

Narrowing down the mass range of ultra-light dark matter

Elisa G. M. Ferreira

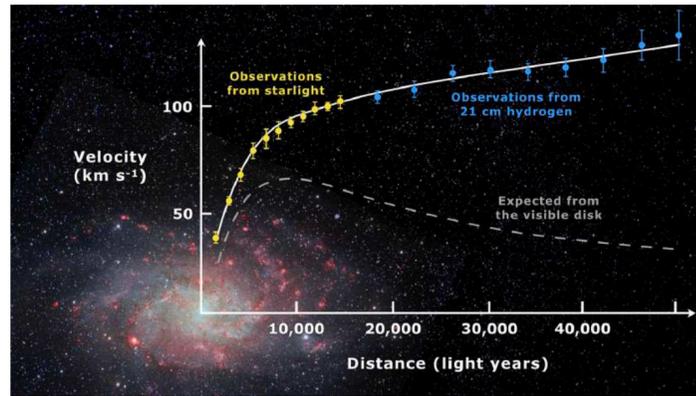
Kavli IPMU

KMI/NITEP School 2026: Dark Matter -
From Ultra Light To Super Massive

11/March/2026

Evidences for dark matter

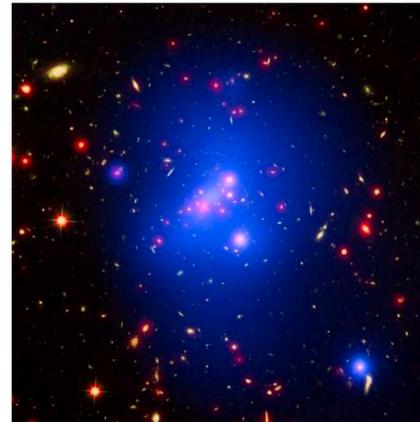
Galaxy rotation curves



Credit: Mario De Leo

- Mass fraction
- Distribution

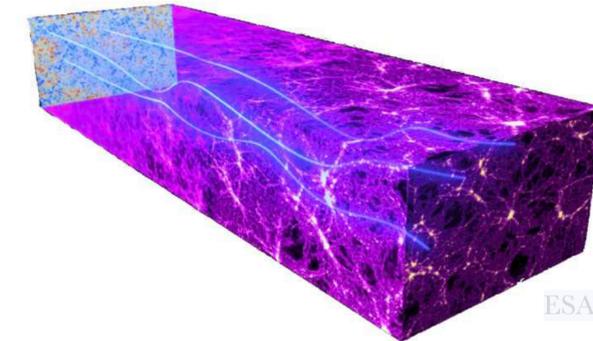
Clusters



CC BY 4.0

- Mass fraction
- Distribution

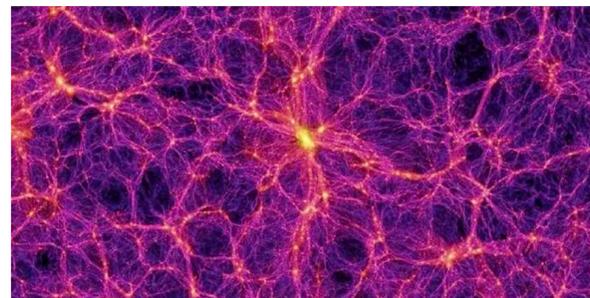
Lensing



ESA

- | | | |
|-----------------|----------------|-----------------|
| Strong lensing | Weak lensing | Micro lensing |
| • Mass fraction | • Distribution | • Mass fraction |
| • Distribution | • Shape | • Smoothness |
| | • Structure | |

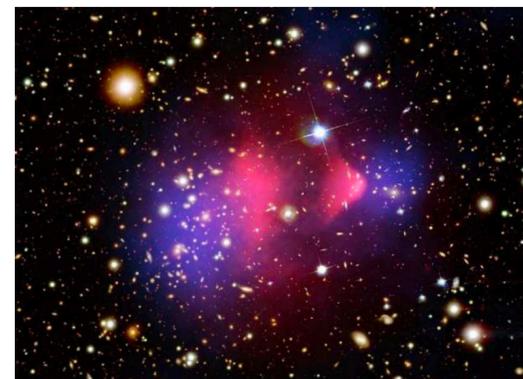
Large Scale Structure



Springel & others / Virgo Consortium

- CMB/LSS
- Ratio of DM/collisional matter
- Thermal history

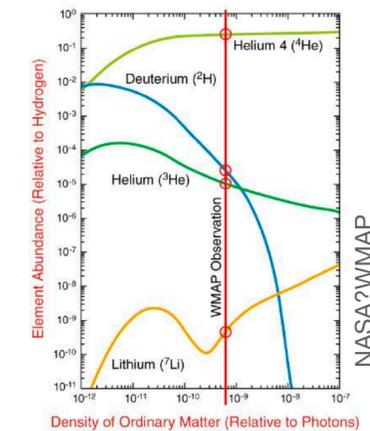
Cluster collision



NASA/CXC/CfA and NASA/STScI

- Distribution
- Separation from collisional matter
- Self-interaction

Big Bang Nucleosynthesis

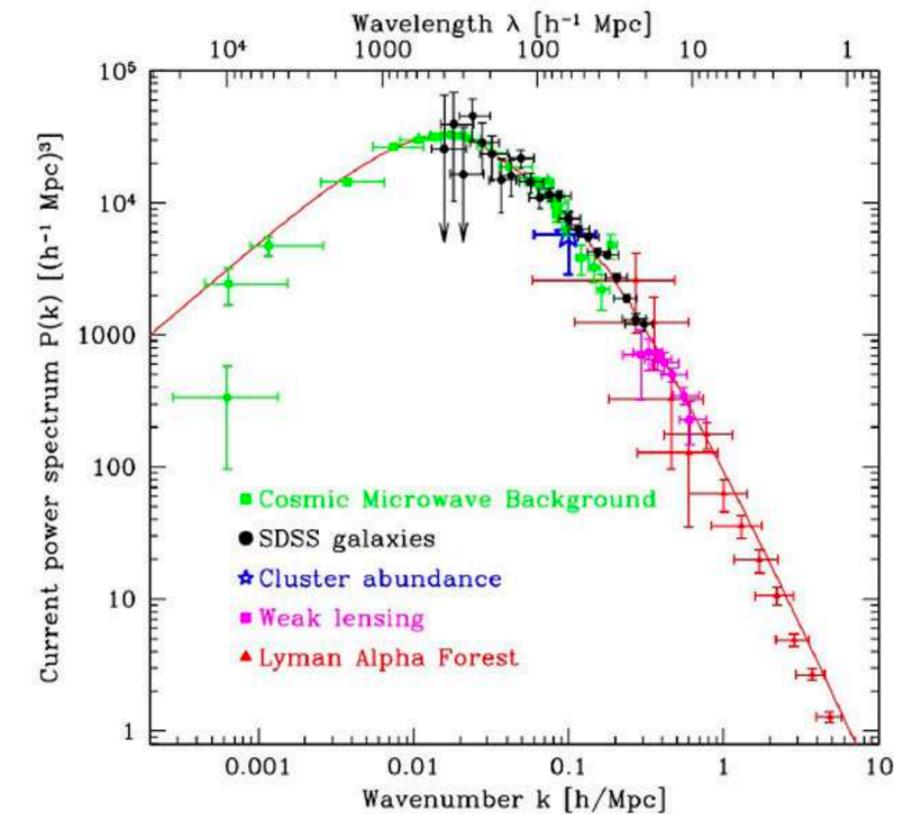


- Amount of baryons

Cold dark matter

Λ CDM

- **Cold:** moves much slower than c
- **Pressureless:** gravitational attractive, clusters
- **Dark** (transparent): no/weakly electromagnetic interaction
- **Collisionless:** no/weakly self-interaction or interaction with baryons
- **Abundance:** amount of dark matter today known



What we *don't* know

- What is DM? Nature

- ~~Cold~~ →

How cold it is? WDM

- ~~Pressureless~~ →

Cluster on all scales?

- ~~Dark~~ →

Non-gravitational interaction? Milicharged DM

- ~~Collisionless~~ →

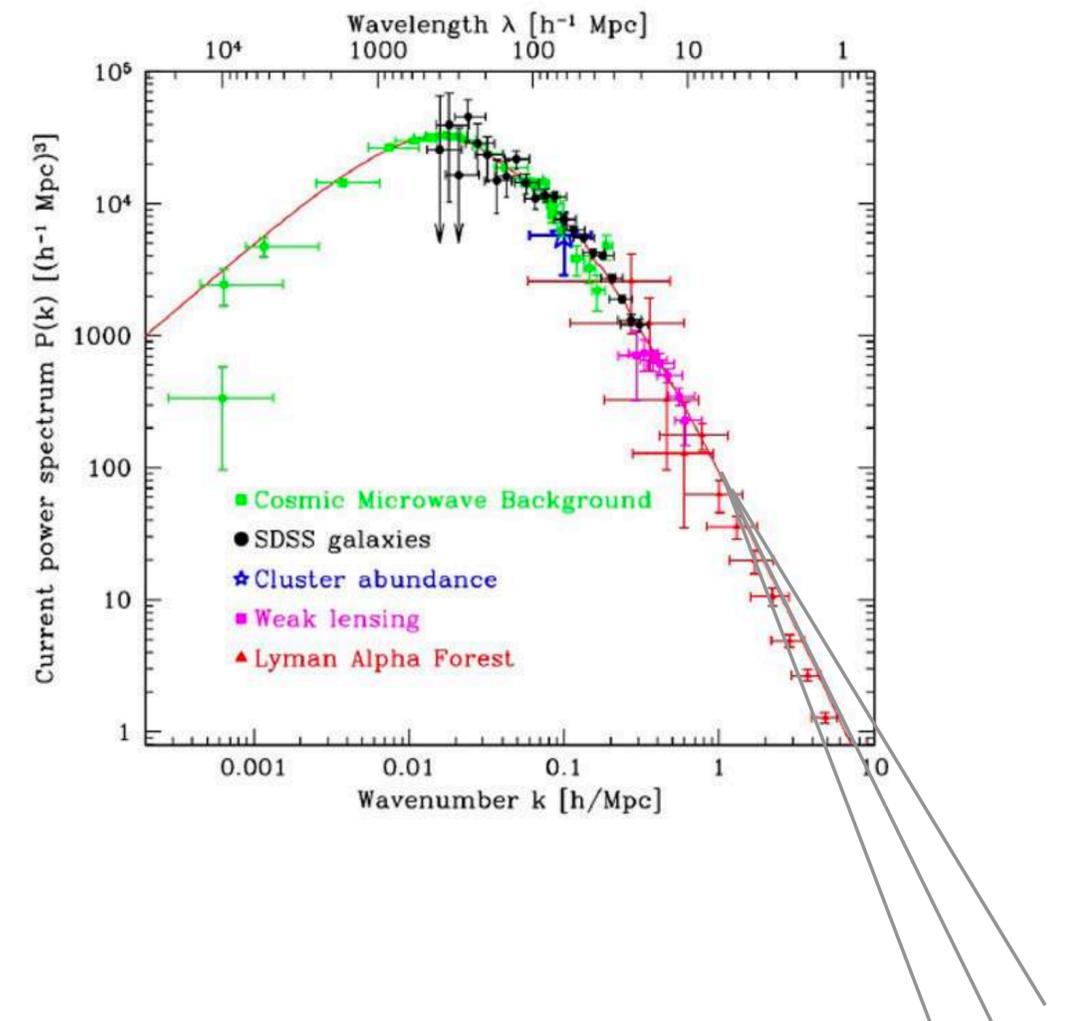
How small self-interaction? SIDM

Although still behaves like CDM on large scales

Small scale behaviour: still “weakly” constrained and small scale challenges

Small scale curiosities: **cusp-core**, missing satellites, BTFR, ...

Power spectrum: highly constrained for $k > 10 \text{ Mpc}^{-1}$
highly **un**constrained for $k < 10 \text{ Mpc}^{-1}$



Model building: pre-requisites for a *dark matter candidate*

- **Cold or warm**

Thermal candidate: $m_{dm} \geq \text{keV}$

Has to be non-relativistic at BBN Or produced cold by a non-thermal mechanism
- **Reproduce large and small scale distribution**

Clusters like pressure-less fluid on large scales $k \lesssim 10 \text{ Mpc}^{-1}$

Clustering on scales smaller than $k \gtrsim 10 \text{ Mpc}^{-1}$ highly unconstrained
- **Non-interacting or weakly interacting (Dark, collisionless)**

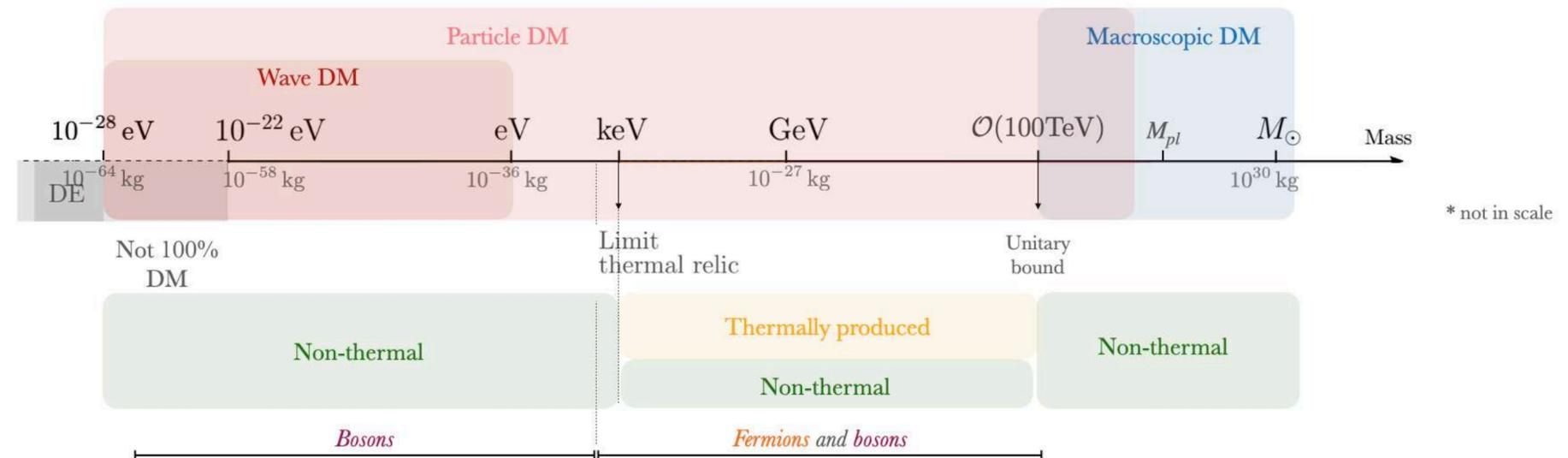
Can have a small electromagnetic interaction. Bound $< \text{milicharge}$; Can interact via the *weak force*

Can have a **self interaction**. Bounds: $\sigma/m_{dm} < 0.13 \text{ cm}^2/\text{g}$, $\sigma/m_{dm} < 0.35 \text{ cm}^2/\text{g}$
- **Abundance**

$\Omega_m = 0.308 \pm 0.012$ (*Planck 2018*)
- **Stable**

If it is a particle, it has to be stable with lifetime \gg than the age of the universe

Mass scale of
dark matter



What we *don't* know

- What is DM? What is the nature of DM?

State of the “art”



What is *dark matter*?

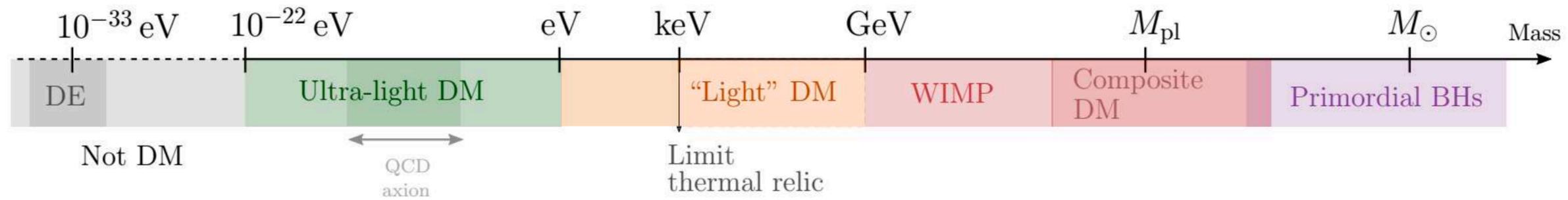
- What is the nature of DM?

State of the “art”



Mass scale of DM

80 orders of magnitude

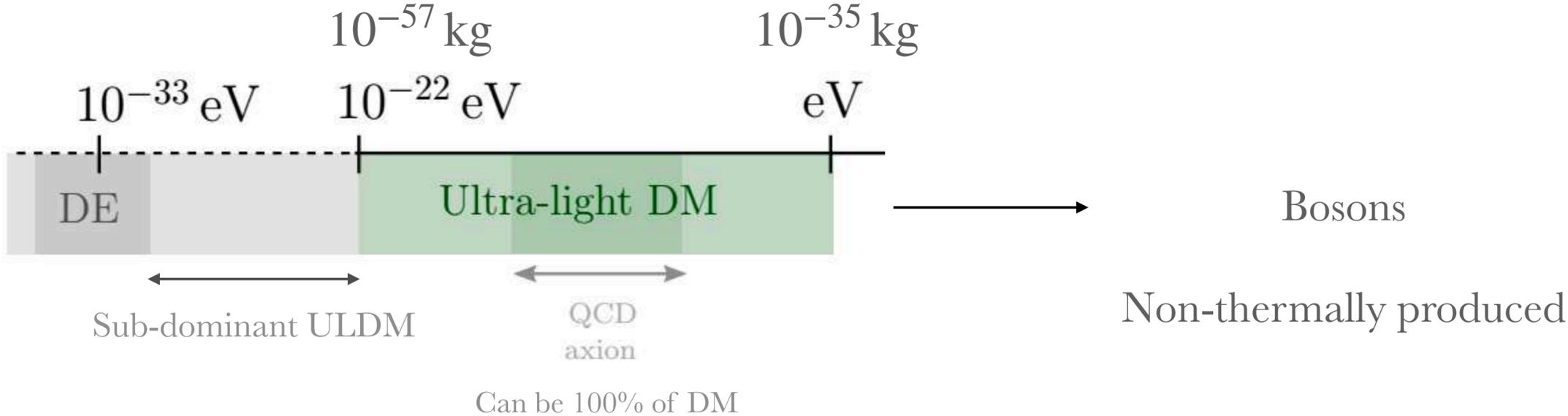
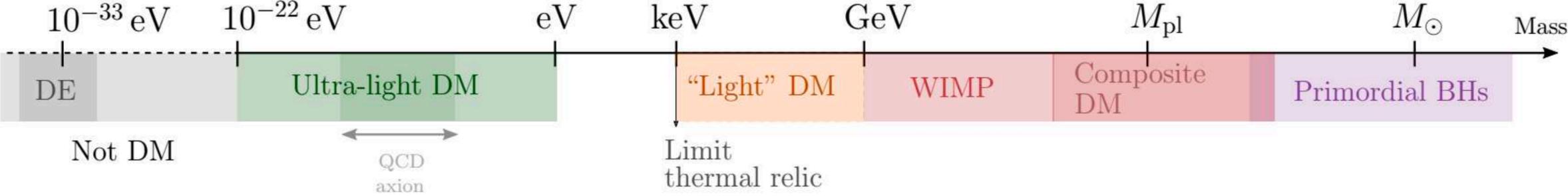


Ultra-light fields

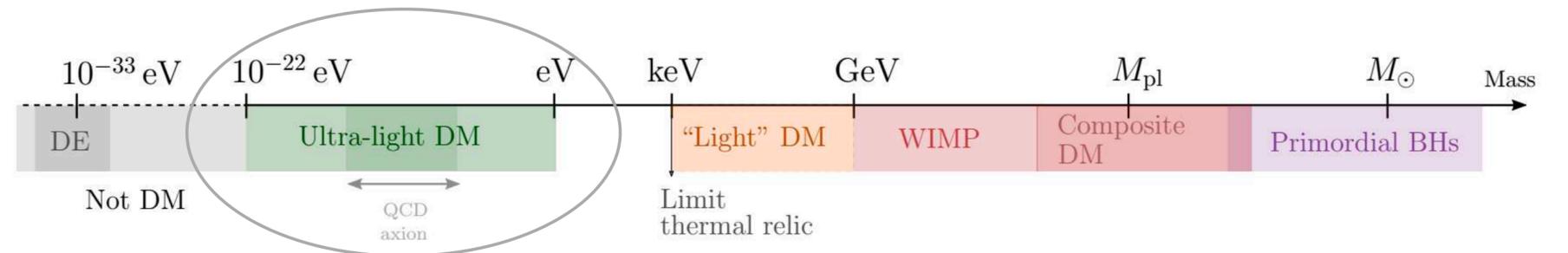
Ultra-light candidate, cold

Large $\lambda_{\text{dB}} \sim 1/mv$

Lightest possible candidate for DM or DE



Ultra-light dark matter

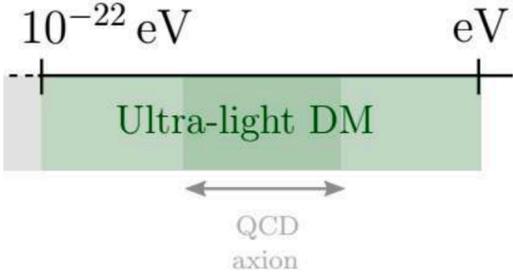


"Ultra-light dark matter", **E.Ferreira**, 2020.

"Wave dark matter", **Lam Hui**, 2020.

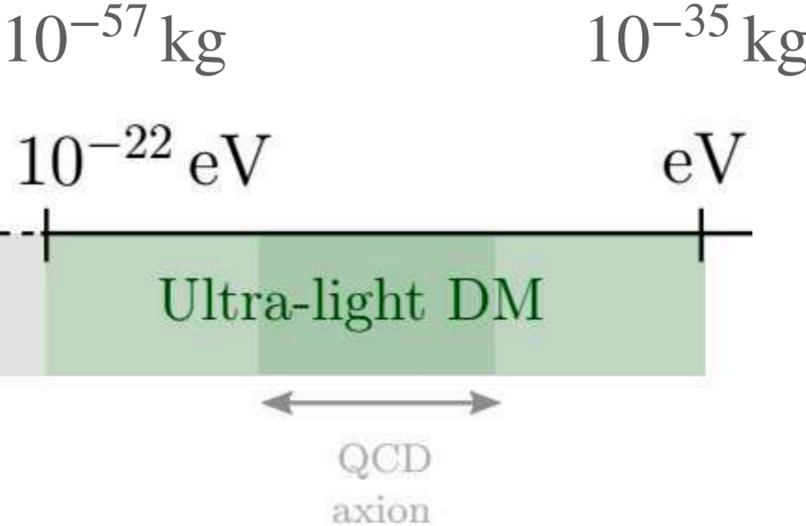
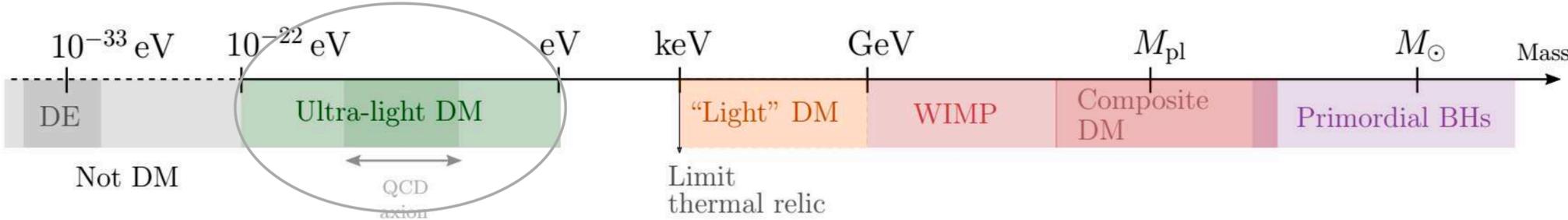
New review on ULDM, **Eberhardt, EF** (to appear)

Ultra-light *Dark Matter*



Ultra-light candidate, cold \longrightarrow Large $\lambda_{\text{dB}} \sim 1/mv$

Lightest possible candidate for DM

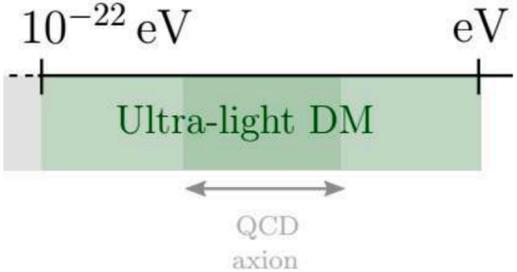


\longrightarrow

Bosons

Non-thermally produced

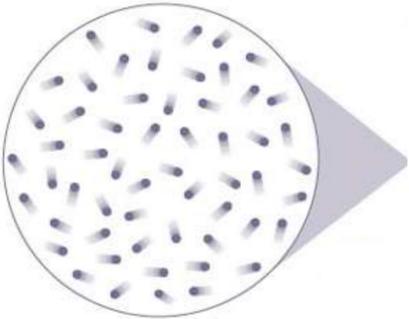
Ultra-light *Dark Matter*



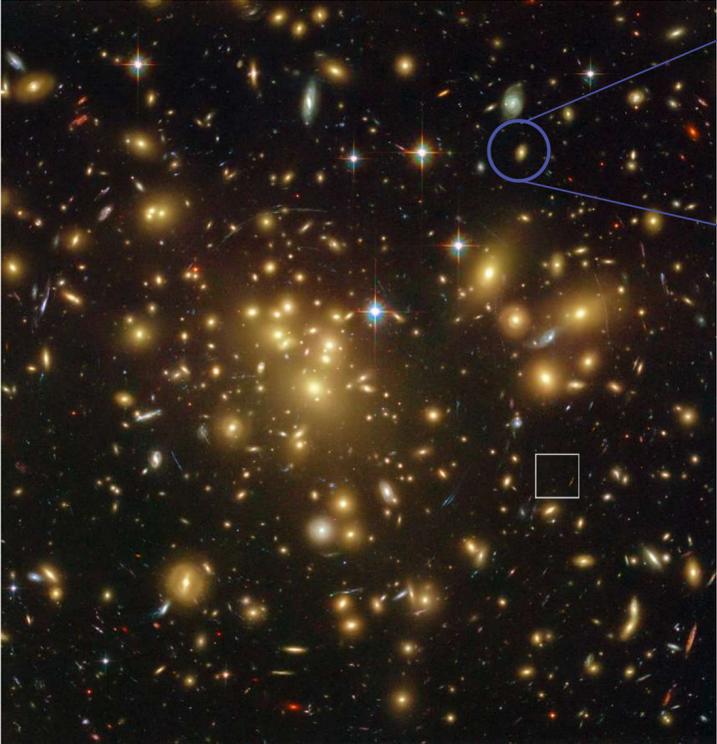
Ultra-light candidate \longrightarrow Large $\lambda_{dB} \sim 1/mv$

Lightest possible candidate for DM

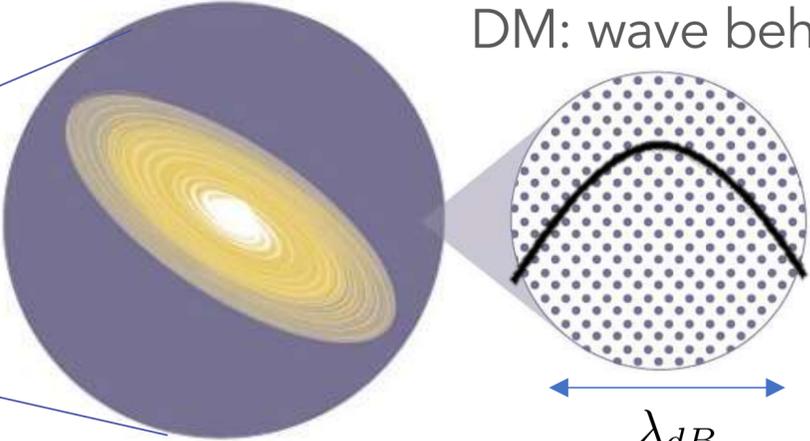
Large scales:
DM behaves like standard particle DM (**CDM**).



