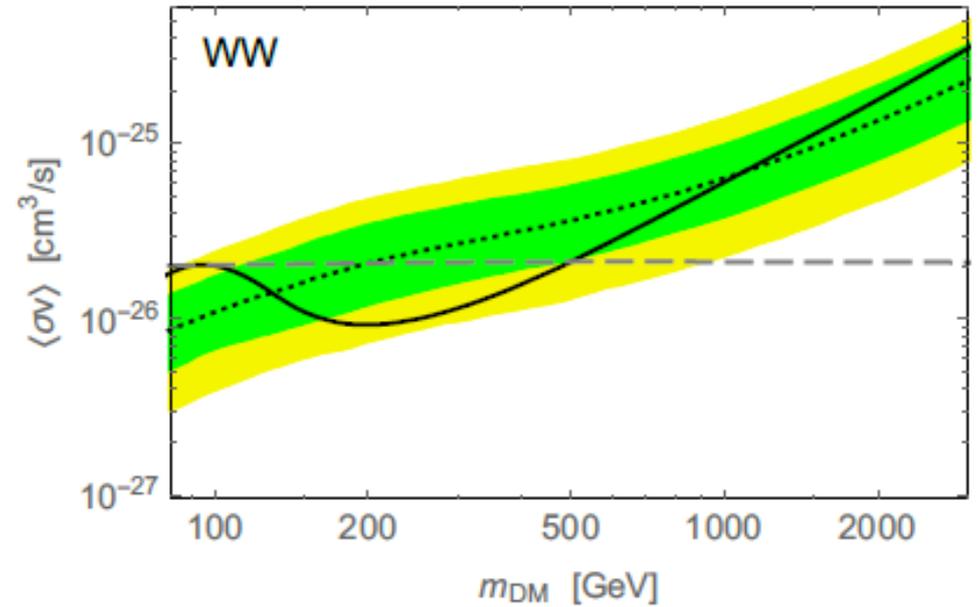
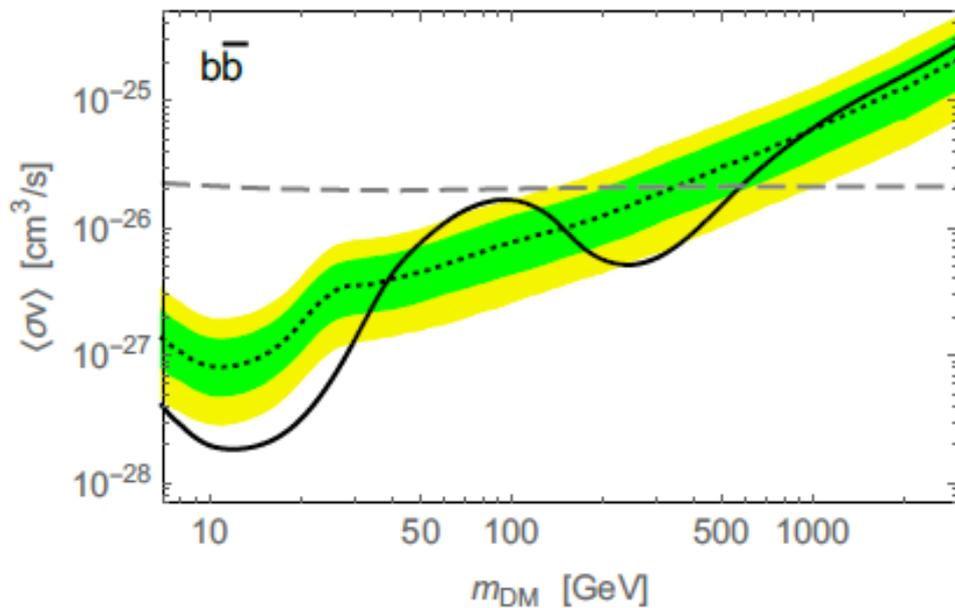
An antiproton excess??

Recent analyses using a large collection of data of antiproton production, and an improved analysis of the propagation uncertainties, lower the significance to 2.2σ .



Reinert, Winkler.
1712.00002

DM constraints from antiproton data



Reinert, Winkler.
1712.00002