DM: particles
 $d \gg \lambda_{dB}$



Adapted from Quanta



Galaxy halo

DM: wave behaviour

λ_{dB}
 $d \ll \lambda_{dB}$

Small scales:
DM behaves like a **wave**

$$10^{-25} \text{ eV} \lesssim m \lesssim \text{eV}$$

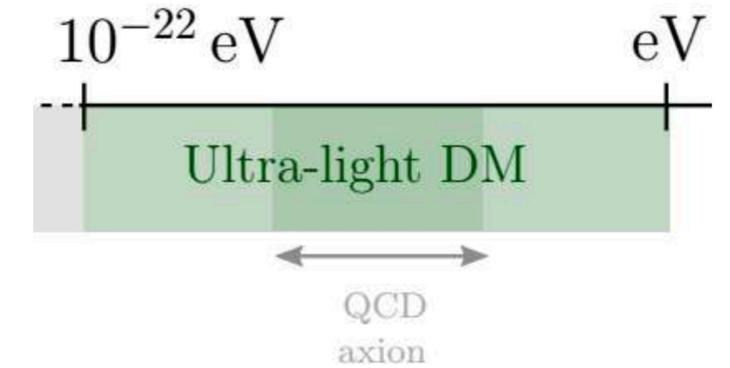
$$\lambda_{dB}^{ULDM} \sim \text{pc} - \text{kpc}$$

Motivation: *particle physics*

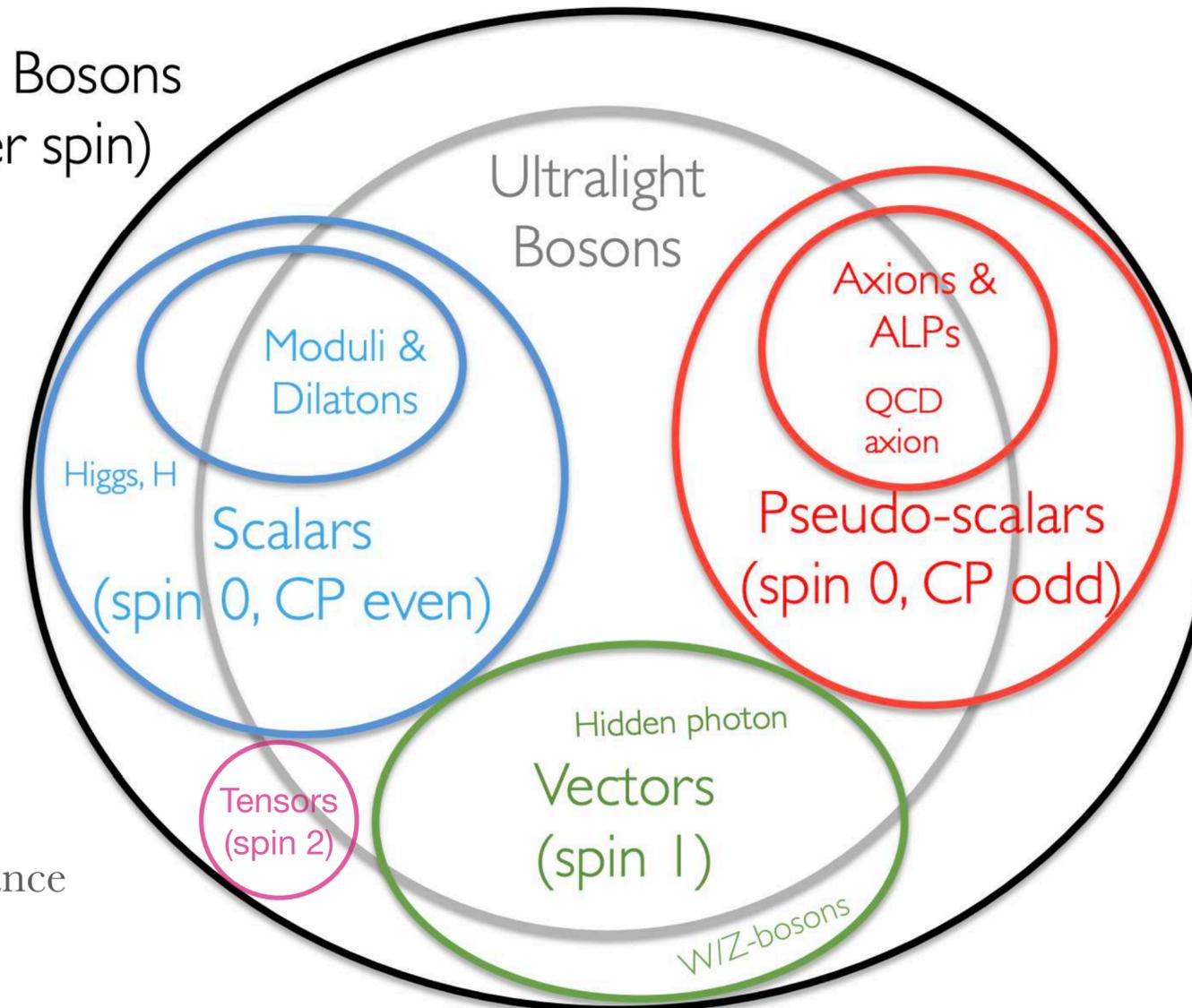
ULDM candidates

Natural candidate for a light scalar field is a pseudo-Nambu Goldstone boson

Many extensions of the Standard Model predict additional massive bosons



Massive Bosons
(integer spin)

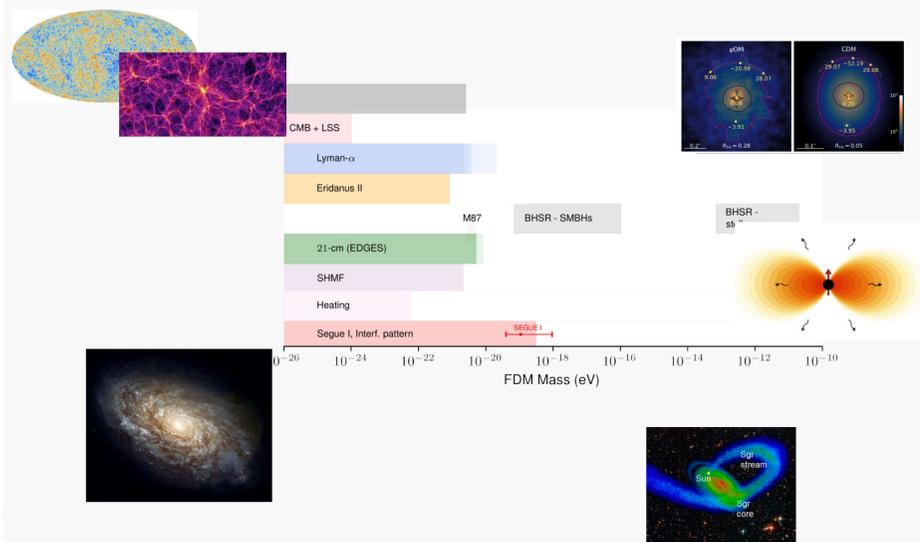


- Formation mechanism: needs to have a relic abundance that gives the correct DM abundance

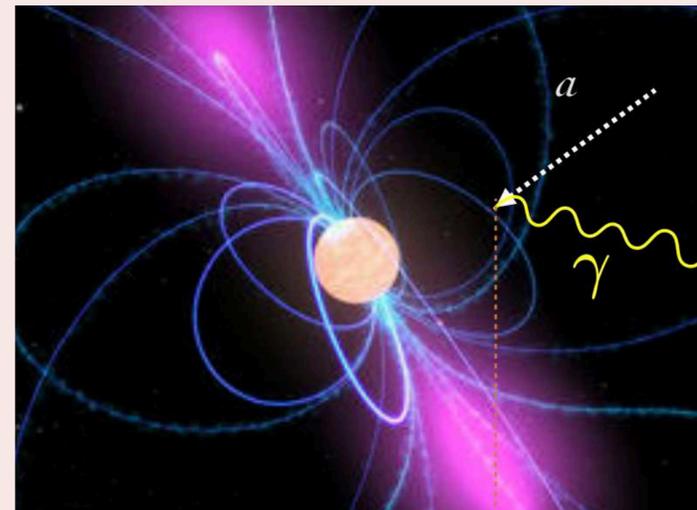
Outline

This talk!

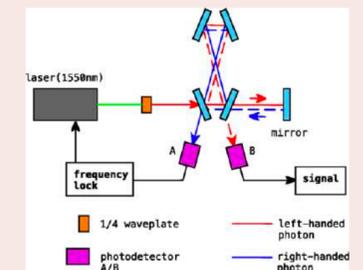
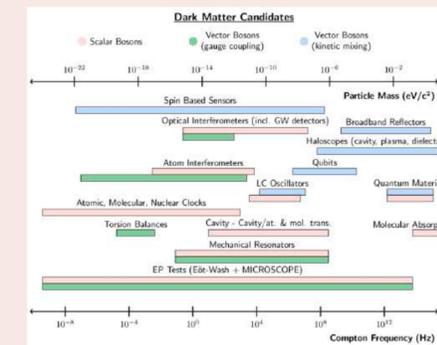
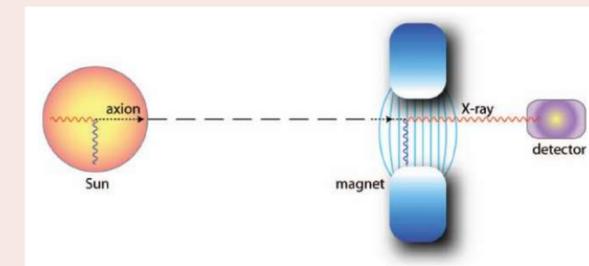
Cosmological and astrophysical searches



Indirect detection



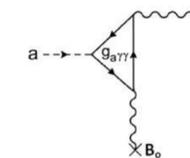
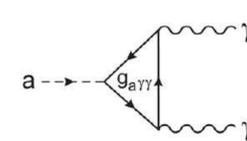
"Direct detection" Axion/ALPs experiments



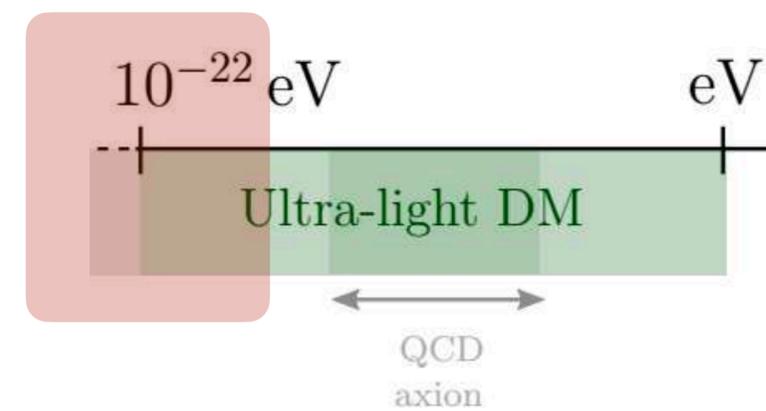
Gravitational

For most of this talk:
Gravitational signatures!

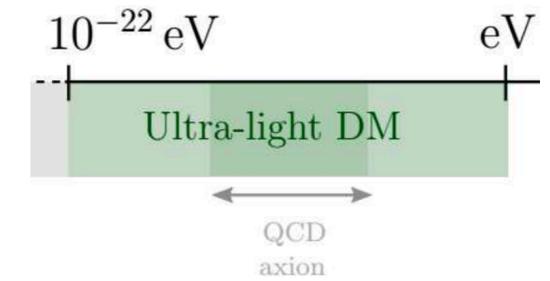
Interactions with the SM



Astrophysical signatures



Ultra-light Dark Matter -classes



3 classes:

Fuzzy DM (FDM)

- Gravitationally bounded ultra-light scalar field model

m

Self Interacting FDM (SIFDM)

- Presence of (weakly) self-interaction

m

g

DM Superfluid

- Forms a superfluid in galaxies
- MOND behaviour interior of galaxies

Axion and ALP (axion like particles)

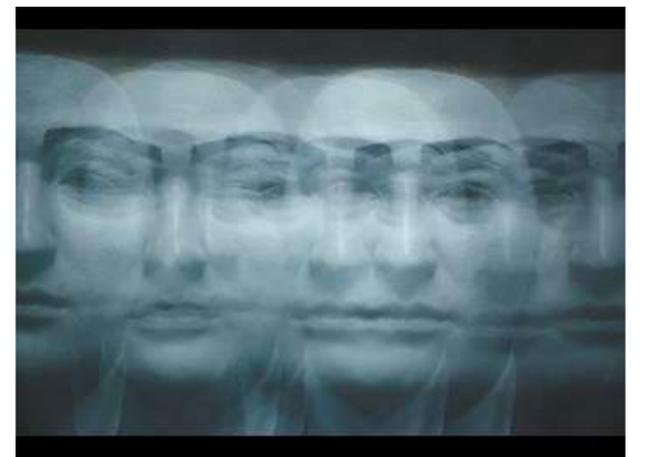
$$i\dot{\psi} = \left(-\frac{1}{2m} \nabla^2 + \frac{g}{8m^2} |\psi|^2 - m\Phi \right) \psi$$

$$\mathcal{L} = P(X)$$

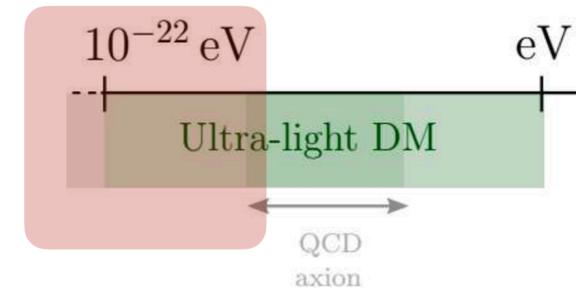
→ Connection with condensed matter and particle physics!

“Ultra-light dark matter”, **E.Ferreira**, 2020. *The Astronomy and Astrophysics Review*.

Fuzzy dark matter



Fuzzy Dark Matter



Fuzzy DM (FDM)

- Gravitationally bounded ultra-light scalar field model

m

Wave DM Ultra-light axions

Focus *more* on spin 0 particles here!

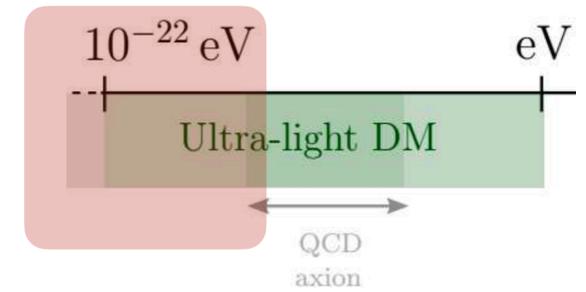
$$10^{-22} \text{ eV} \lesssim m \lesssim 10^{-17} \text{ eV}$$

Hu W, Barkana R, Gruzinov A (2000 a,b)

(Reviews: *EF (2021)*, *J. Niemeyer (2019)*, *L. Hui (2021)*)

Cosmological evolution

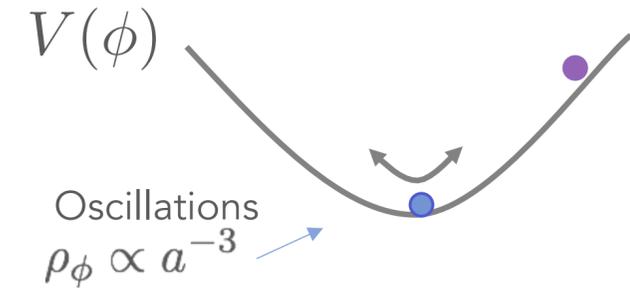
Boson/ Scalar field in a cosmological (FRW) background



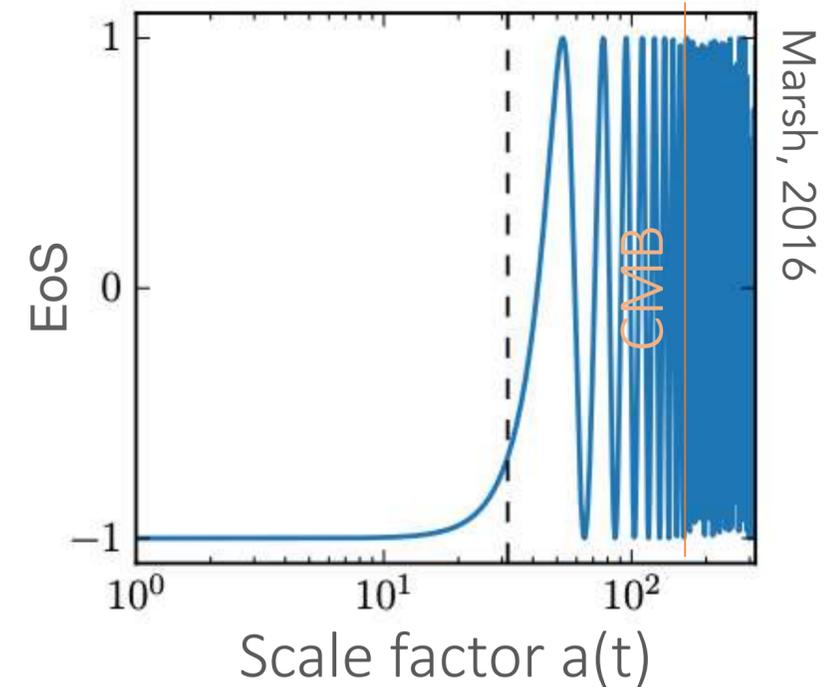
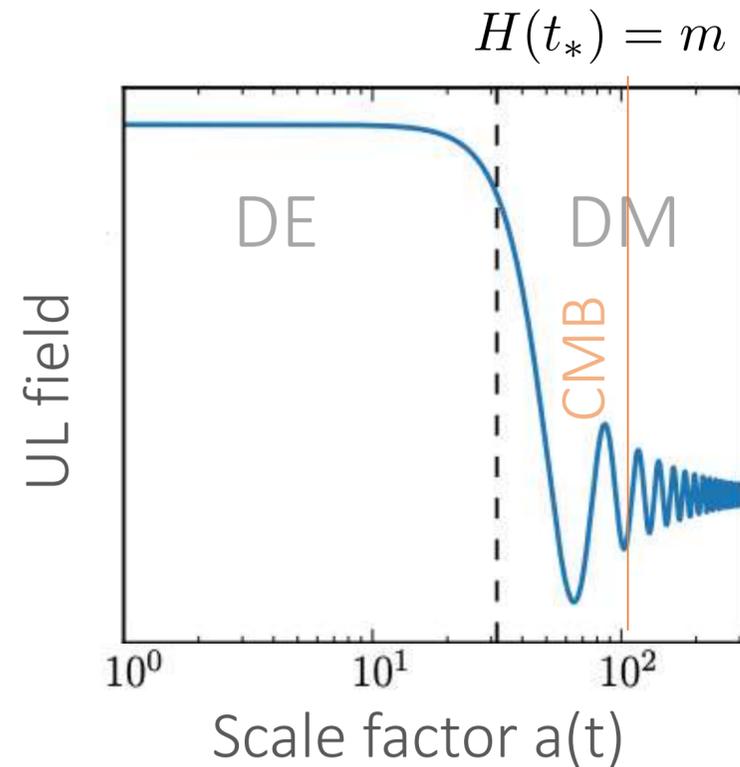
$$\ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$$

FDM

{	$H \gg m$	\implies	$\phi_{\text{early}} = \phi(t_i)$	\longrightarrow	$\omega = -1$	DE
	$H \ll m$	\implies	$\phi_{\text{late}} \propto e^{imt}$	\longrightarrow	$\langle \omega \rangle = 0$	DM



$m > 10^{-28} \text{ eV} \sim H(a_{\text{eq}})$



Ultra-light fields as Dark Energy

Behave as (most of) dynamical dark energy with $w \sim -1$ for

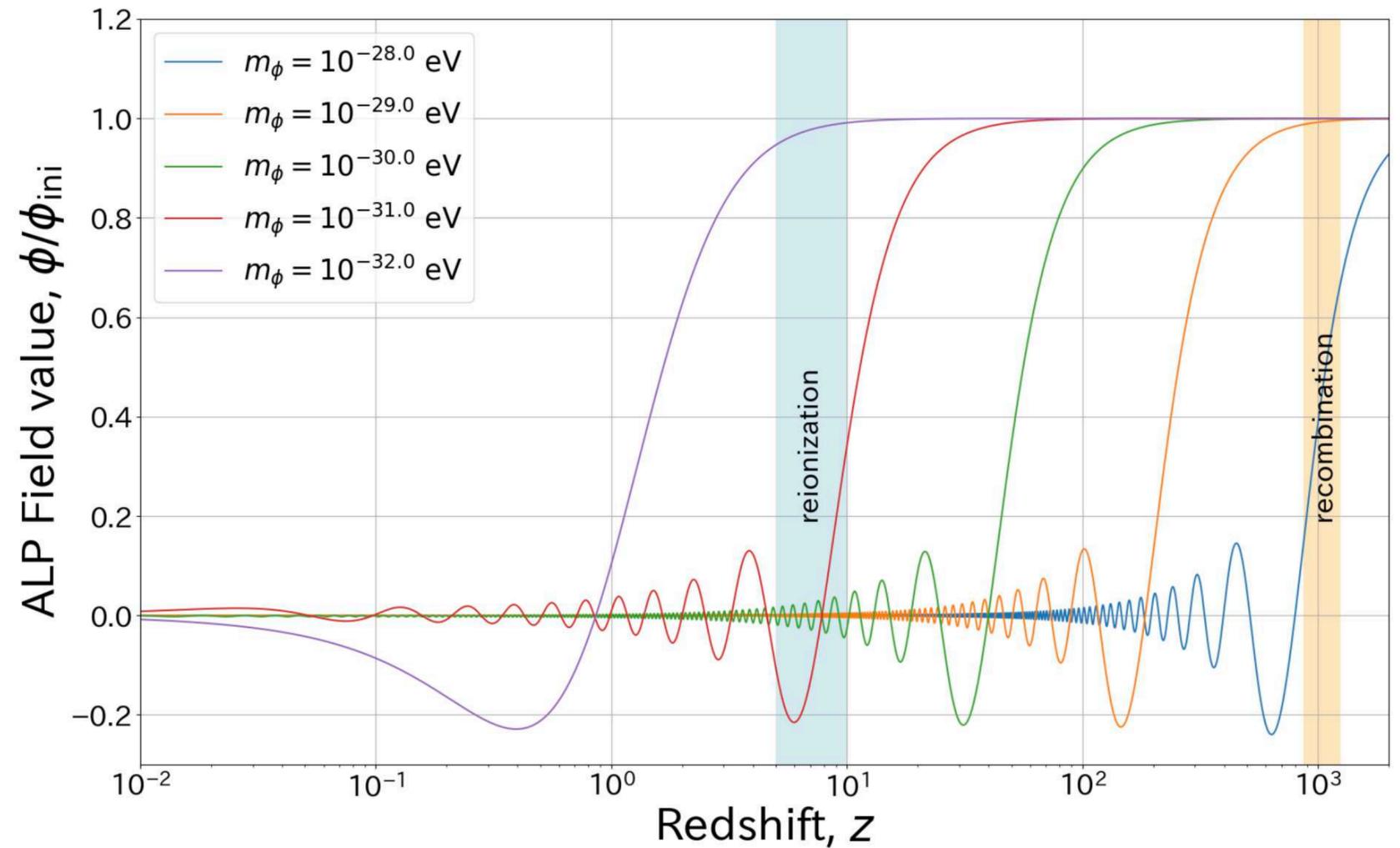
$$m_{\text{fdm}} < 10^{-32} \text{ eV}$$

Like quintessence with an axion-like potential:

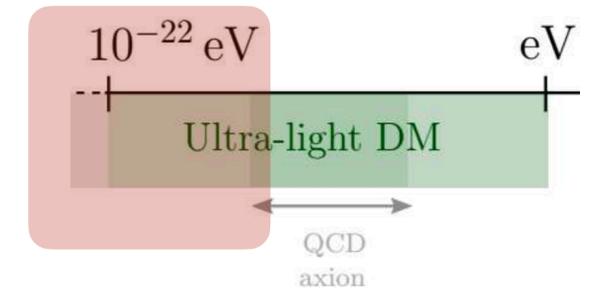
$$V(\phi) = \Lambda^4 [1 - \cos(\phi/f_a)]^n$$

$$\Lambda^2 = m_a f_a$$

(Also early dark energy)



Structure formation - *non-relativistic regime*



Evolution on small scales: take non-relativistic regime of the theory, relevant for structure formation.

Schrödinger-Poisson system : describe the FDM and the SIFDM

$$\left\{ \begin{array}{l} i\dot{\psi} = \left(-\frac{1}{2m}\nabla^2 + \frac{g}{8m^2}|\psi|^2 - m\Phi \right) \psi \\ \nabla^2\Phi = 4\pi G(m|\psi|^2 - \bar{\rho}) \end{array} \right.$$

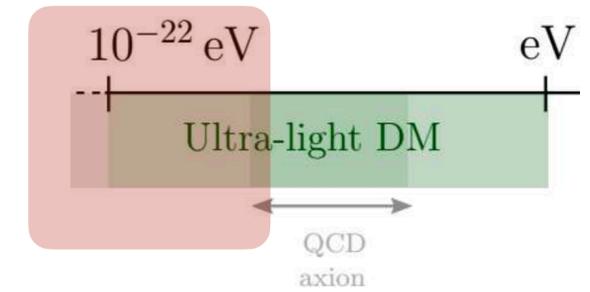
Schrödinger equation
(Gross-Pitaevskii)

Poisson equation

$g = 0 \longrightarrow$ FDM
 $g \neq 0 \longrightarrow$ SIFDM

Fundamentally different than
CDM/WDM/SIDM!

Structure formation - non-relativistic regime



Evolution on small scales: take non-relativistic regime of the theory, relevant for structure formation.

Schrödinger-Poisson system : describe the FDM and the SIFDM

$$\begin{cases} i\dot{\psi} = \left(-\frac{1}{2m}\nabla^2 + \frac{g}{8m^2}|\psi|^2 - m\Phi \right) \psi \\ \nabla^2\Phi = 4\pi G(m|\psi|^2 - \bar{\rho}) \end{cases}$$

Schrödinger equation
(Gross-Pitaevskii)

Poisson equation

$g = 0 \rightarrow$ FDM
 $g \neq 0 \rightarrow$ SIFDM

Fundamentally different than
CDM/WDM/SIDM!

Madelung equations

$(\psi \equiv \sqrt{\rho/m} e^{i\theta} \text{ and } \mathbf{v} \equiv \nabla\theta/m)$

$$\dot{\rho} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\dot{\mathbf{v}} + (\mathbf{v} \cdot \nabla)\mathbf{v} = -\frac{1}{m} \left(V_{grav} - P_{int} - \frac{1}{2m} \frac{\nabla^2 \sqrt{\rho}}{\sqrt{\rho}} \right)$$

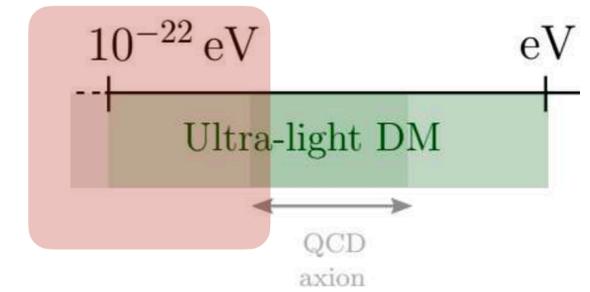
$$P_{int} = K\rho^{(j+1)/j} = \frac{g}{2m^2}\rho^2$$

Quantum pressure

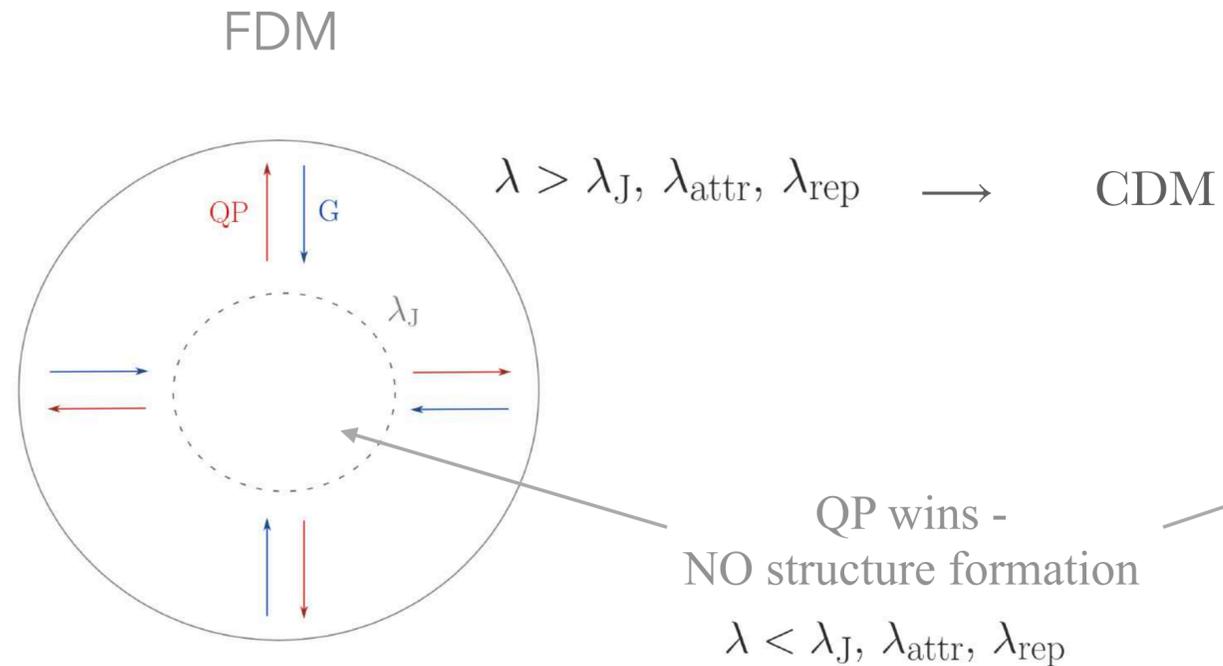
Finite Jeans length -
Suppresses
structure formation
on small scales

FLUID
DESCRIPTION

Structure formation - perturbation and stability



Finite clustering scale - no structure formation on small scales



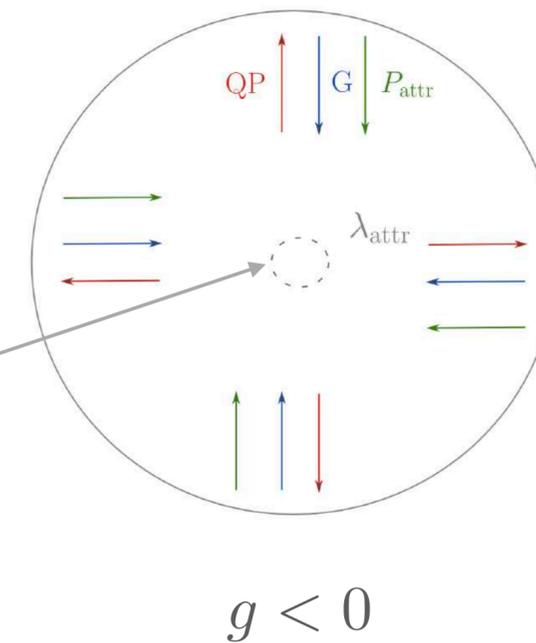
Finite size coherent core – Bose stars

$$\lambda_J = 55 \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-1/2} \left(\frac{\rho}{\bar{\rho}} \right)^{-1/4} (\Omega_m h)^{-1/4} \text{ kpc}$$

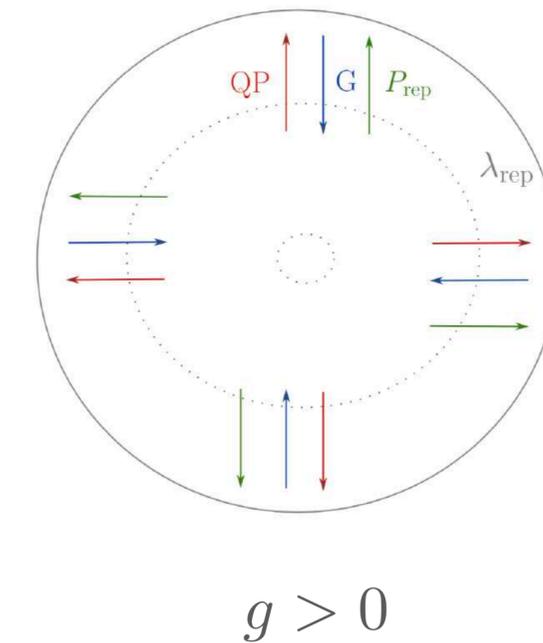
$m \leq 10^{-20} \text{ eV} \Rightarrow \lambda_{dB} > \mathcal{O}(\text{kpc})$ Galactic scales

SIFDM

ATTRACTIVE



REPULSIVE

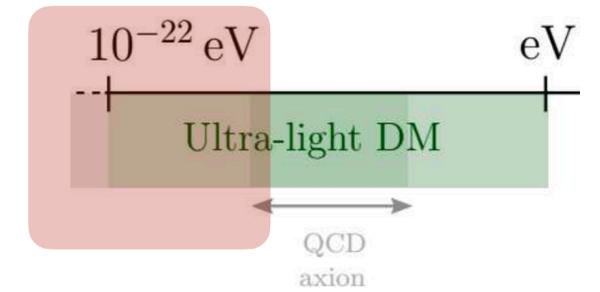


For attractive interactions can only form localized clumps (solitons)

QCD axion: $m \sim 10^{-5} \text{ eV}$
 $\lambda_a \sim -10^{-48}$ \rightarrow $l_{soliton} \sim 10^{-5} \text{ kpc}$

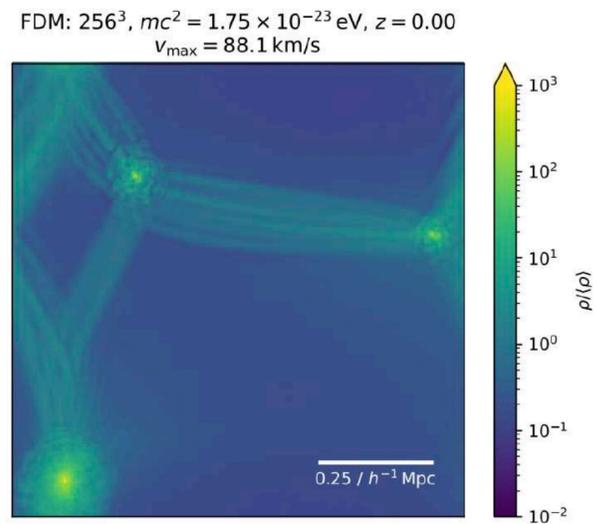
Phenomenology

RICH PHENOMENOLOGY ON SMALL SCALES

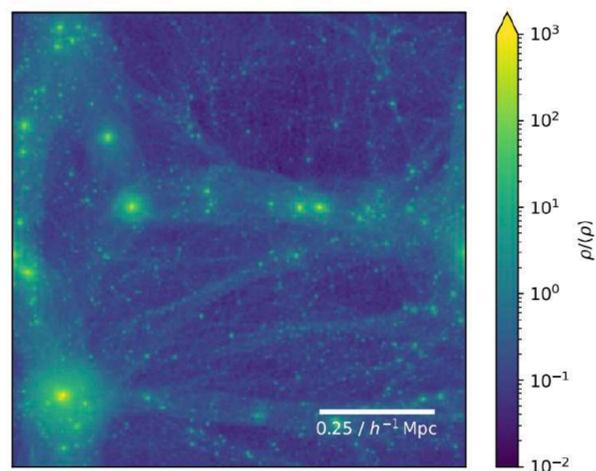


* Focus only in gravitational signatures

Suppression of small structures

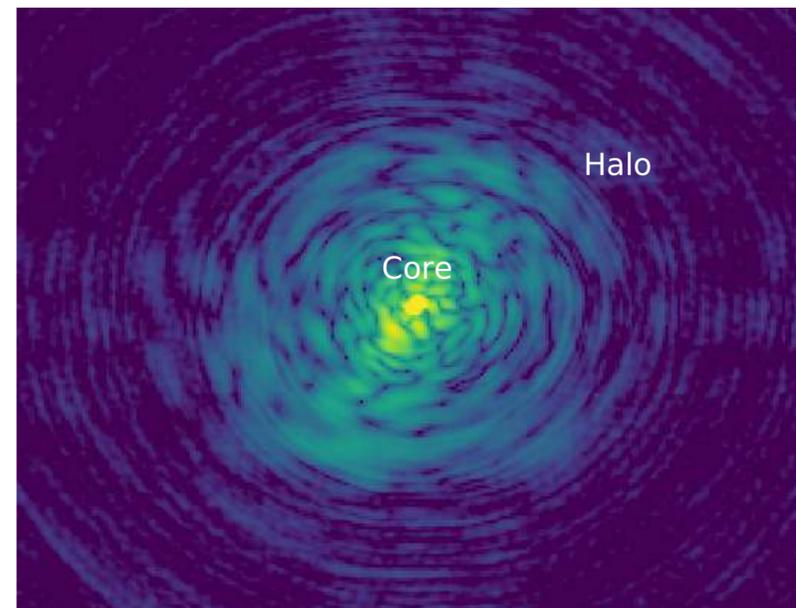


CDM: 256^3 , $z = 0.00$

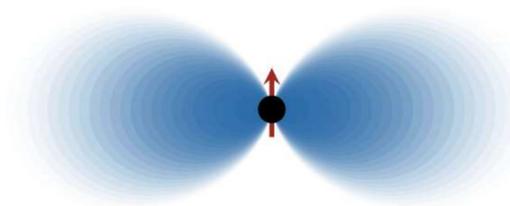


S. May et al. 2021

Formation of a solitonic core

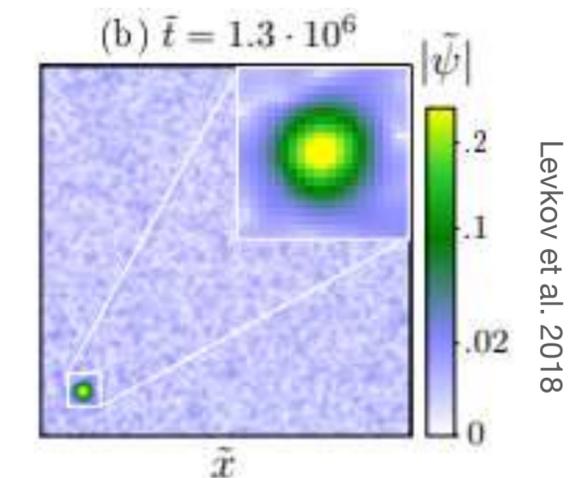


Axion clouds

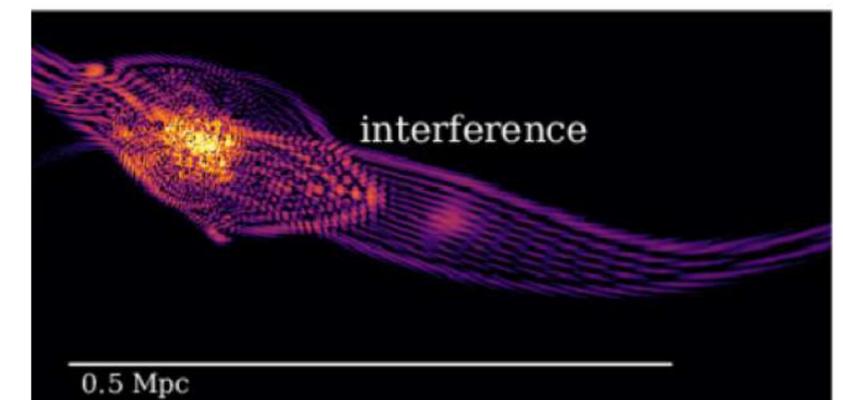


Baumann et al. 2019

Dynamical effects



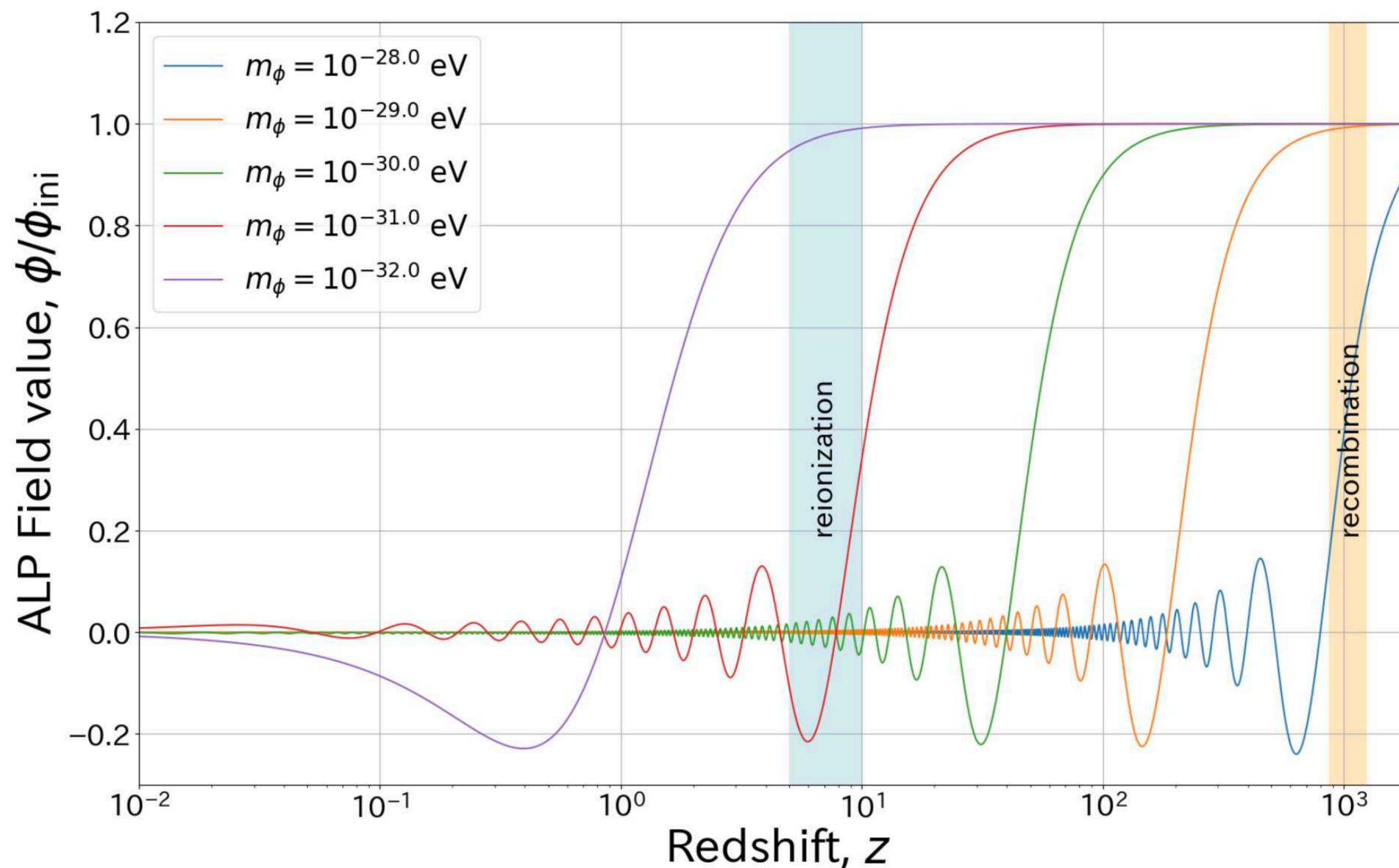
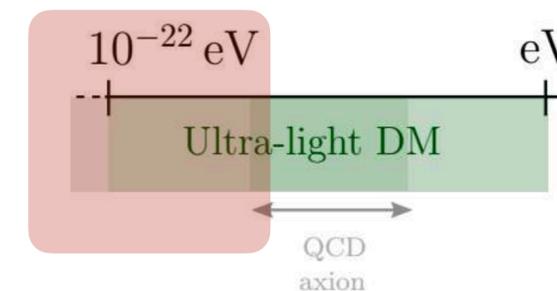
Wave interference



Mocz et al. 2017

Linear evolution

Boson/ Scalar field in a cosmological (FRW) background



Boltzmann codes: axionCAMB, axionECAMB, AxiCLASS

New emulator (to appear *soon*)

Condition DM today:

$$m > 10^{-28} \text{ eV} \sim H(a_{\text{eq}})$$

Non-linear evolution - *simulations*

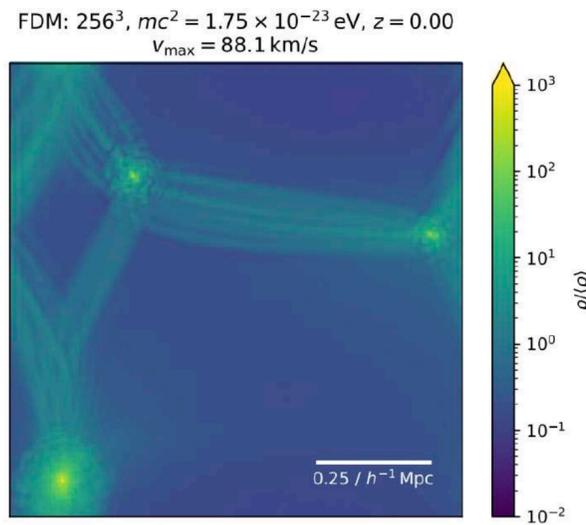
Pseudo-spectral methods

Solves the Schrödinger-Poisson equations.

→ Used widely in the field to simulate: isolated halos, the formation of cores, and cosmological simulations

Expensive! $\Delta t \sim \Delta x^2$

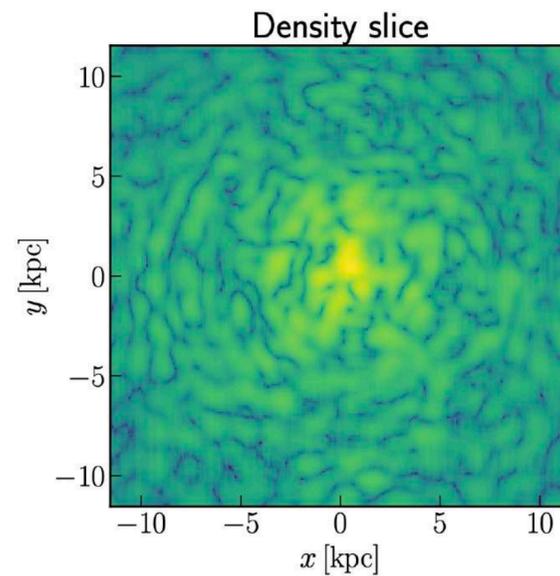
Largest to date:
10/Mpc/h



S. May et al. 2021

Mock halo generation

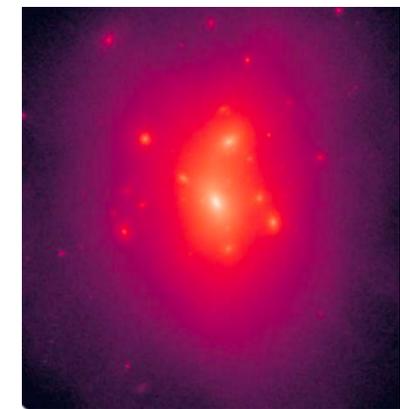
- Soliton collisions
- Eigenvalue decomposition: semi-analytical model to describe the halo



Eberhardt et al. 2024

Approximation schemes

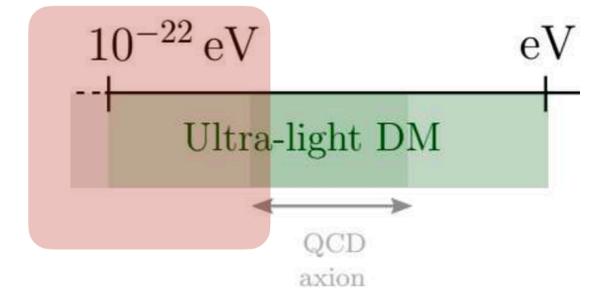
- Eigenvalue solvers
- Madelung simulations
- **N-body schemes** (or initial condition sims)



Nadler et al. 2024

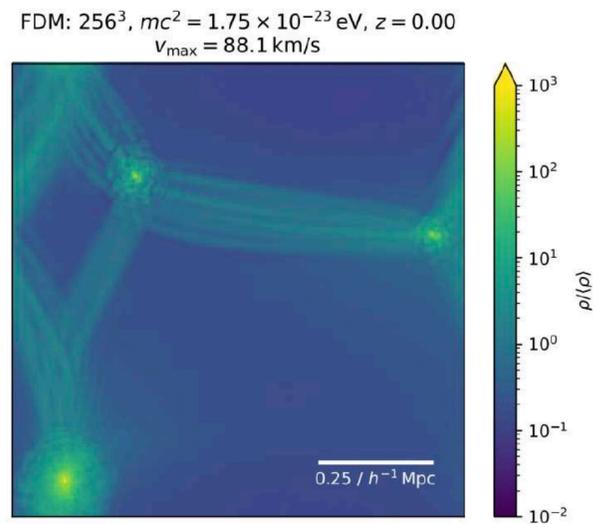
Phenomenology

RICH PHENOMENOLOGY ON SMALL SCALES

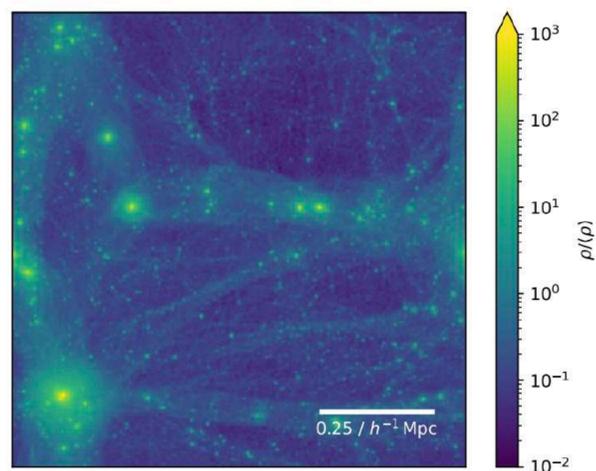


* Focus only in gravitational signatures

Suppression of small structures

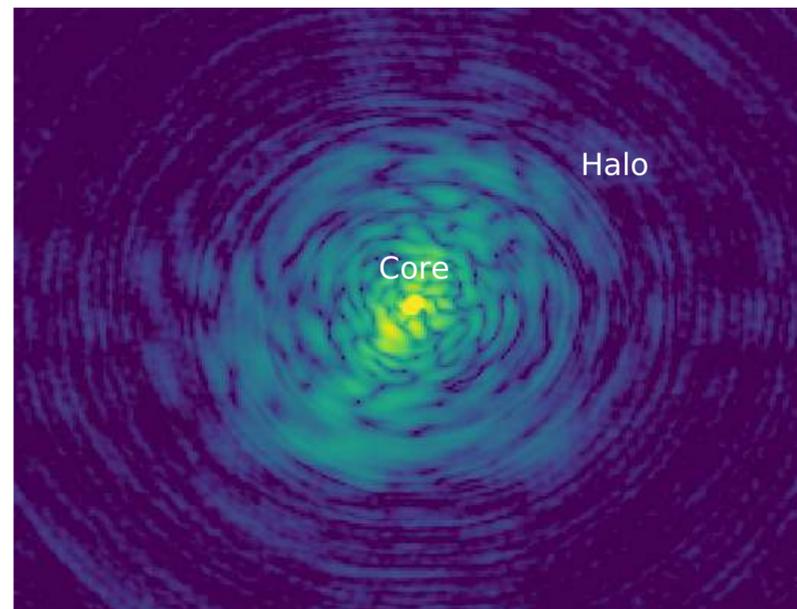


CDM: 256^3 , $z = 0.00$

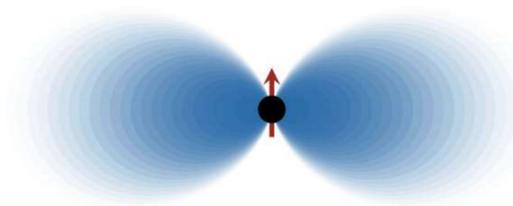


S. May et al. 2021

Formation of a solitonic core

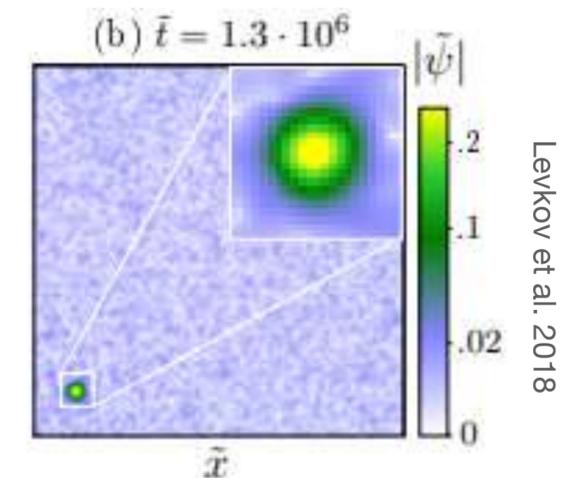


Axion clouds

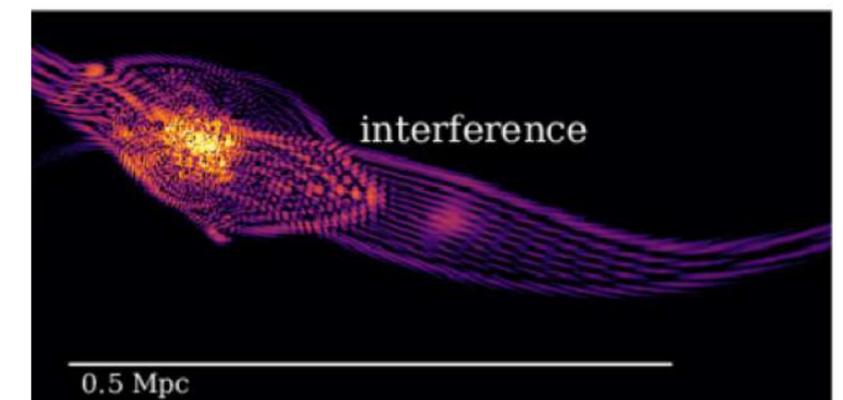


Baumann et al. 2019

Dynamical effects



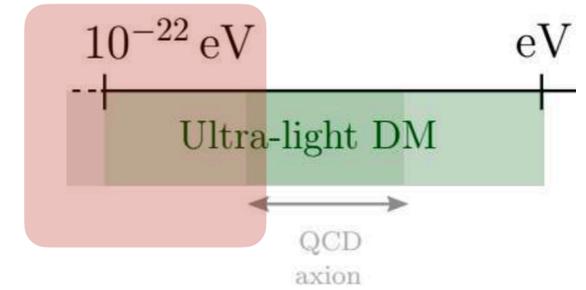
Wave interference



Mocz et al. 2017

Phenomenology

Suppression of small structures

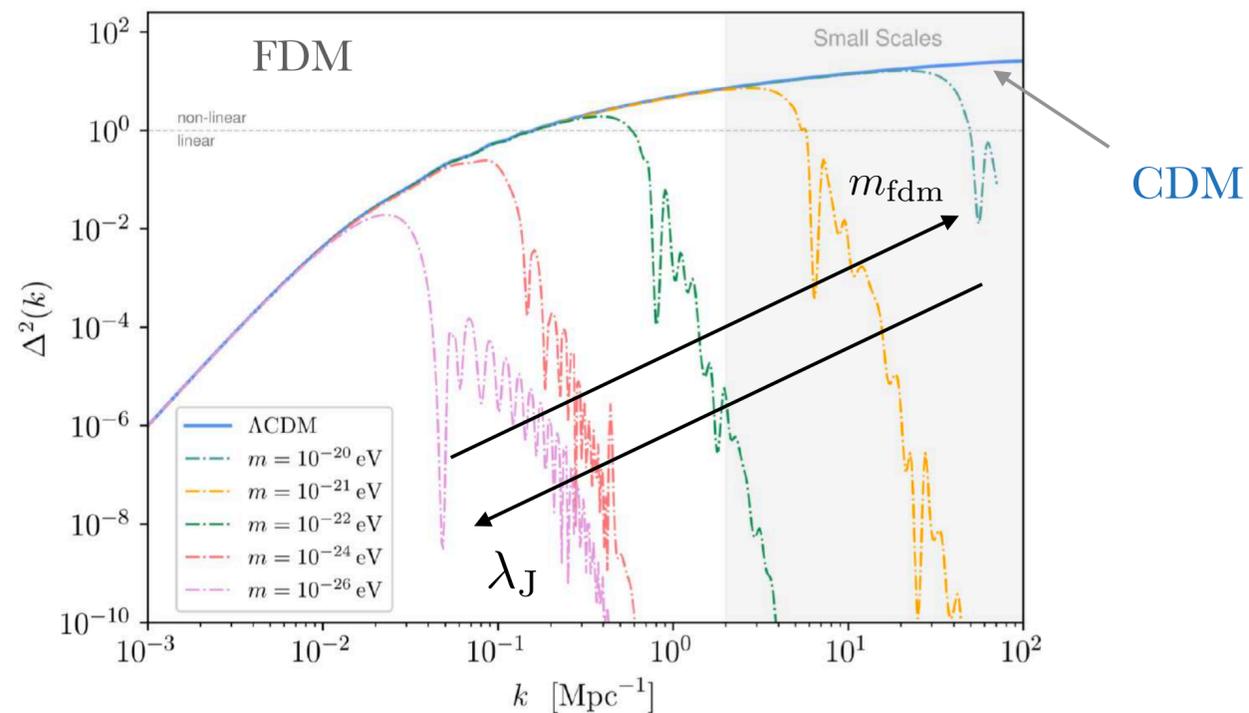


Finite Jeans length λ_J or $\lambda_{\text{attr}}, \lambda_{\text{rep}}$

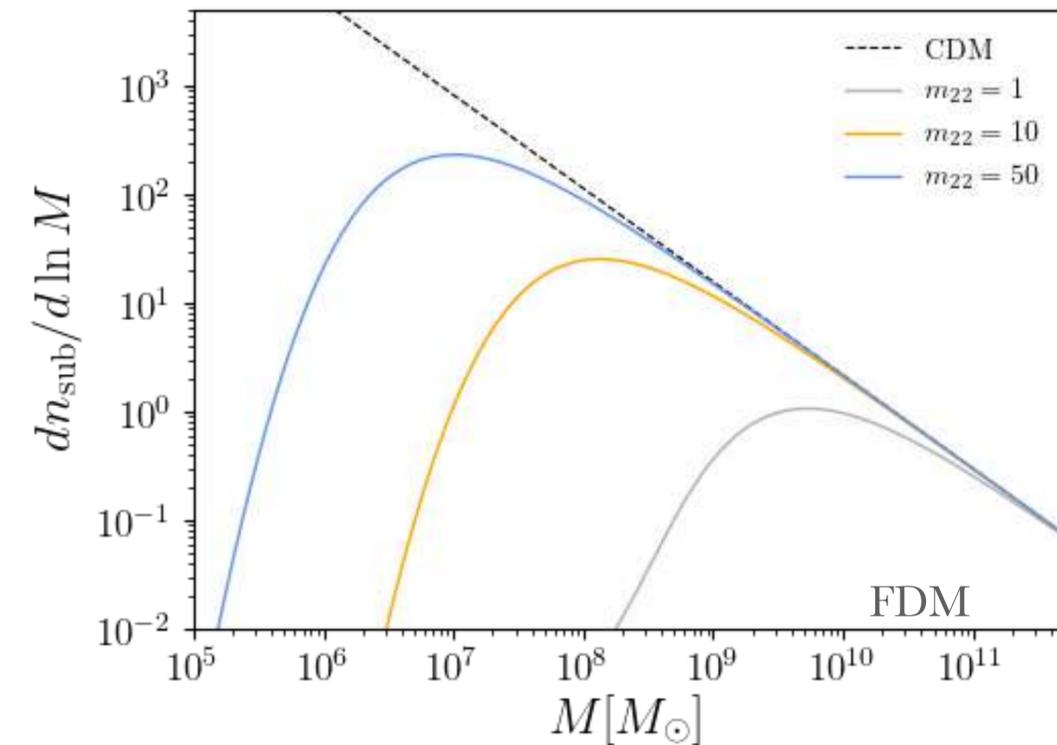
$$\lambda_J = 55 \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-1/2} \left(\frac{\rho}{\bar{\rho}} \right)^{-1/4} (\Omega_m h)^{-1/4} \text{ kpc}$$

Suppresses small scale structure

POWER SPECTRUM



(sub) HALO MASS FUNCTION

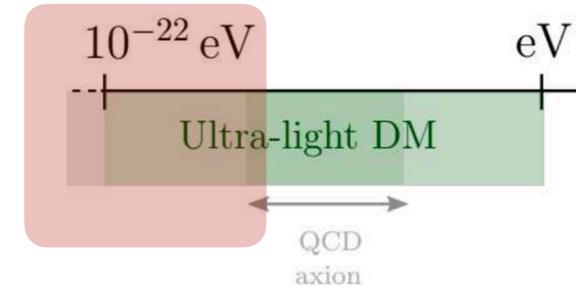


Power spectrum: highly constrained for $k > 10 \text{ Mpc}^{-1}$
 unconstrained for $k < 10 \text{ Mpc}^{-1}$

* hard to get a proper prediction!

Phenomenology

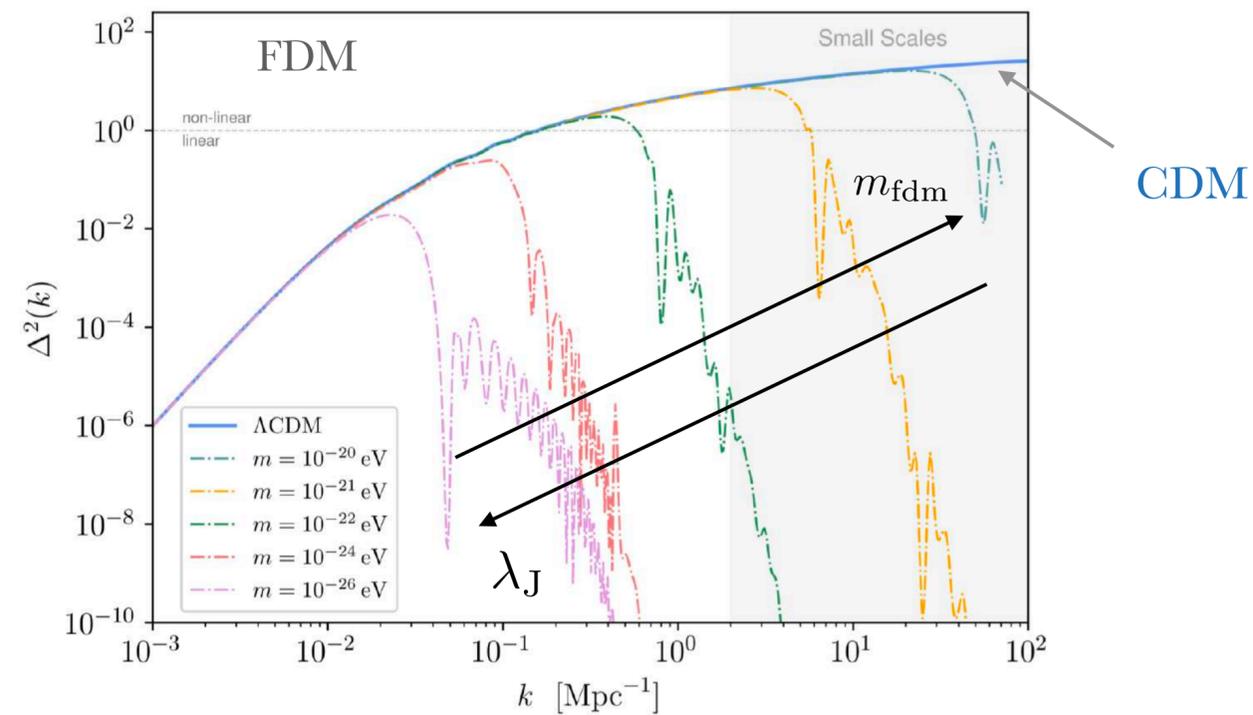
Suppression of small structures



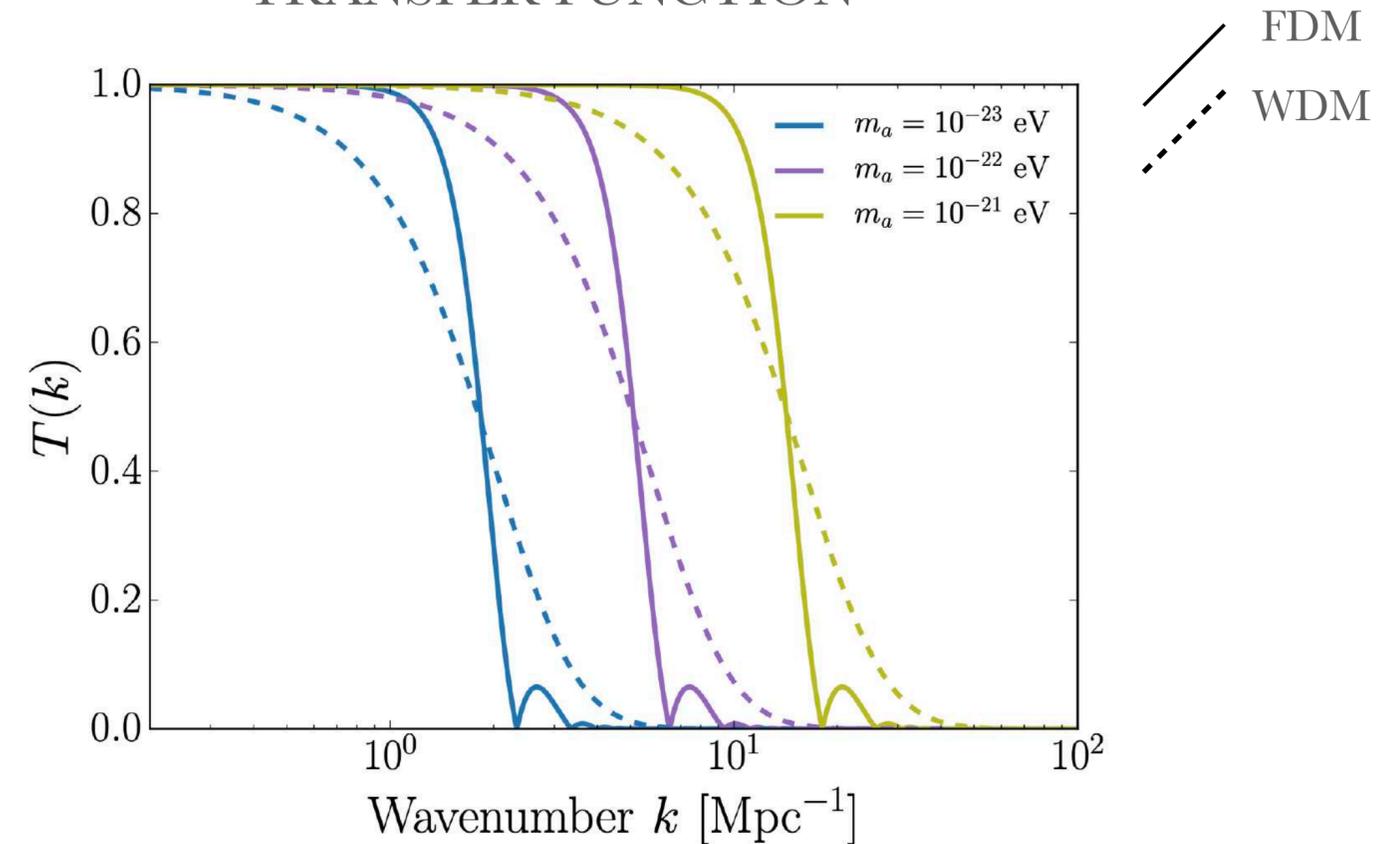
Finite Jeans length λ_J or $\lambda_{\text{attr}}, \lambda_{\text{rep}}$ \longrightarrow

Suppresses small scale structure

POWER SPECTRUM

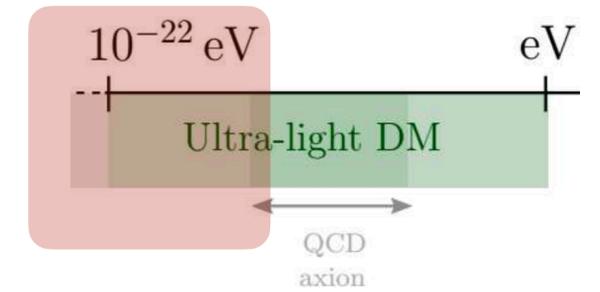


TRANSFER FUNCTION



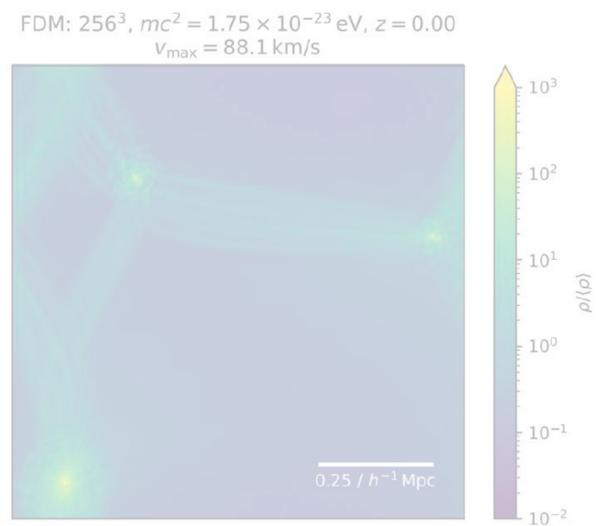
- Degenerate with WDM

Phenomenology

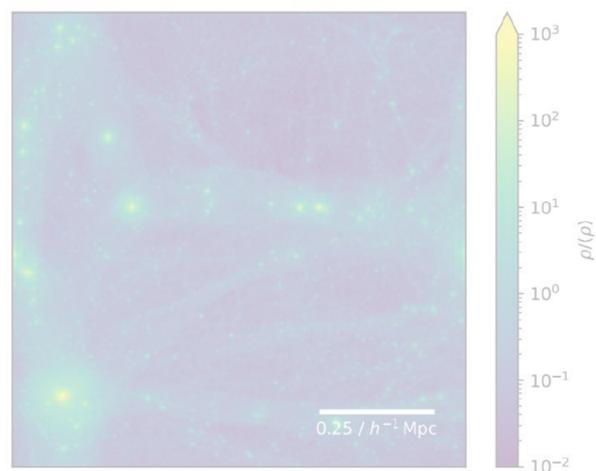


RICH PHENOMENOLOGY ON SMALL SCALES

Suppression of small structures

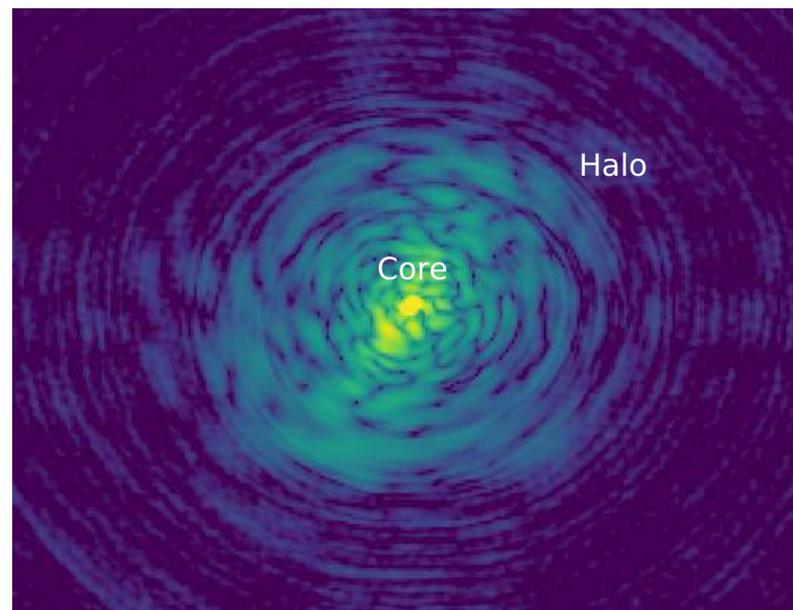


CDM: 256^3 , $z = 0.00$

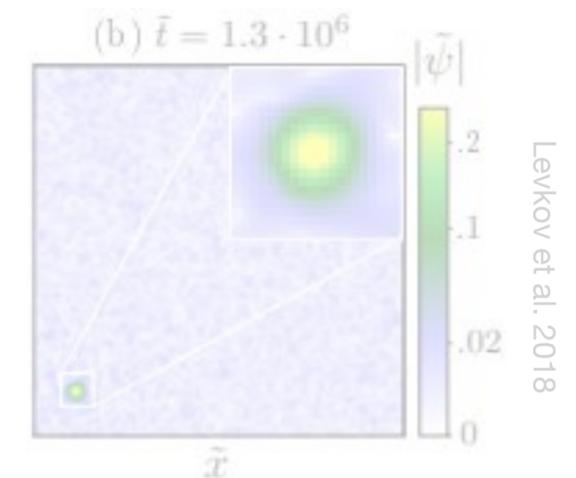


S. May et al. 2021

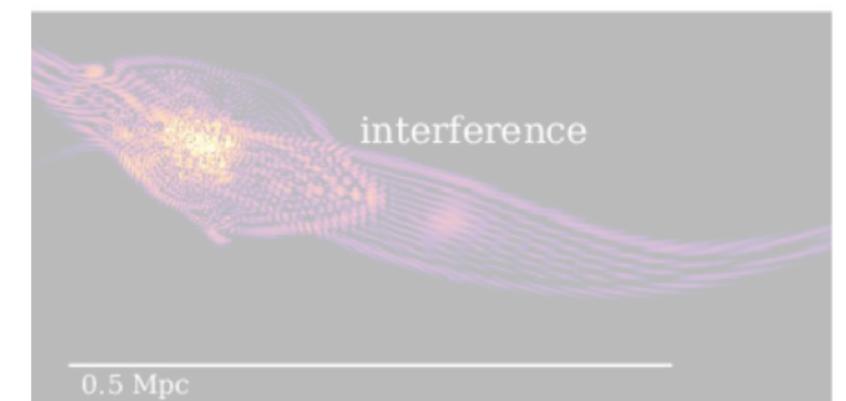
Formation of a solitonic core



Dynamical effects



Wave interference



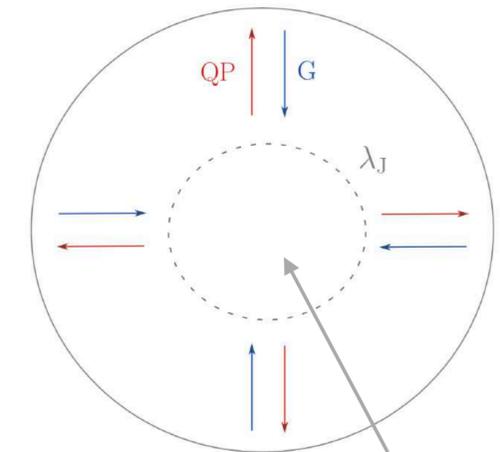
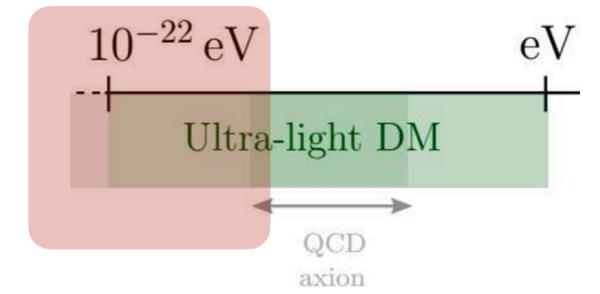
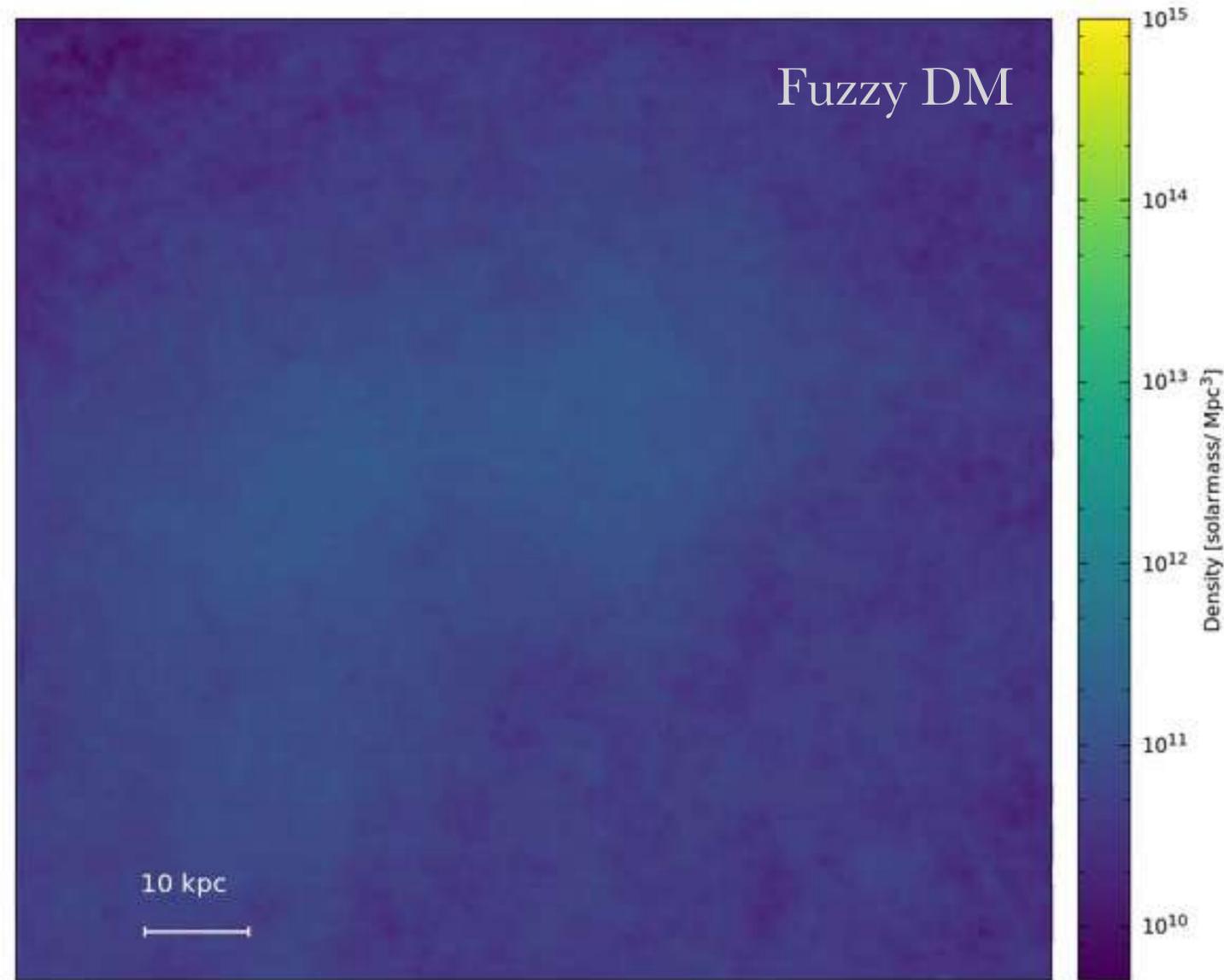
Mocz et al. 2017

Phenomenology

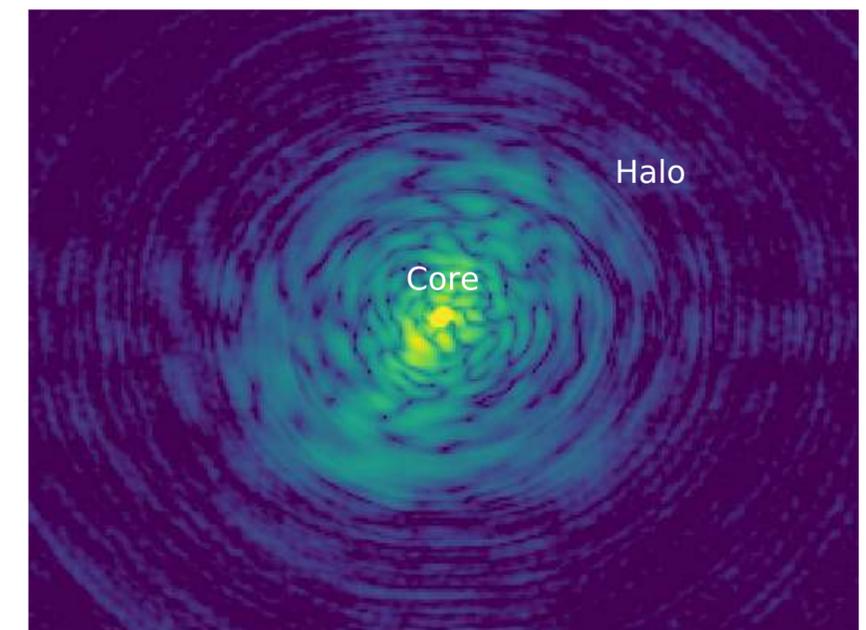
Formation of **cores**

$$m = 10^{-22} \text{ eV} \quad N = 512^3 \quad L = 300 \text{ kpc}$$

NON-LINEAR
evolution: need
simulations

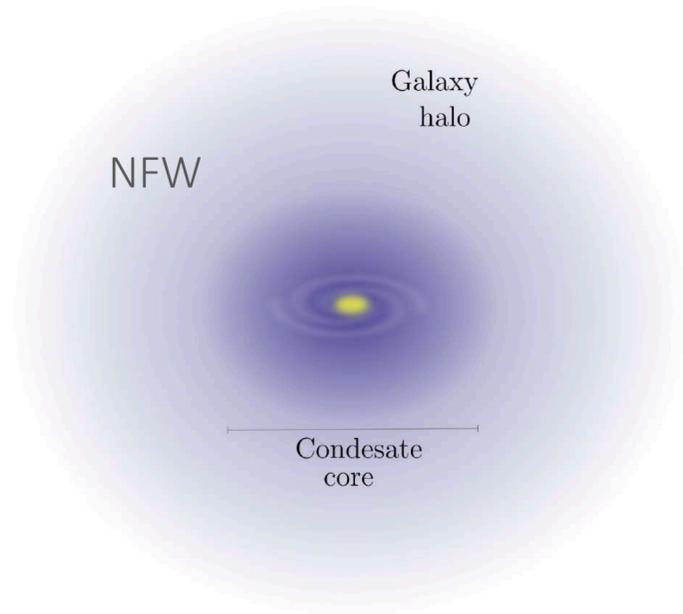


NO structure formation
Stable, oscillating solution

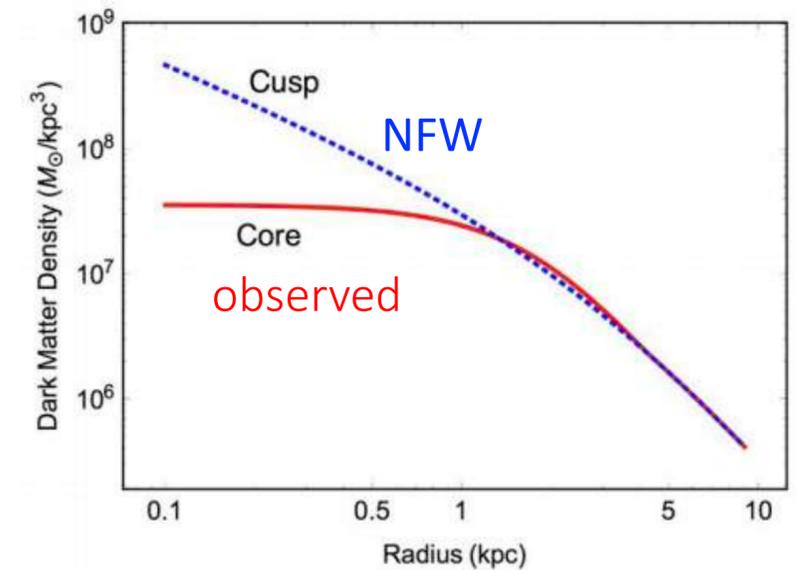
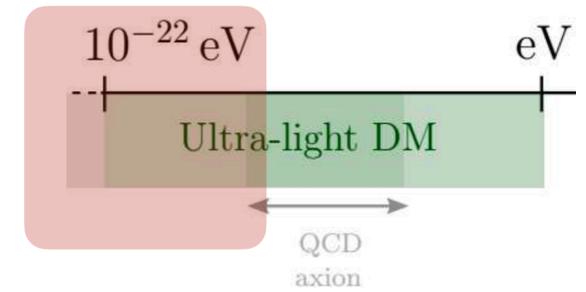


Phenomenology

Formation of **cores**



$$\rho(r) \simeq \begin{cases} \rho_c & \text{for } r \leq r_c \\ \rho_{\text{NFW}} & \text{for } r \geq r_c \end{cases}$$



FDM From simulations Schive et al. 2014, fitting function:

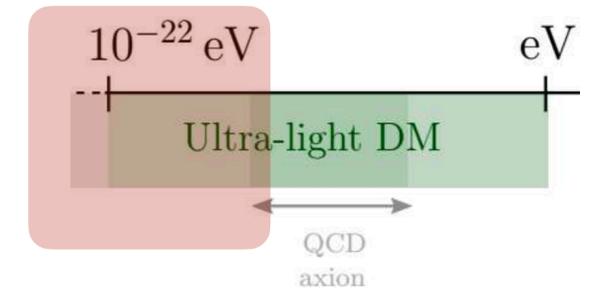
$$\rho_c \simeq \frac{1.9 \times 10^{-2}}{[1 + 0.091 (r/R_{1/2,c})^2]^8} \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-2} \left(\frac{r_c}{\text{kpc}} \right)^{-4} M_\odot \text{ pc}^{-3},$$

$$r_c \simeq 0.16 \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-1} \left(\frac{M}{10^{12} M_\odot} \right)^{-1/3} \text{ kpc}.$$

Updated in Chan, EF et al 2021

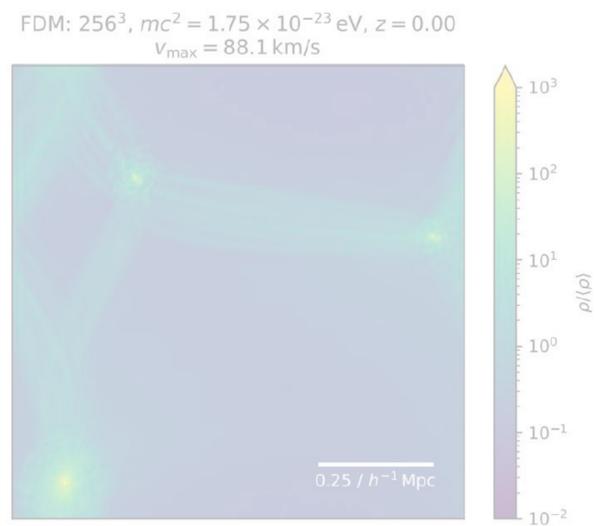
Relations used to compare with **observations**

Phenomenology

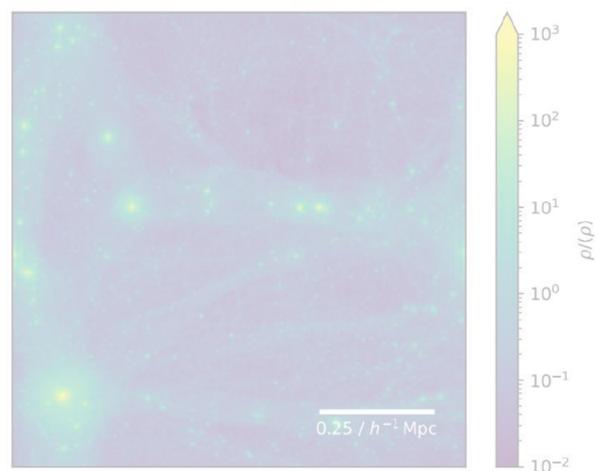


RICH PHENOMENOLOGY ON SMALL SCALES

Suppression of small structures

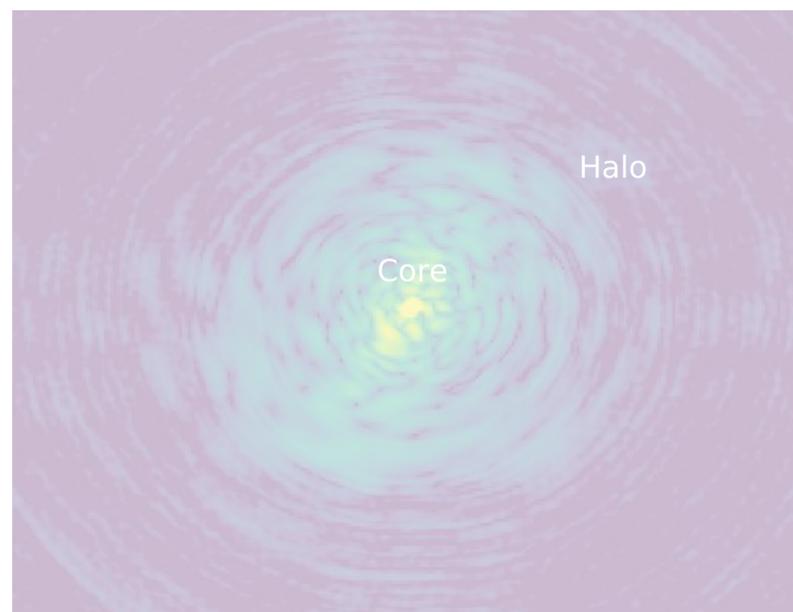


CDM: 256^3 , $z = 0.00$

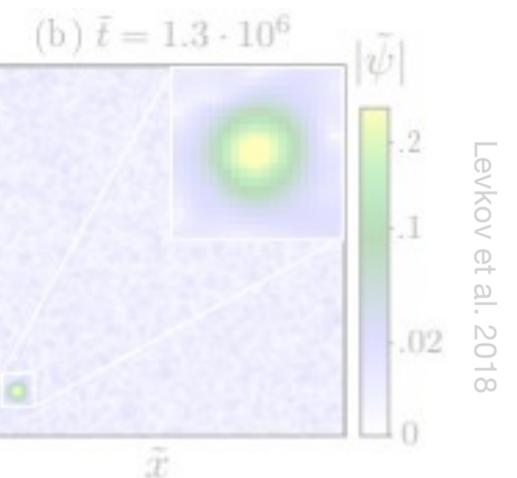


S. May et al. 2021

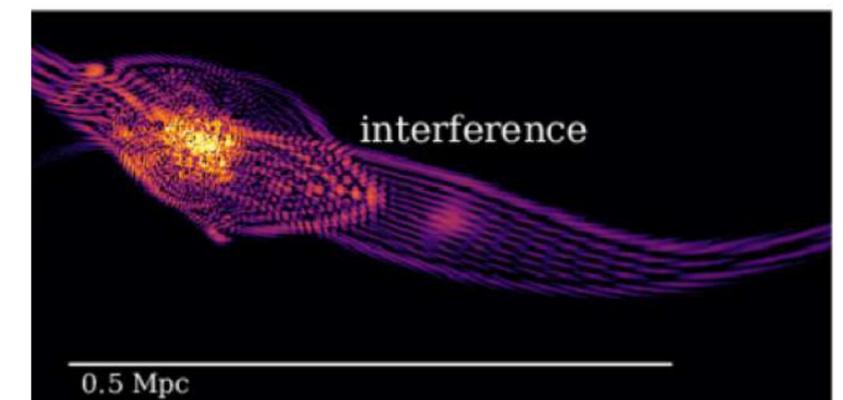
Formation of a solitonic core



Dynamical effects



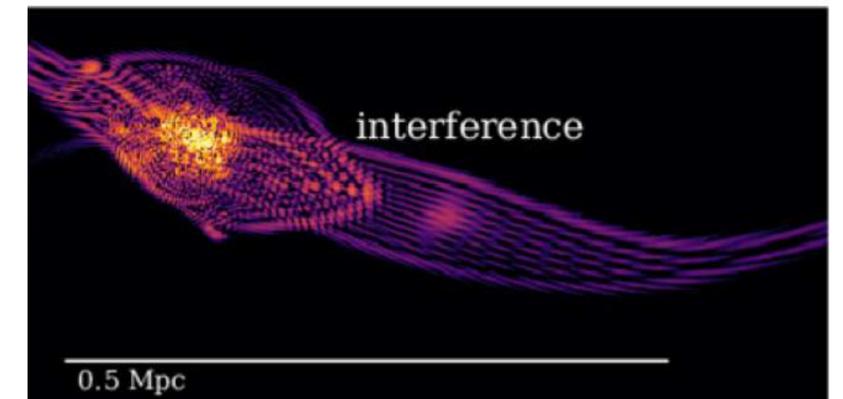
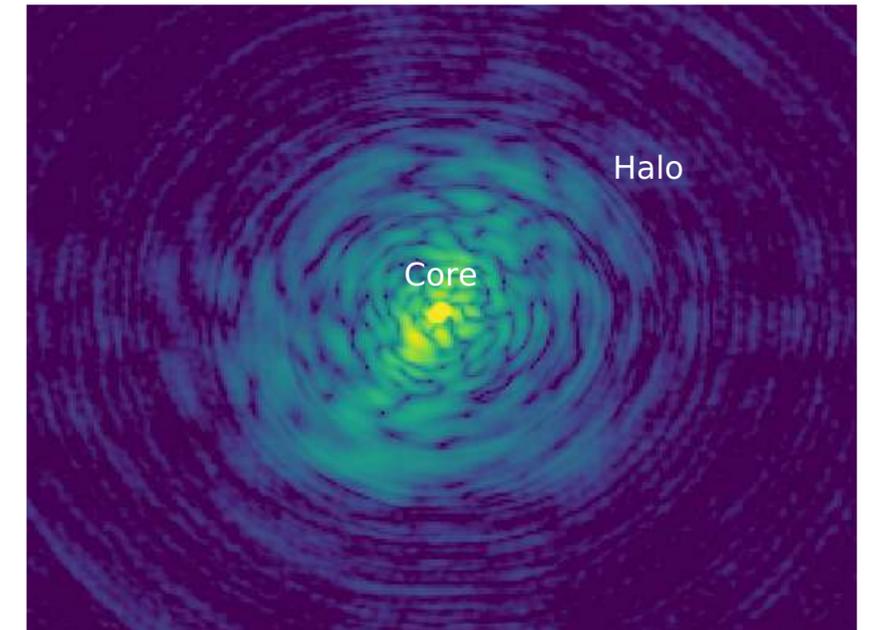
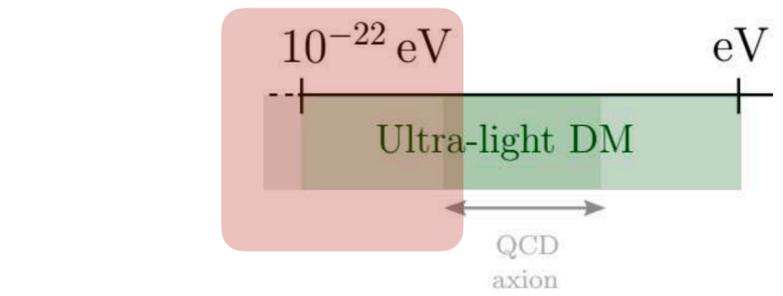
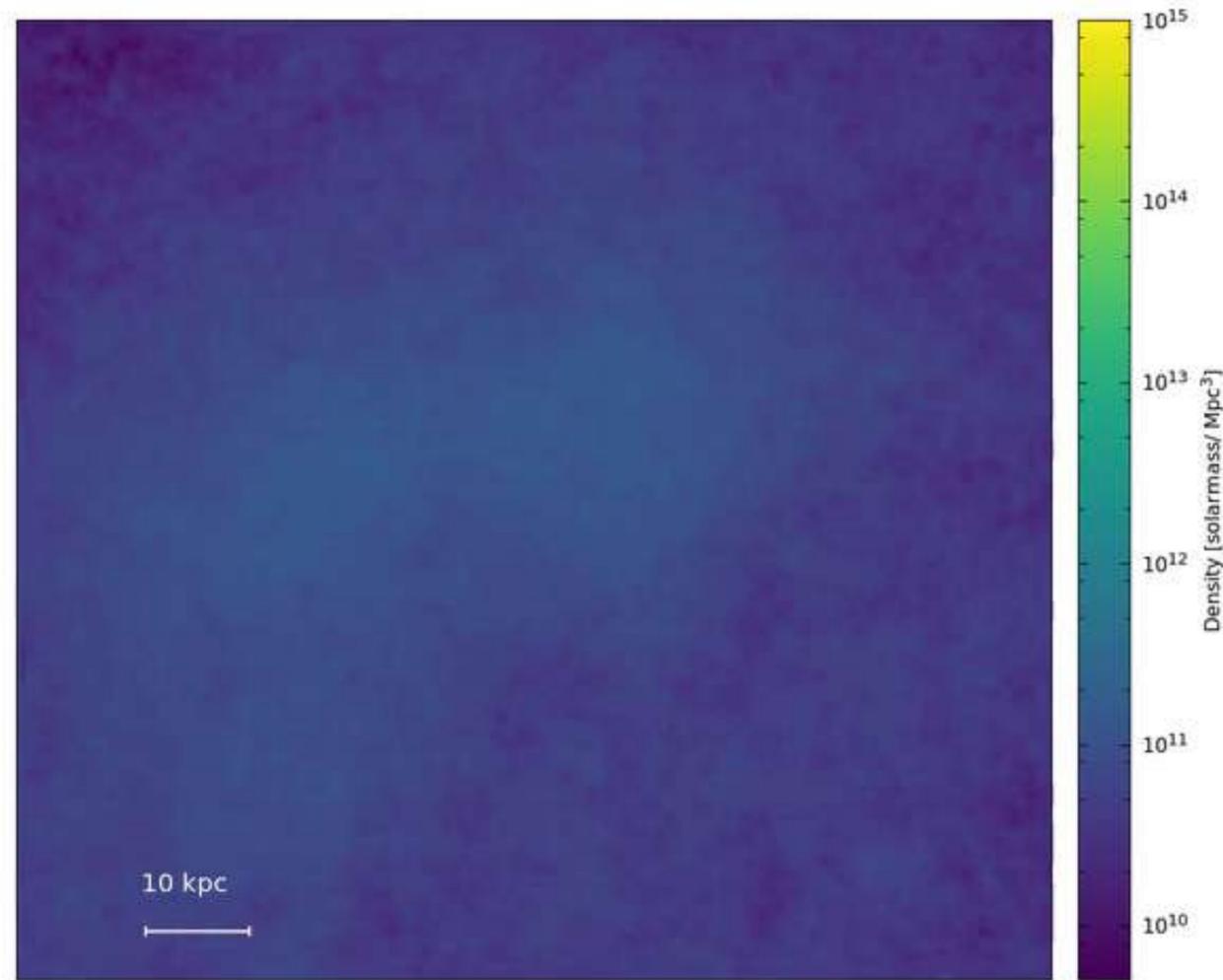
Wave interference



Mocz et al. 2017

Phenomenology

Wave interference: granules and vortices



Order one fluctuations in density \longrightarrow

Constructive interference: granules

Destructive interference

$\sim \lambda_{dB}$

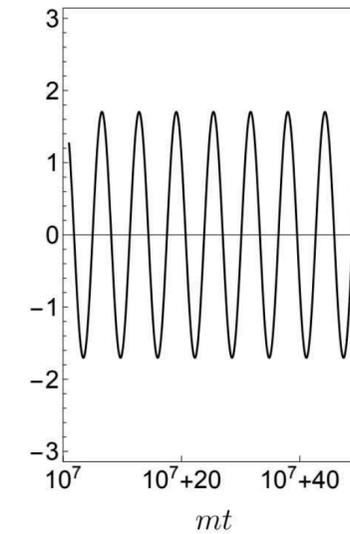
Mocz et al. 2017

Modeling a *granular halo*

Coherent wave oscillation of ULDM

$$\phi(t, \vec{x}) = m^{-1} \sqrt{2\rho(t, \vec{x})} \cos[mt + \theta]$$

Fixed Constant
freq. phase



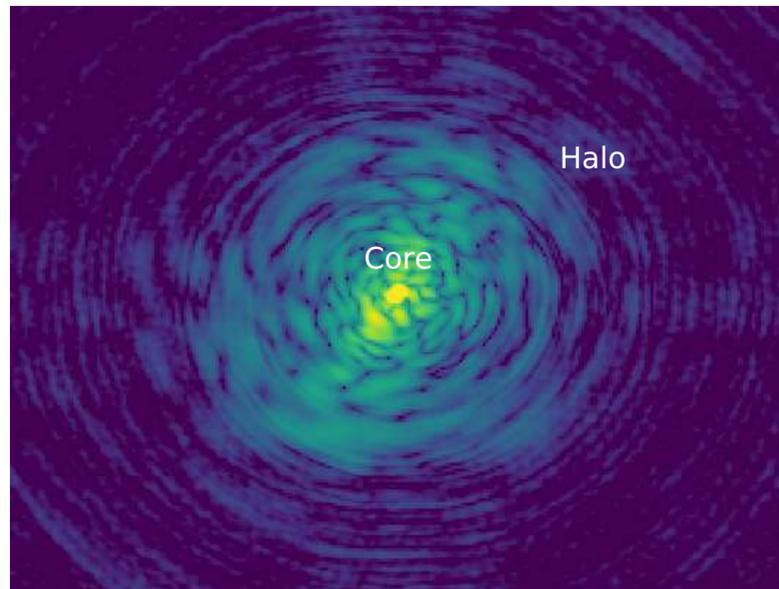
Modeling a *granular halo*

Coherent wave oscillation of ULDM

$$\phi(t, \vec{x}) = m^{-1} \sqrt{2\rho(t, \vec{x})} \cos[mt + \theta]$$

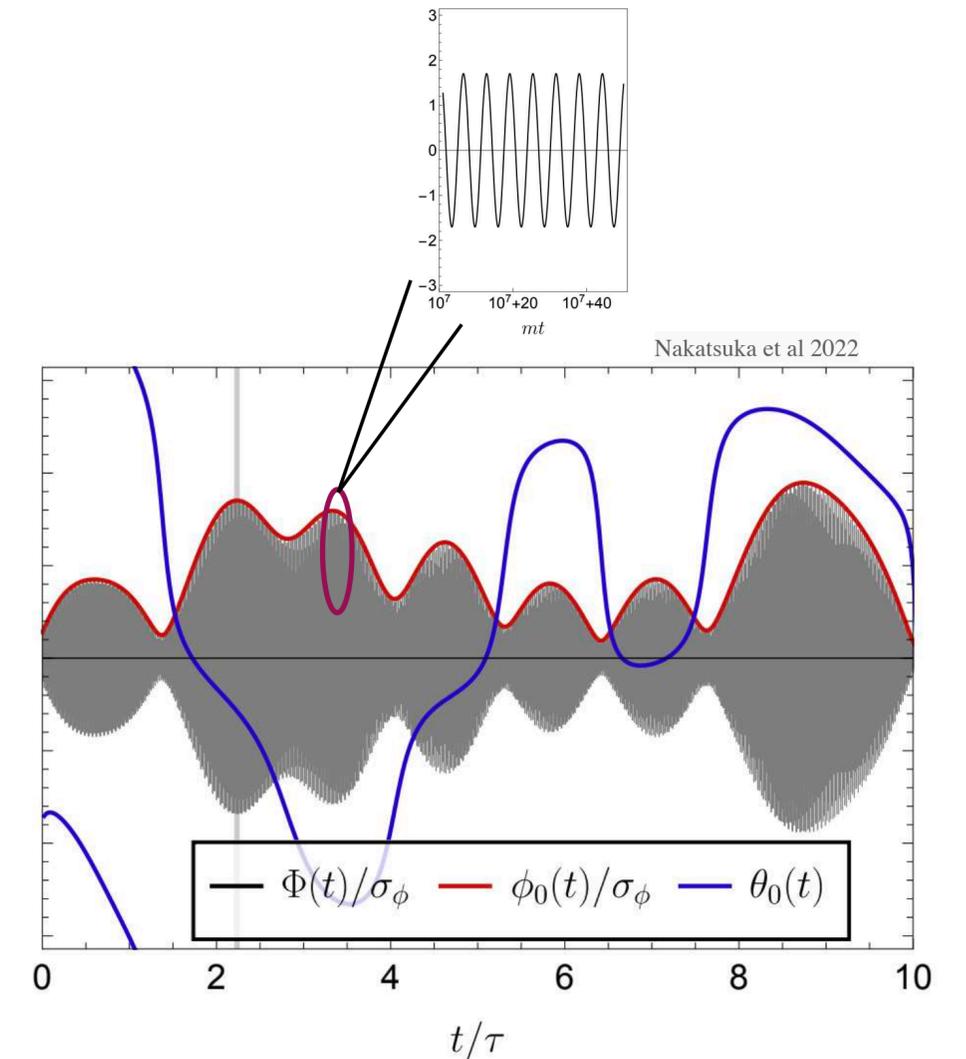
Fixed
freq. Constant
phase

But, the halo in these models is like this:



Superposition of plane waves

$$\left| \begin{matrix} \text{wavy line} \\ \text{wavy line} \end{matrix} \right. = \left| \text{single wavy line} \right|$$



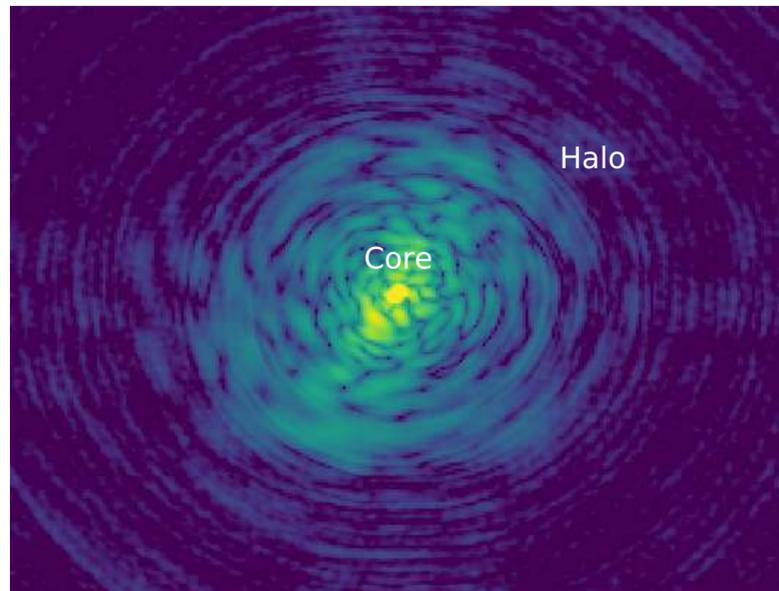
Modeling a *granular halo*

Coherent wave oscillation of ULDM

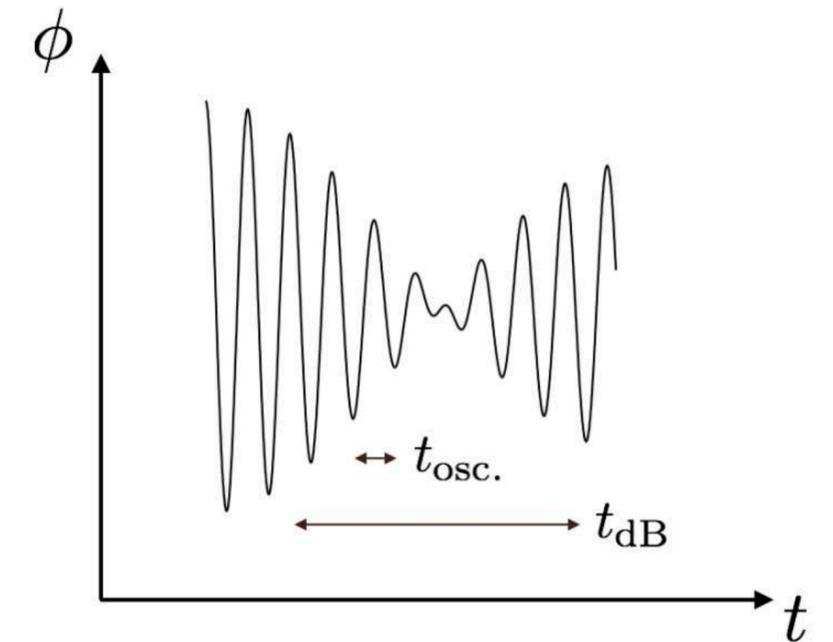
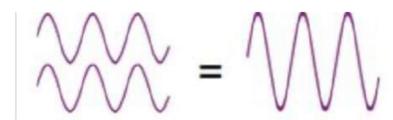
$$\phi(t, \vec{x}) = m^{-1} \sqrt{2\rho(t, \vec{x})} \cos[mt + \theta]$$

Fixed
freq. Constant
phase

But, the halo in these models is like this:



Superposition of plane waves



$$t_{\text{osc.}} = 2\pi/m$$

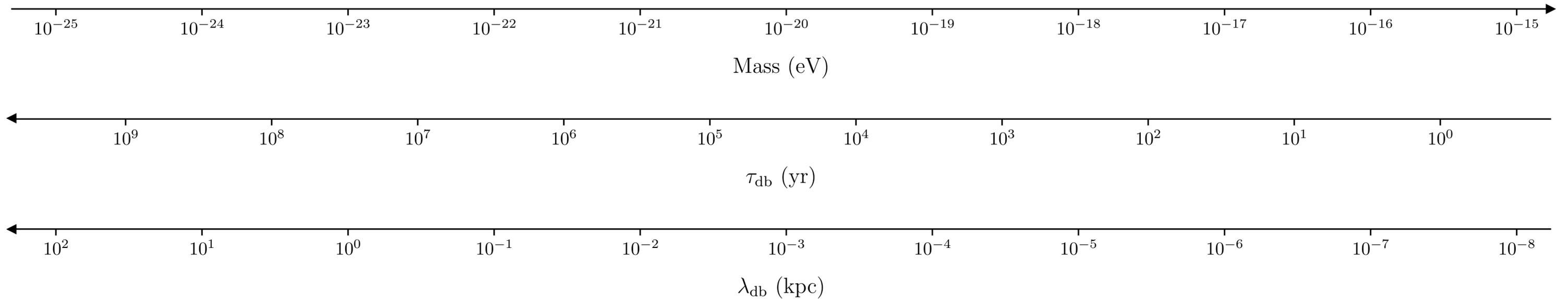
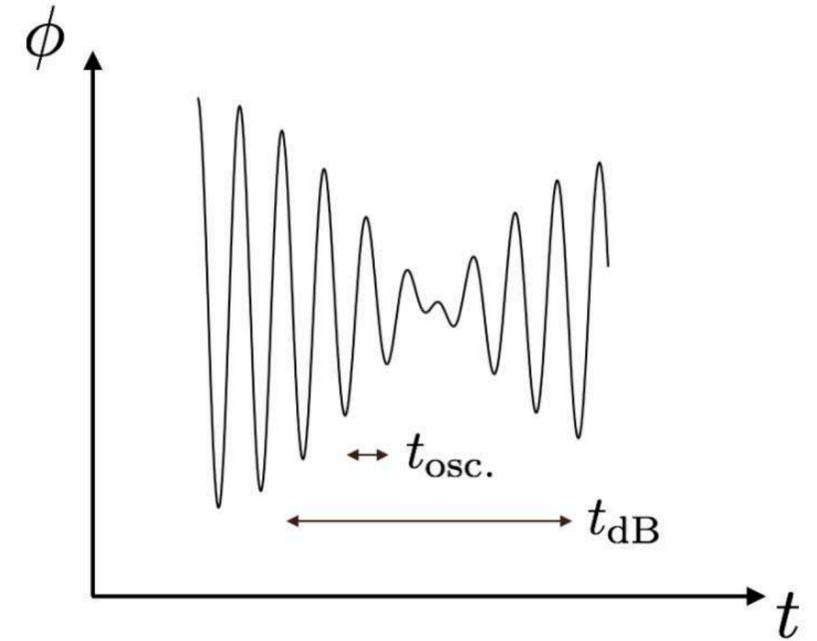
$$t_{\text{dB}} = 2\pi/(mv^2)$$

$$= 1.9 \times 10^6 \text{ yr} \left(\frac{10^{-22} \text{ eV}}{m} \right) \left(\frac{250 \text{ km/s}}{v} \right)^2$$

Modeling a *granular halo*

$$t_{\text{osc.}} = 2\pi/m$$

$$t_{\text{dB}} = 2\pi/(mv^2) \\ = 1.9 \times 10^6 \text{ yr} \left(\frac{10^{-22} \text{ eV}}{m} \right) \left(\frac{250 \text{ km/s}}{v} \right)^2$$



Modeling a *granular halo*

Full SP simulations can describe perfectly this interference pattern (while fluid ones *cannot* describe it)

OR

We can adopt simpler descriptions of the galactic halo to describe this effect.

1) A simple model of a galactic halo, consider a **superposition of plane waves**:

Random phase halo model

$$\psi(t, \vec{x}) = \sum_{\vec{k}} A_{\vec{k}} e^{iB_{\vec{k}}} e^{i\vec{k} \cdot \vec{x} - i\omega_k t}$$

Randomly distributed

Wave interference produces de-Broglie-scale, order unity density fluctuations which vary on time scale of t_{dB}

This collection of plane waves can also be represented like this:

$$\phi(t, \vec{x}) = A(\vec{x}) \cos(mt + \alpha(\vec{x}))$$

describes the interference patterns

2) Another model would **superimpose eigenstates** of a desired gravitational potential (Lin et al. 2018, Li et al. 2021)

Perform an eigenmode decomposition of the halo wavefunction, where the eigenmodes are for a fixed gravitational potential
 → ω_k is the energy of each eigenmode (labeled abstractly by k), with $e^{i\vec{k} \cdot \vec{x}}$ replaced by the corresponding eigenfunction.

$$\psi(r, \theta, \phi, t) = \sum_{n,l,m} A_{nlm} F_{nlm}(r, \theta, \phi) e^{-iE_{nl}t/\hbar}$$

Energy eigenvalue

$$F_{nlm}(r, \theta, \phi) = R_{nl}(r) Y_l^m(\theta, \phi)$$

Radial eigenfunction

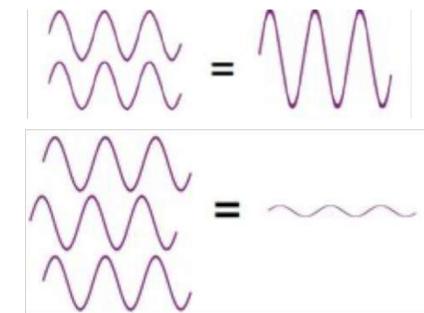
energy eigenmodes of the gravitational potential of the virialized halo

Vector, higher spin or multicomponent *FDM*

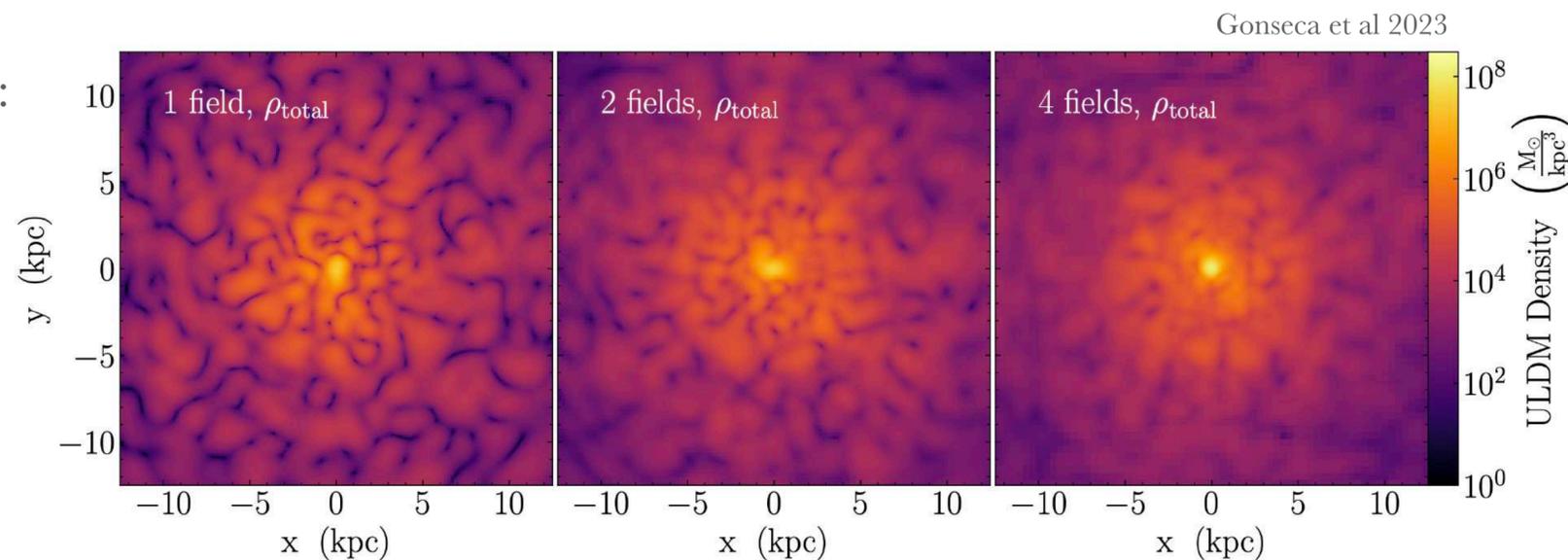
ULDM or ULA are a coherent wave - same frequency and constant phase difference

Multiple coherent waves

Interference patterns



For ULDM:



Multiple FDM or VFDM (or higher spin s FDM) *attenuates* the granule amplitude by

$$\frac{[\delta\rho/\rho]_{\text{nfdm},s}}{[\delta\rho/\rho]_{\text{fdm}}} \propto \frac{1}{\sqrt{(2s+1)}} = \frac{1}{\sqrt{N}}$$

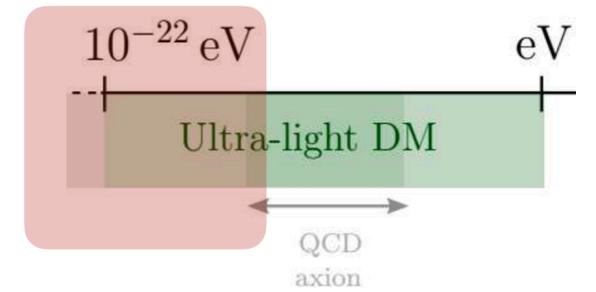
(Amin et al 2022)

Vector (and higher-spin) FDM Amin et al 2022

(Vector FDM = 3 x same mass FDM (spin 0))

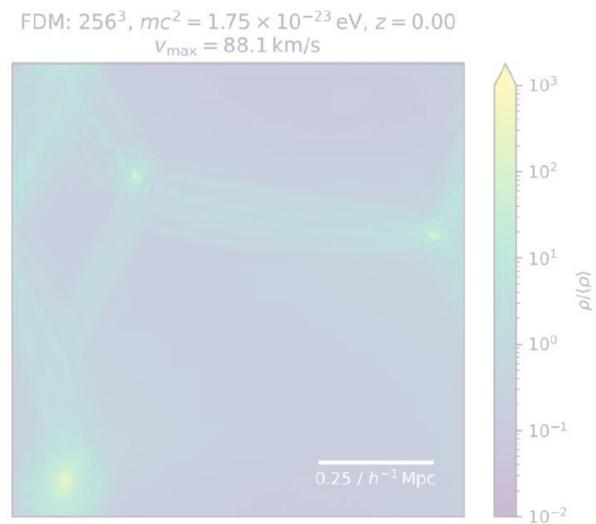
Multicomponent FDM Gonseca et al 2023

Phenomenology

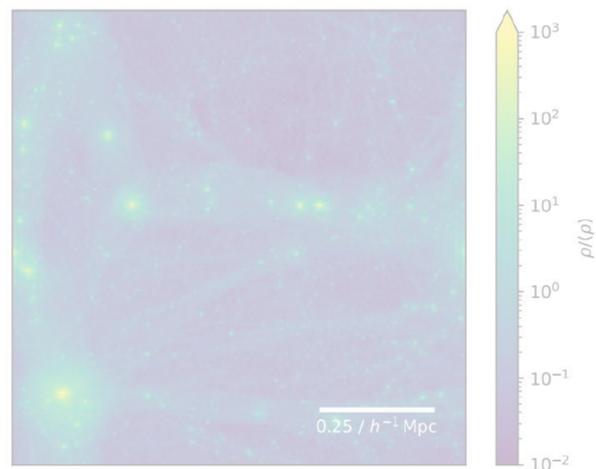


RICH PHENOMENOLOGY ON SMALL SCALES

Suppression of small structures

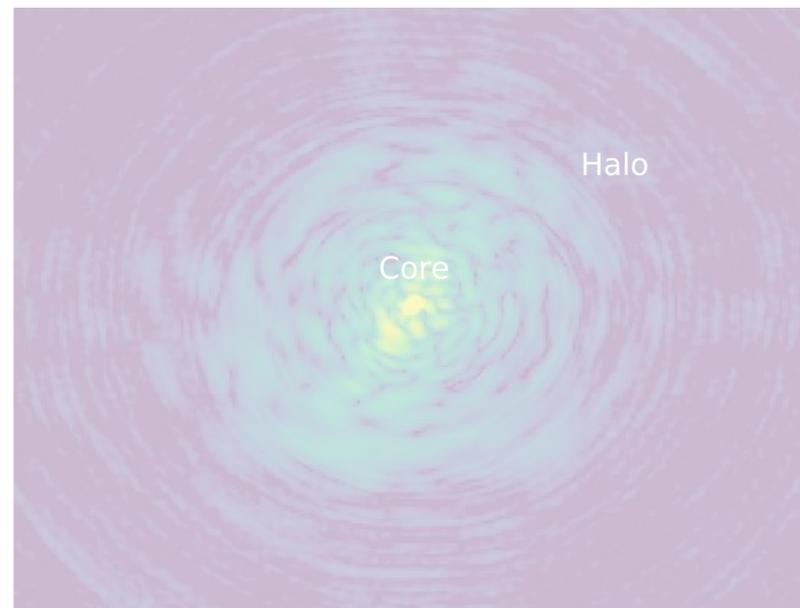


CDM: 256^3 , $z = 0.00$

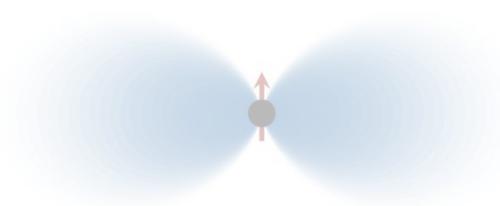


S. May et al. 2021

Formation of a solitonic core

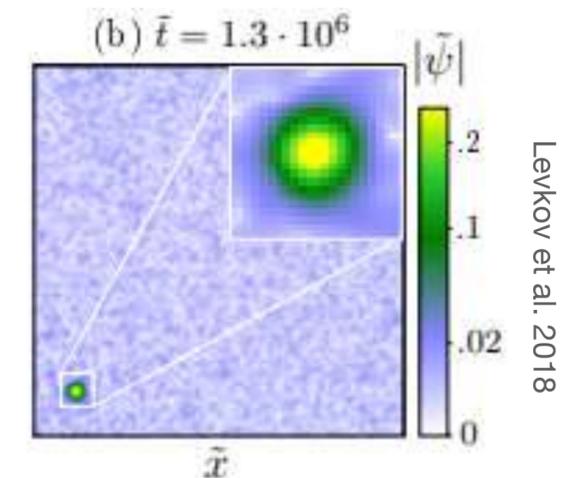


Axion clouds

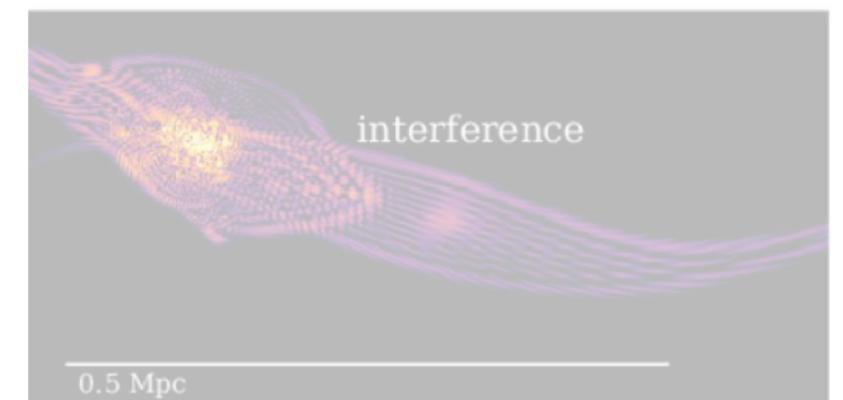


Baumann et al. 2019

Dynamical effects



Wave interference

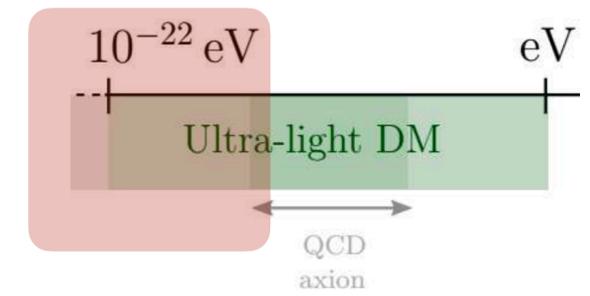


Mocz et al. 2017

Phenomenology

Dynamical effects

Relaxation, oscillation, friction, and heating

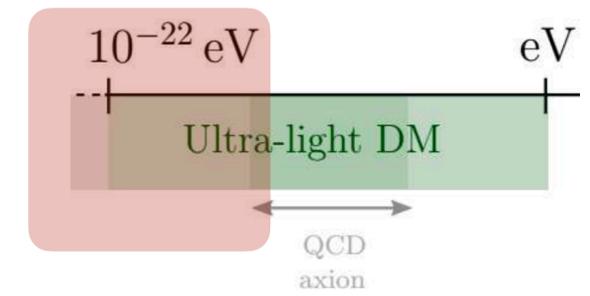


Phenomenology

Dynamical effects

Relaxation, oscillation, friction, and heating

Formation of a BEC / superfluid



Phenomenology

Dynamical effects

Relaxation, oscillation, friction, and heating

Formation of a BEC / superfluid

- **Thermalization** (and **condensation**) *seem* to happen inside the galaxy!
 Formation of a **soliton** (ground state) or **Bose star** in the interior of galaxies

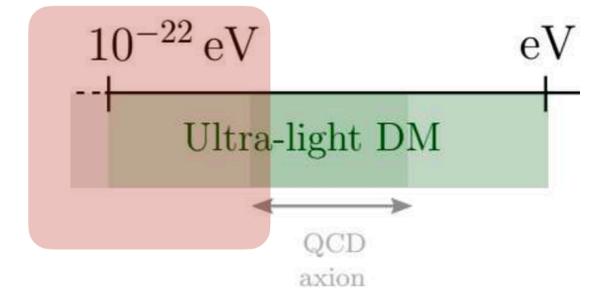
- Formation of a condensate and a core occur from **gravitational interaction**.

Condensation/relaxation time: $\tau_{\text{gr}} \gg \tau_{\text{int}}$

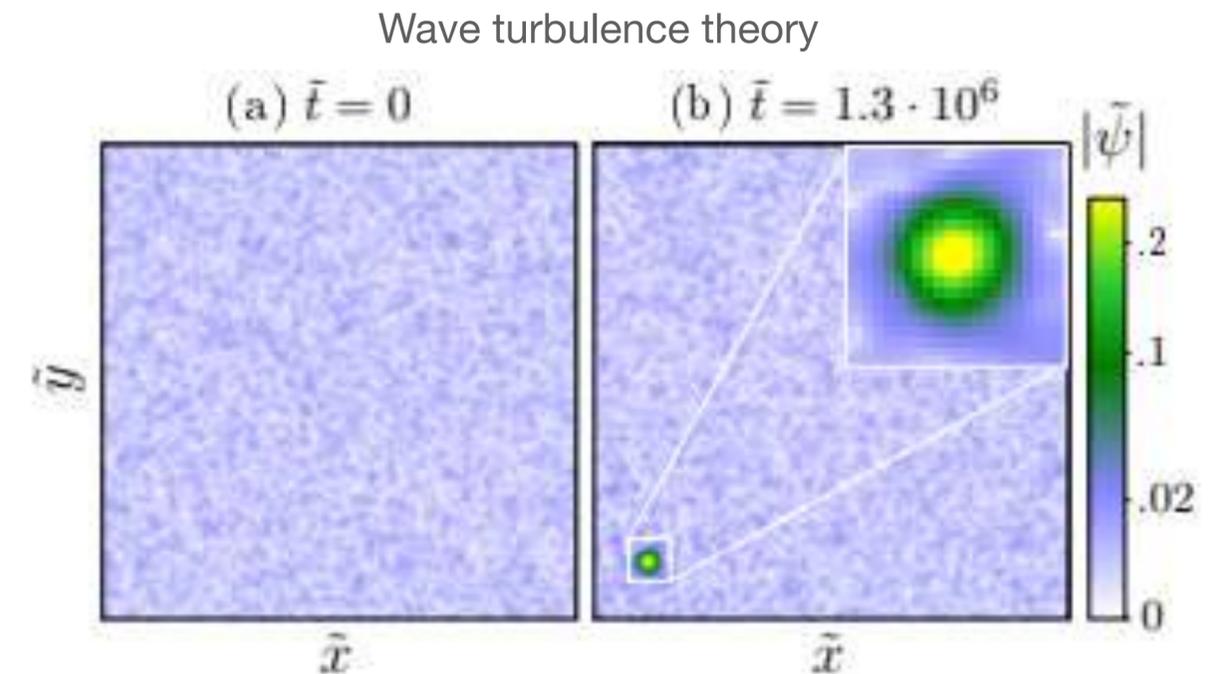
$$\tau_{\text{gr}} \sim 10^6 \text{ yr} \left(\frac{m}{10^{-22} \text{ eV}} \right)^3 \left(\frac{v}{30 \text{ km/s}} \right)^6 \left(\frac{\rho}{0.1 M_{\odot}/\text{pc}^3} \right)^{-2}$$

$$\tau_{\text{int}} = \frac{1}{\sqrt{8}|g|n}$$

Smaller than the age of the universe!



A. Guth M. Hertzberg, C. Prescod-Weinstein (2014)



Levkov et al. 2018, Kirpatrick et al. 2020

Phenomenology

Dynamical effects

Relaxation, oscillation, friction, and heating

Formation of a BEC / superfluid

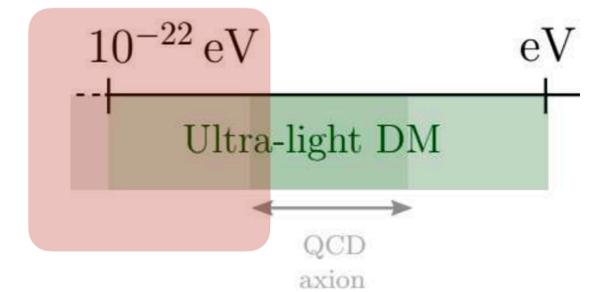
Open question!

- Need theoretical work to describe *analytically* the formation of these solitons

- Evolution all classical?

- *Allali and Hertzberg 2020*
- *Dvali and Zell 2018*
- *A. Eberhardt et al. 2022, 2023*
- *M. Yamaguchi et al.*

Re-thermalization or not: (Sikivie and Yang 2009; Erken et al. 2012; Marsh 2016; Guth et al. 2015; Castellanos et al. 2014; Davidson and Elmer 2013; Davidson 2015)



(Work in progress)

In collaboration with Yuta Sekino and Ryo Namba

For an overdensity whose size is the typical DM de Broglie wavelength, we find that the decoherence rate in the halo is higher than the present Hubble rate for DM masses $m \lesssim 5 \times 10^{-7}$ eV and in earth based experiments it is higher than the classical field coherence rate for $m \lesssim 10^{-6}$ eV. When spreading of the states occurs, the rates can become much faster, as we quantify. Also, we establish that DM BECs decohere very rapidly and so are very well described by classical field theory.

Phenomenology

Dynamical effects

Relaxation, oscillation, friction, and heating

Formation of a BEC / superfluid

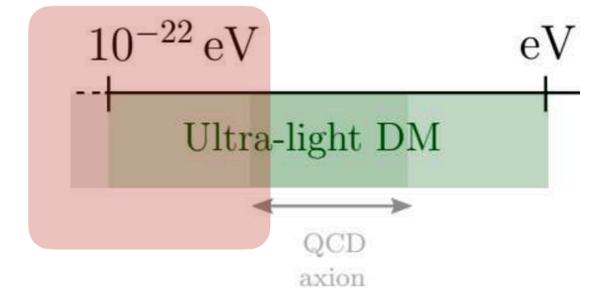
Open question!

- Need theoretical work to describe *analytically* the formation of these solitons

- Evolution all classical?

- Allali and Hertzberg 2020
- Dvali and Zell 2018
- A. Eberhardt et al. 2022, 2023
- M. Yamaguchi et al.

Re-thermalization or not: (Sikivie and Yang 2009; Erken et al. 2012; Marsh 2016; Guth et al. 2015; Castellanos et al. 2014; Davidson and Elmer 2013; Davidson 2015)



(Work in progress)

In collaboration with Yuta Sekino and Ryo Namba

"For an overdensity whose size is the typical DM de Broglie wavelength, we find that the decoherence rate in the halo is higher than the present Hubble rate for DM masses $m \lesssim 5 \times 10^{-7}$ eV and in Earth based experiments it is higher than the classical field coherence rate for $m \lesssim 10^{-6}$ eV. When spreading of the states occurs, the rates can become much faster, as we quantify. Also, we establish that DM BECs decohere very rapidly and so are very well described by classical field theory."

Here: gravitational interactions only; with baryons, much faster!

Phenomenology

Vortices

Vortices are sites where the fluid velocity has a non-vanishing curl

Two ways:

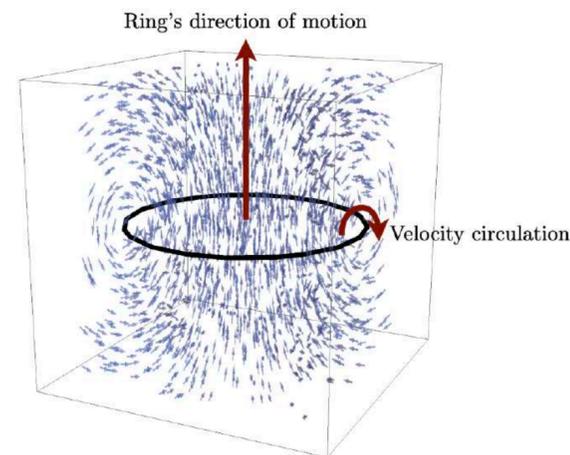
- regions where the density vanishes
- transfer of angular momentum (superfluids only)

Fuzzy DM

Interference of waves leads to **vortices** - where there is **destructive interference**

General defect in 3D

$$c = \frac{1}{m} \oint_{\partial A} d\theta = \frac{2\pi n}{m}$$



Hui et al 2020

$$(\psi \equiv \sqrt{\rho/m} e^{i\theta} \text{ and } \mathbf{v} \equiv \nabla\theta/m)$$

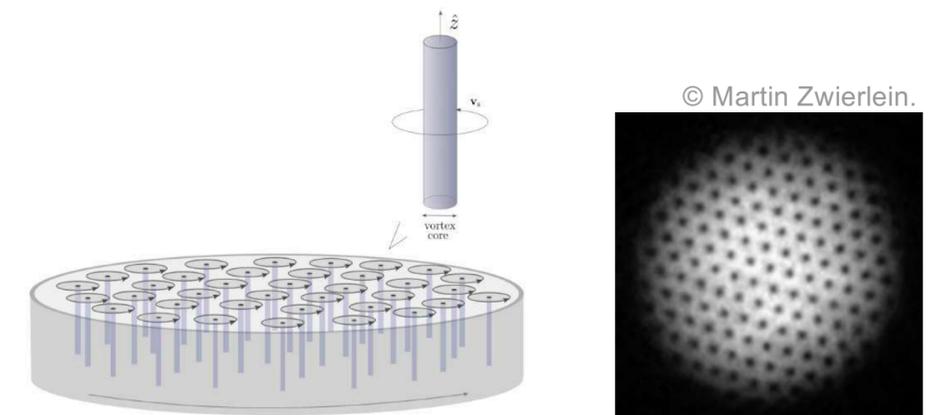
Vel. field is a gradient flow \rightarrow irrotational fluid, no vorticity



Quanta magazine

Self-interacting Fuzzy DM

Superfluid cannot rotate uniformly. If the superfluid rotates faster than the critical vel., network of vortices are formed.



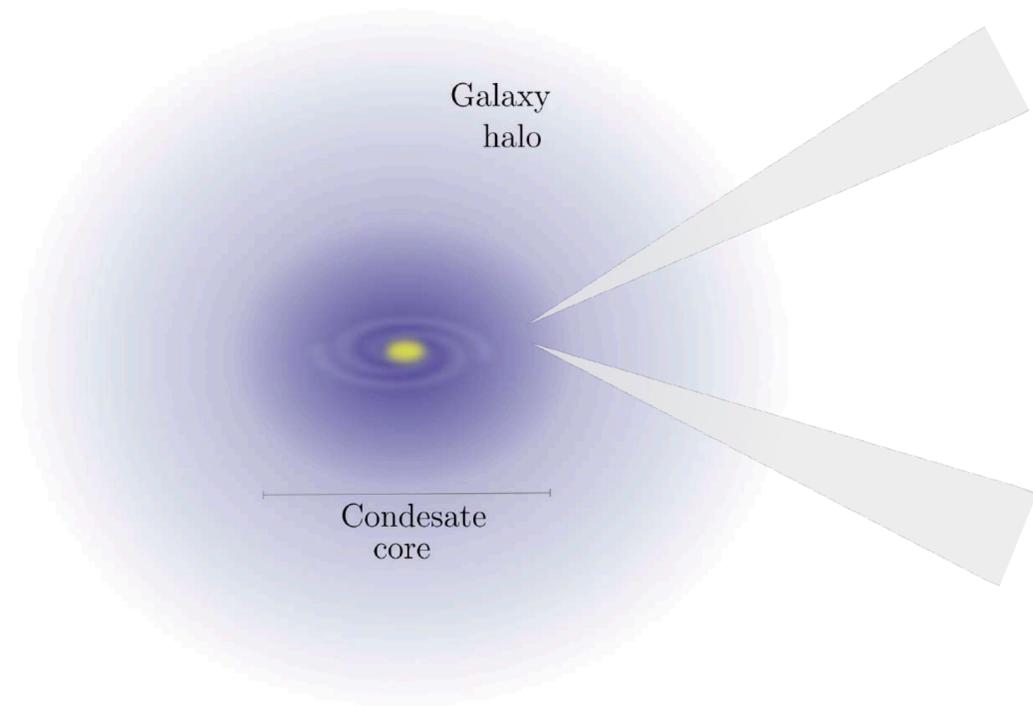
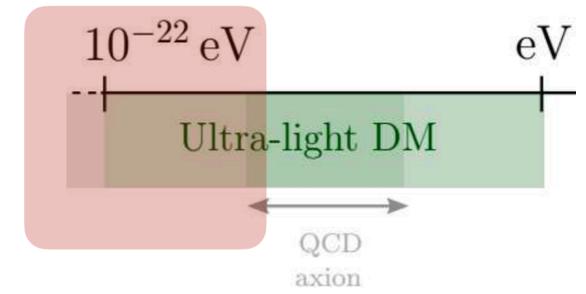
© Martin Zwierlein.

EF, 2020

Phenomenology

Dynamical effects

Relaxation, oscillation, friction, and heating



Heating

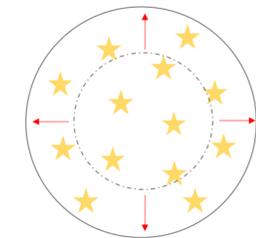
FDM granule



m_{eff}



System (star)
gains energy



Friction

FDM granule



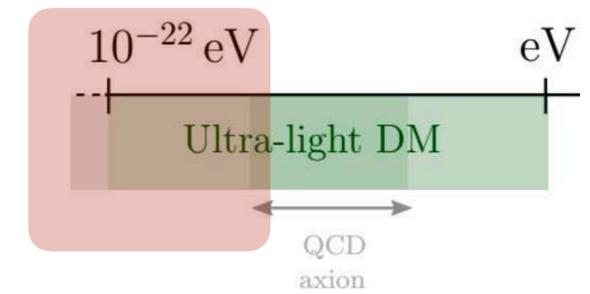
m_{eff}



Globular cluster

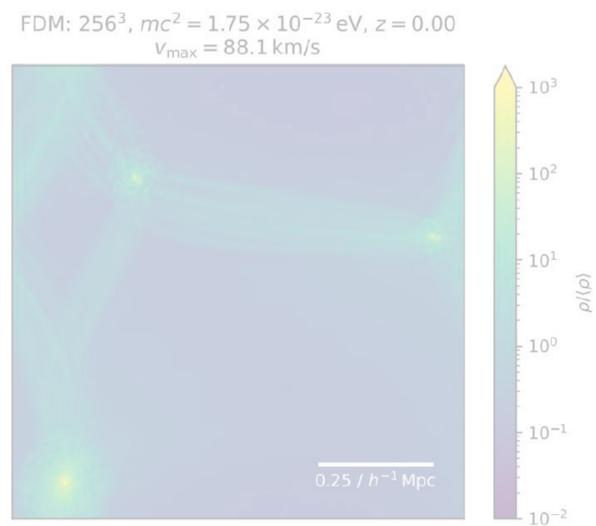
System (GC or BH)
loses energy

Phenomenology

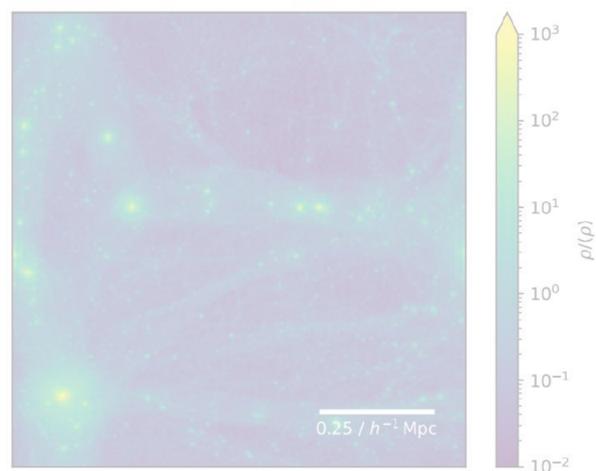


RICH PHENOMENOLOGY ON SMALL SCALES

Suppression of small structures

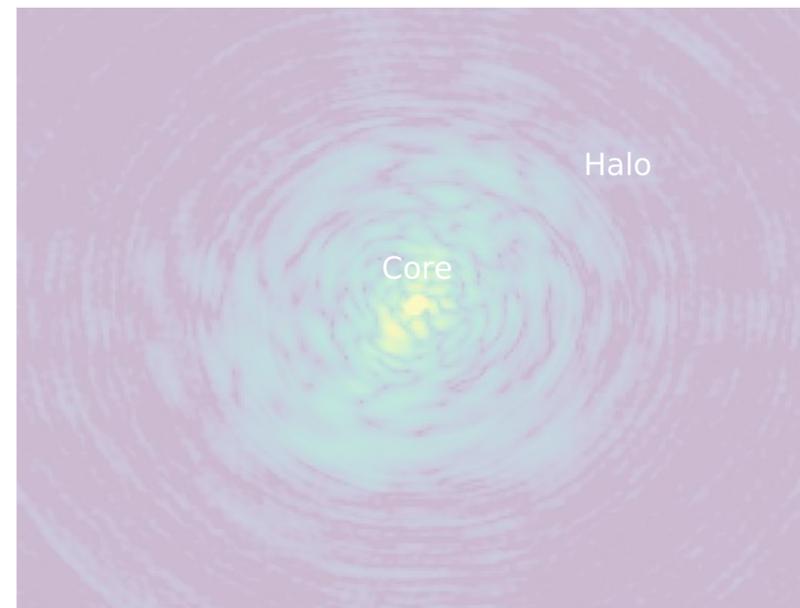


CDM: 256^3 , $z = 0.00$

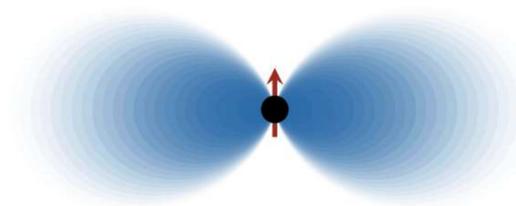


S. May et al. 2021

Formation of a solitonic core

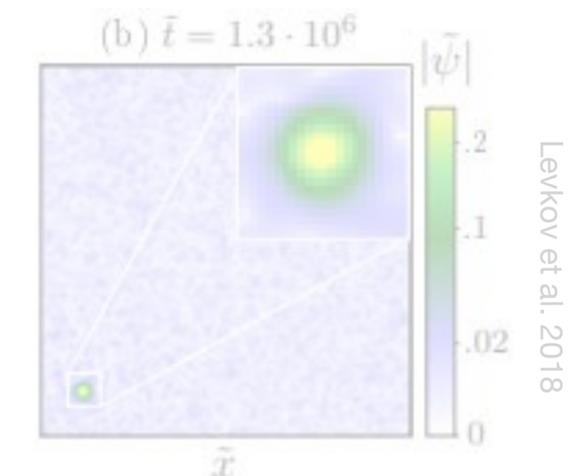


Axion clouds

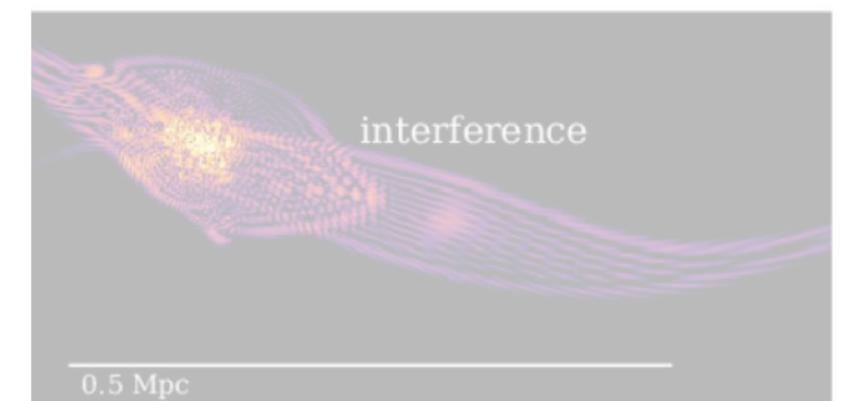


Baumann et al. 2019

Dynamical effects



Wave interference



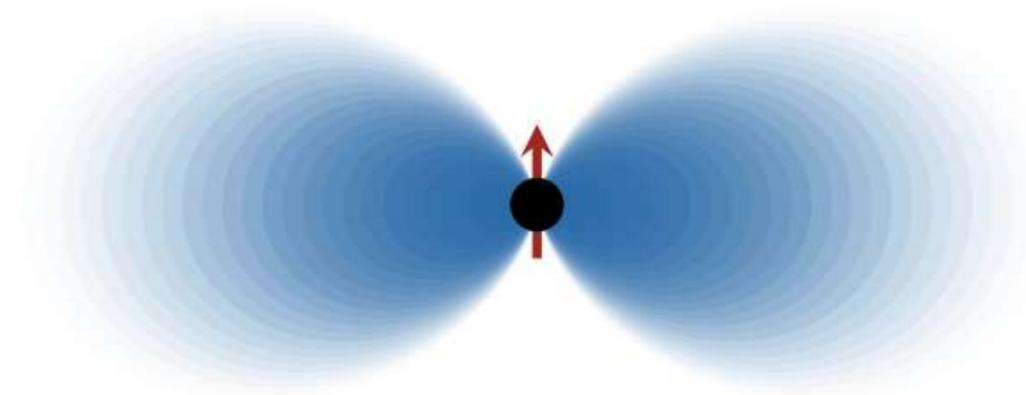
Mocz et al. 2017

Phenomenology

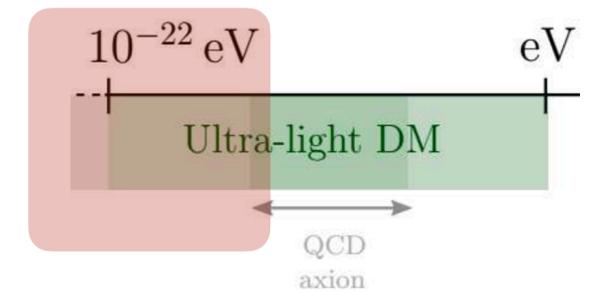
Axion clouds

- Superradiance

Cloud created around rotating BHs



Baumann et al. 2019



- External potential

$$\text{Self-gravity} \left\{ \begin{array}{l} i\dot{\psi} = \left(-\frac{1}{2m} \nabla^2 + \frac{g}{8m^2} |\psi|^2 - m\Phi \right) \psi \\ \nabla^2 \Phi = 4\pi G (m|\psi|^2 - \bar{\rho}) \end{array} \right.$$

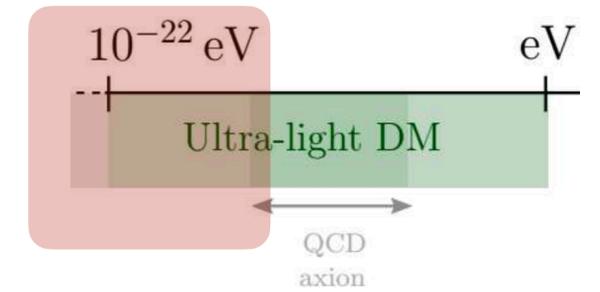
+

External potential

Ex.: BHs, neutron stars, stars, planets, ...

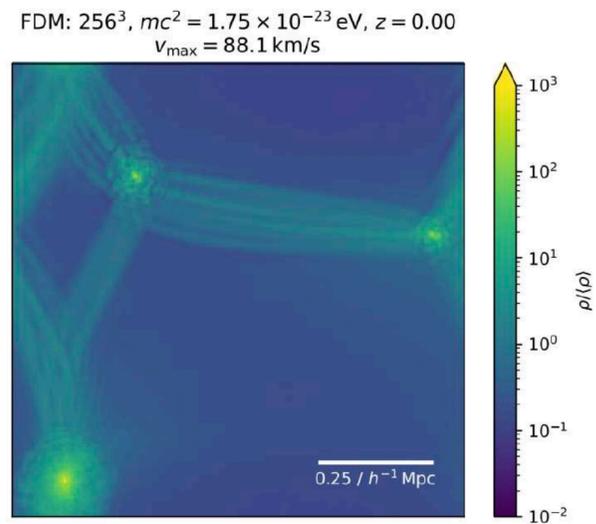
Phenomenology

RICH PHENOMENOLOGY ON SMALL SCALES

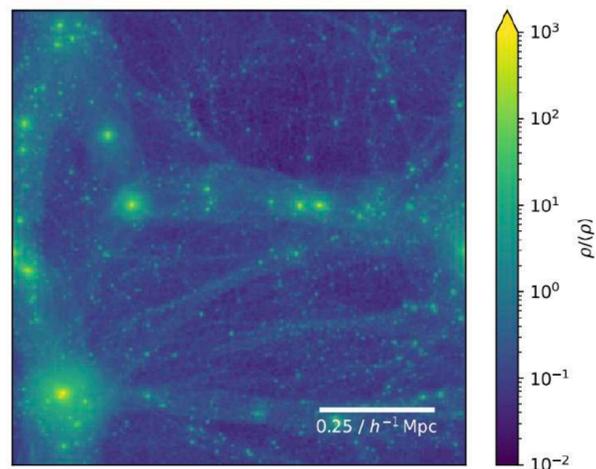


* Focus only in gravitational signatures

Suppression of small structures

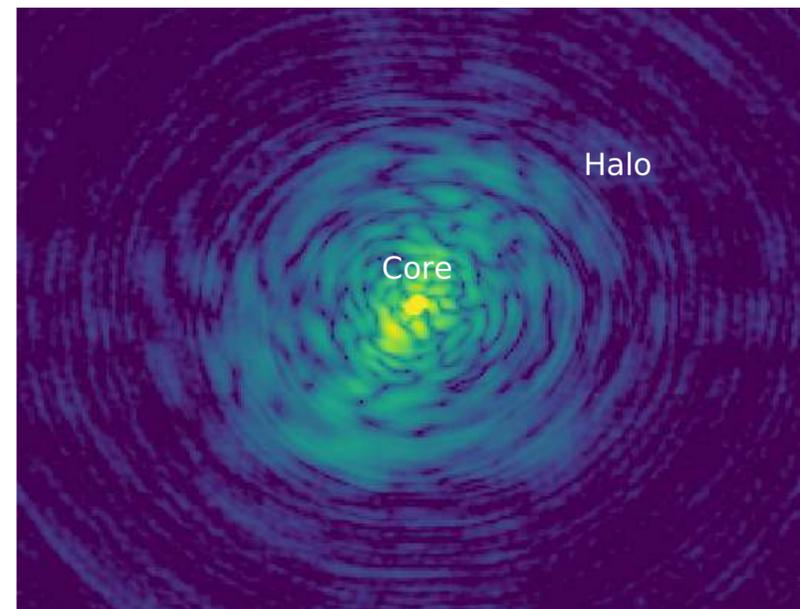


CDM: 256^3 , $z = 0.00$

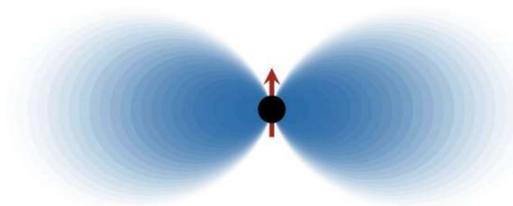


S. May et al. 2021

Formation of a solitonic core

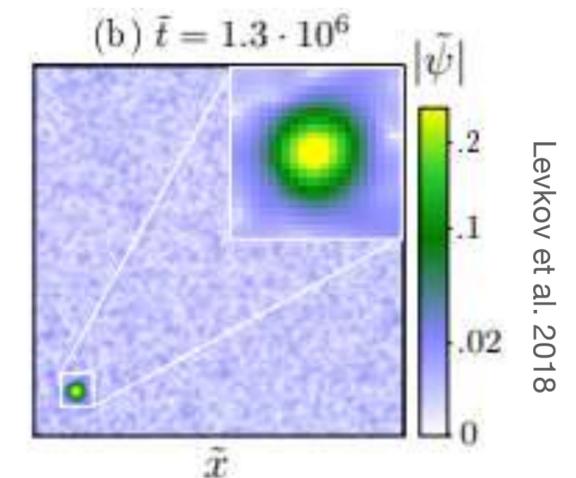


Axion clouds

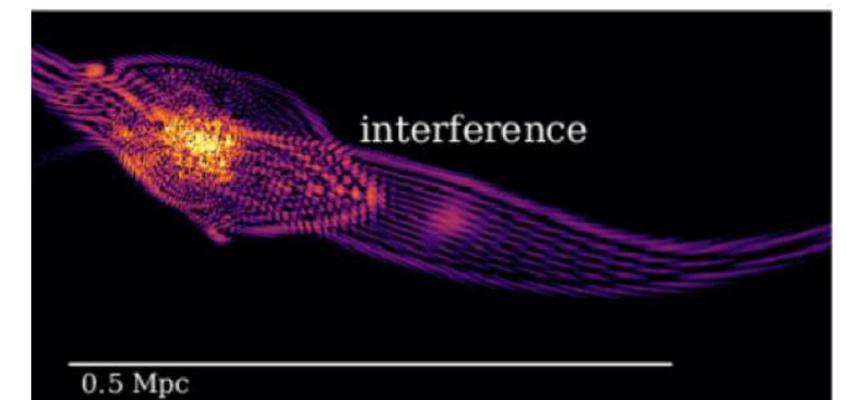


Baumann et al. 2019

Dynamical effects

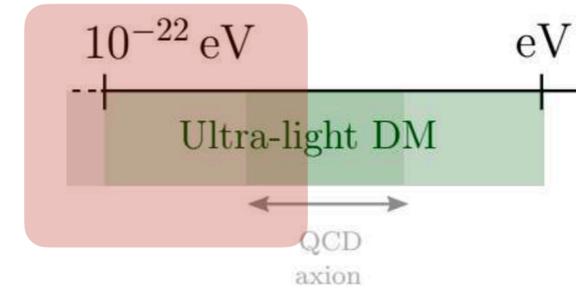


Wave interference



Mocz et al. 2017

Observational implications and constraints

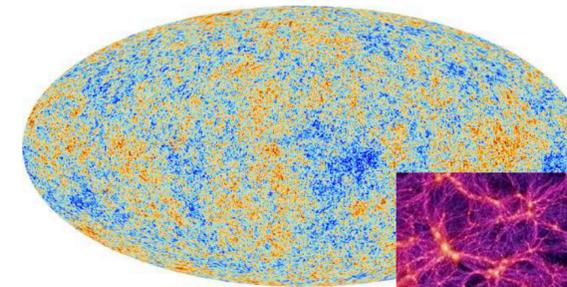


Galaxies

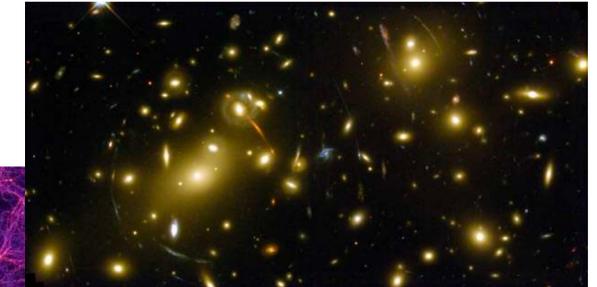


NASA and ESA

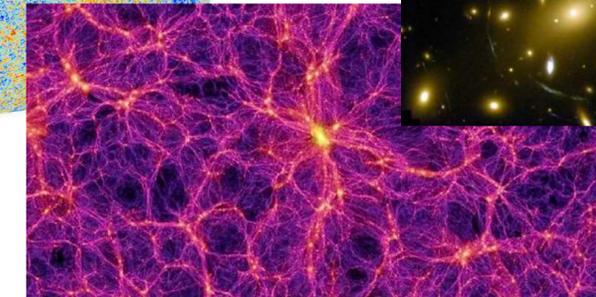
CMB+LSS



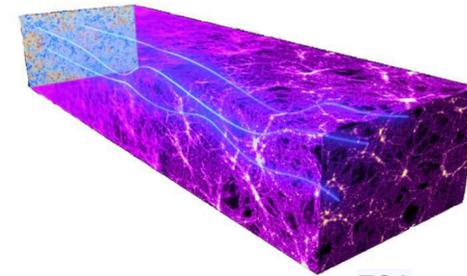
ESA and the Planck Collaboration



NASA and ESA

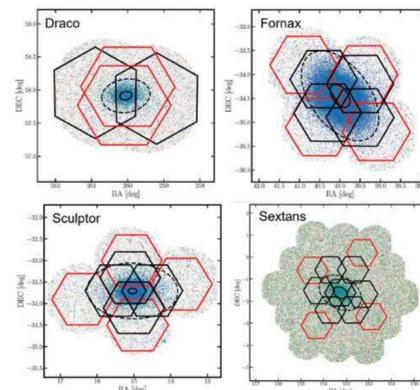


Springel & others / Virgo Consortium

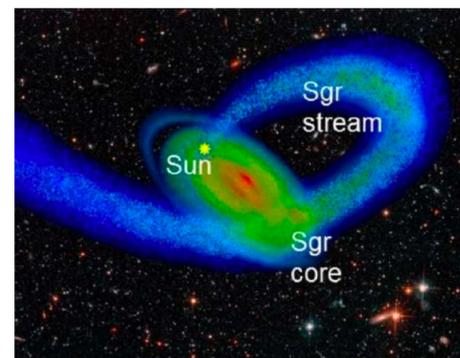


ESA

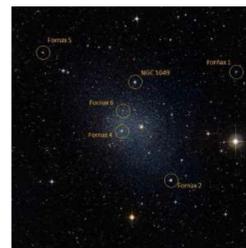
Dwarfs



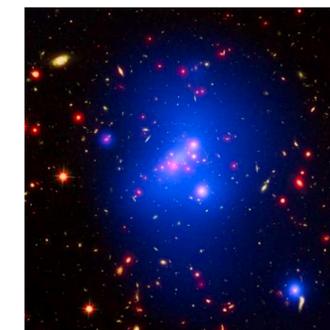
Stellar stream



Globular clusters

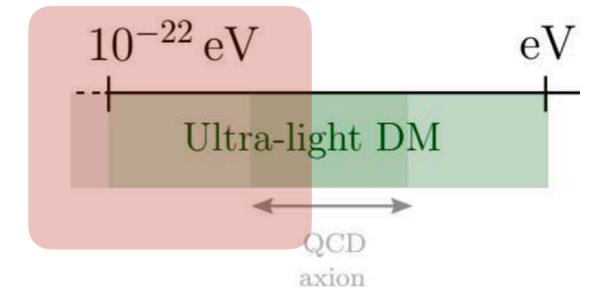


Clusters

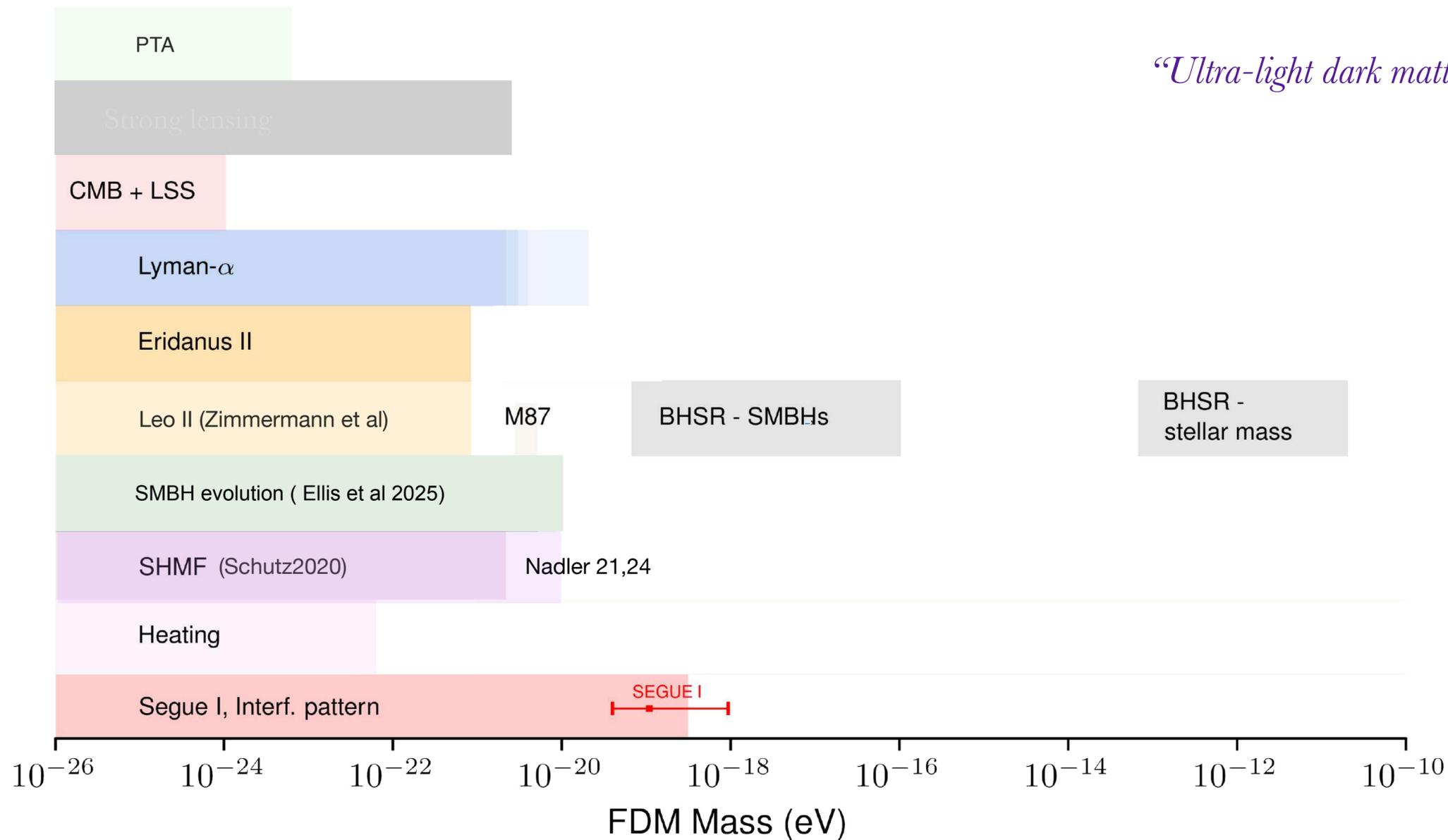


Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass



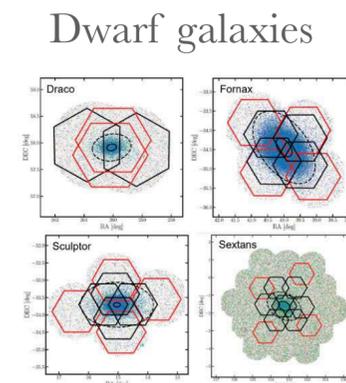
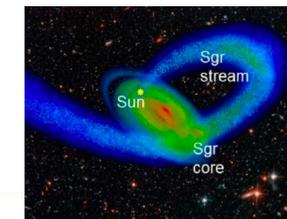
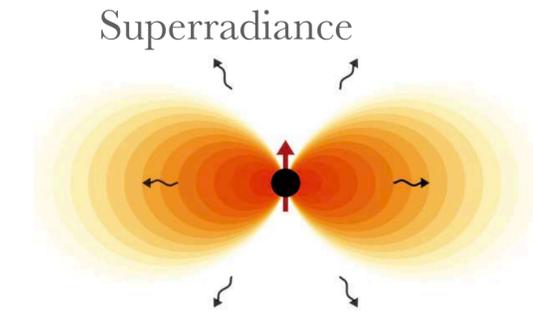
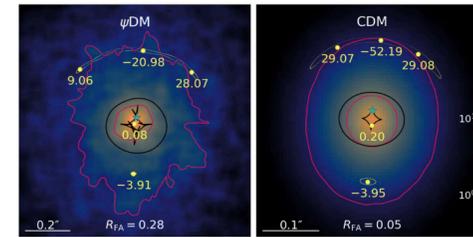
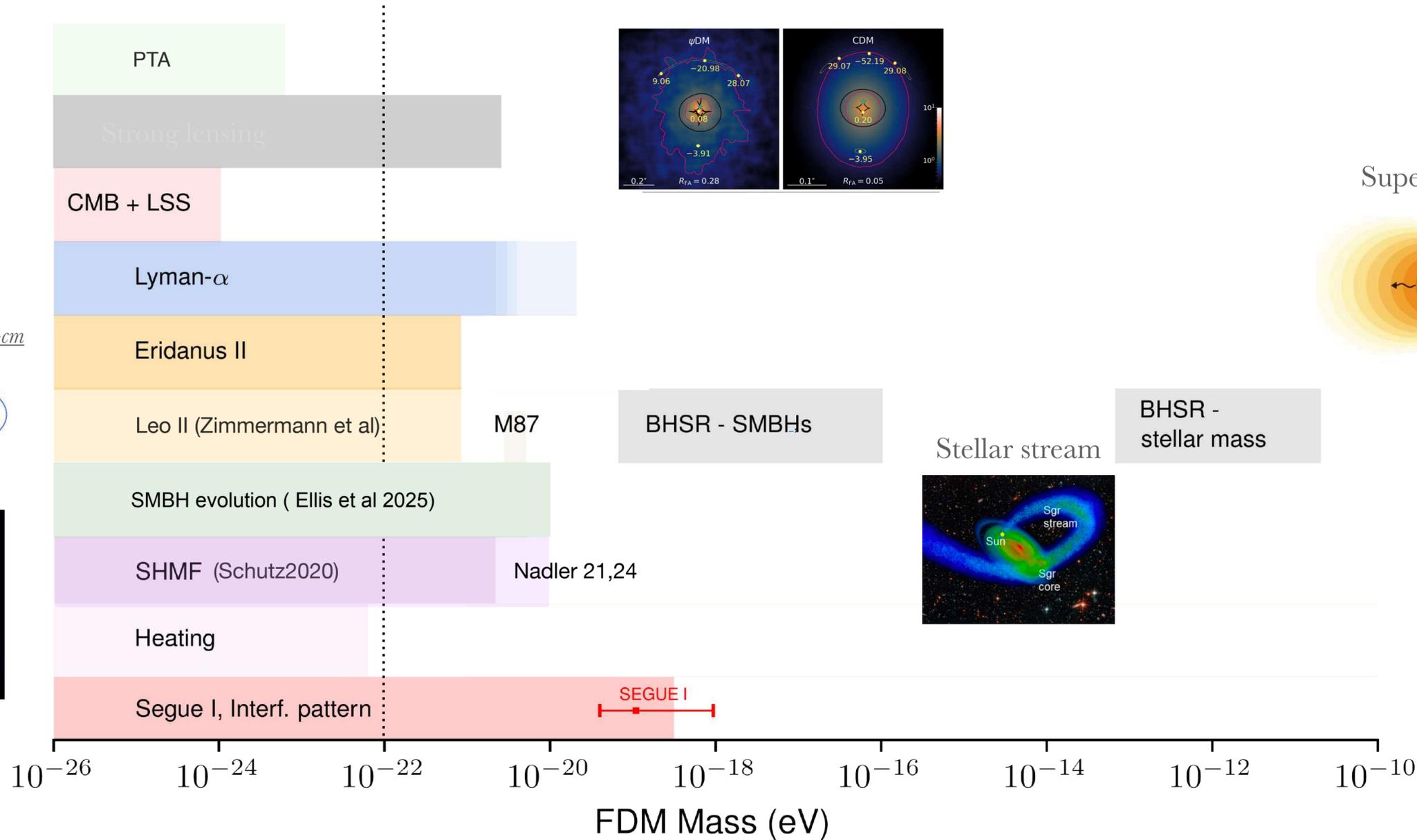
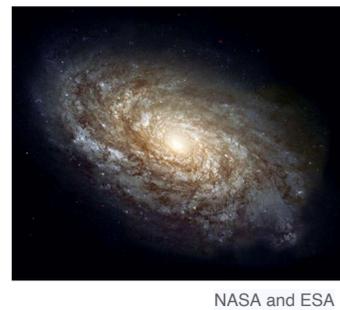
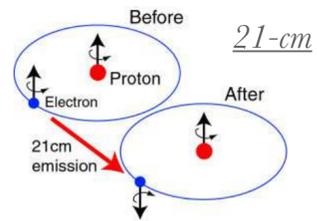
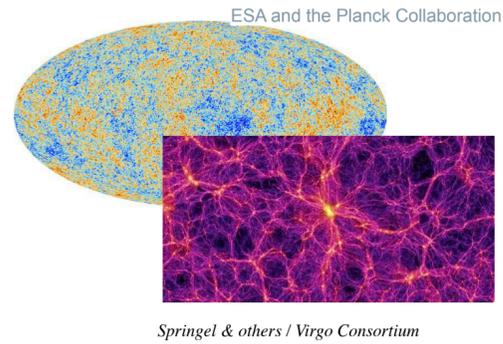
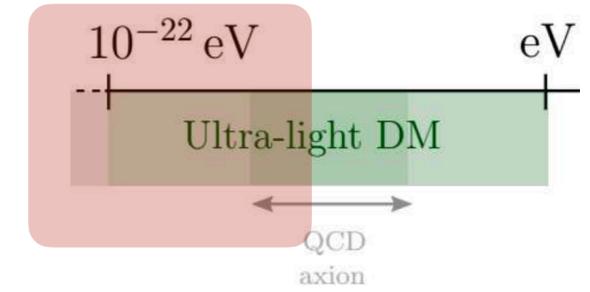
“Ultra-light dark matter”, **E.F.**, 2020. The Astronomy and Astrophysics Review.



Bounds consider FDM is *all* DM

Current status

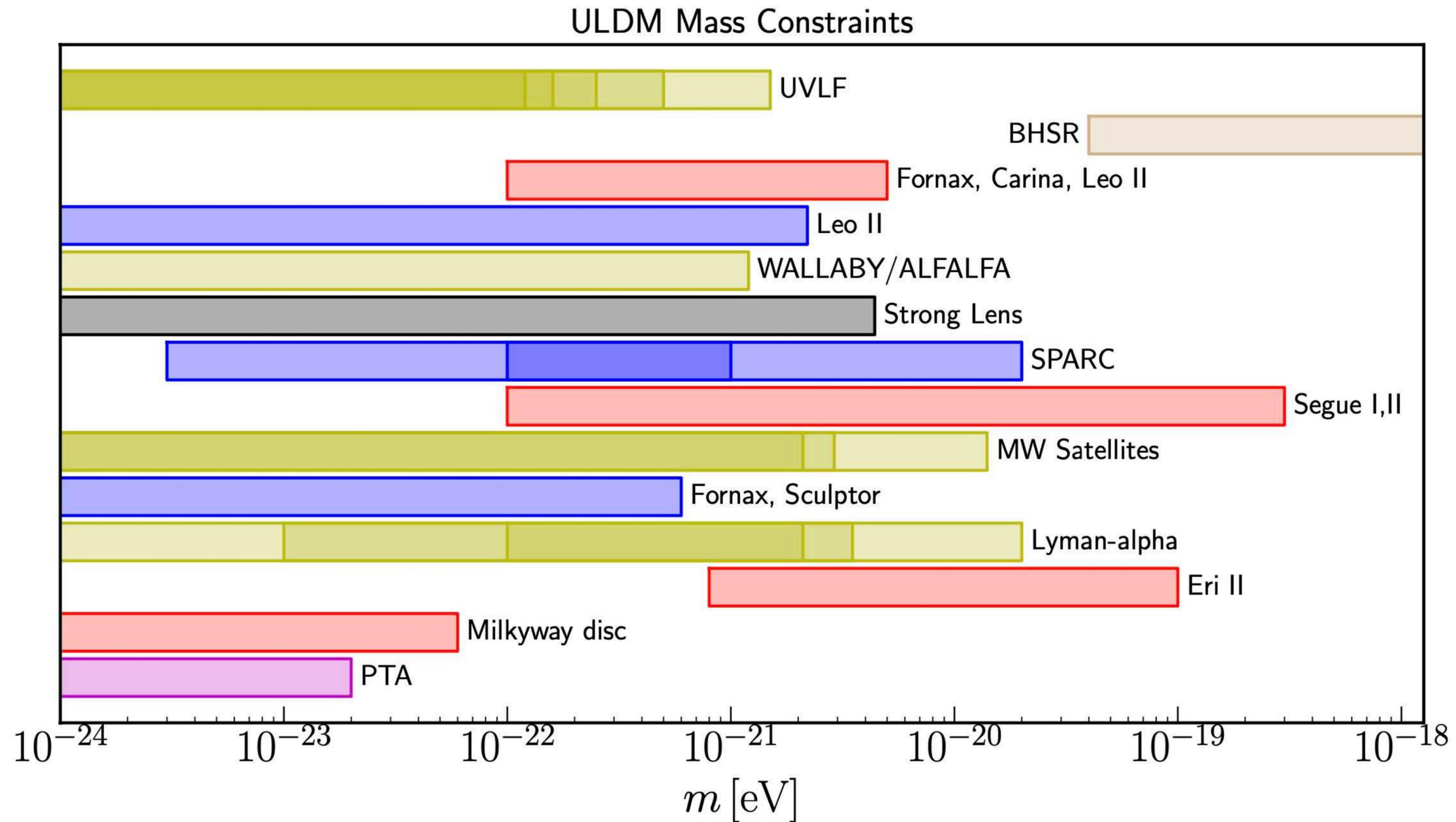
Fuzzy Dark Matter - bounds on the mass



Current status

Fuzzy Dark Matter - bounds on the mass

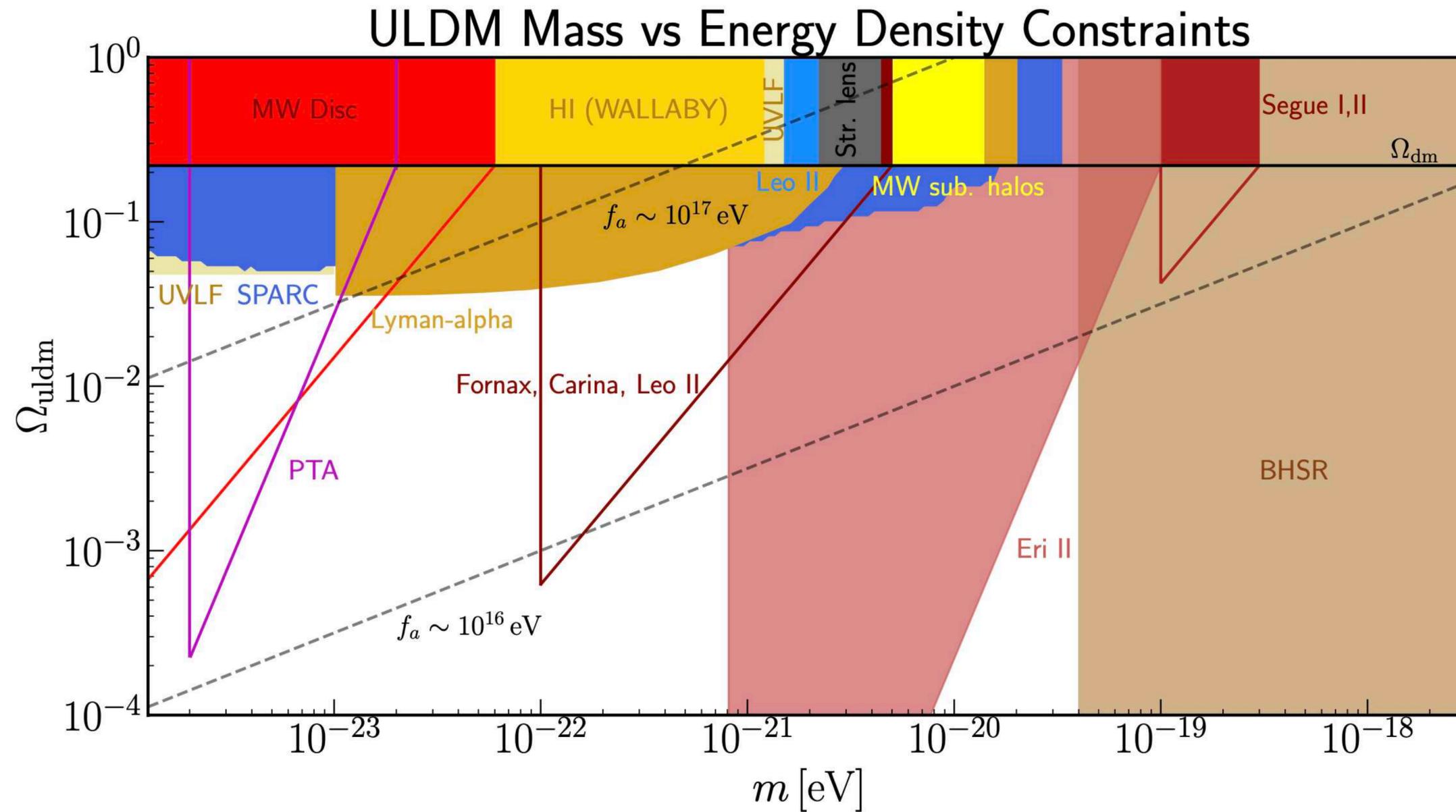
Review: Eberhardt, EF, 2025



Current status

Fuzzy Dark Matter - bounds on the mass

Review: Eberhardt, EF, 2025



How to probe these?

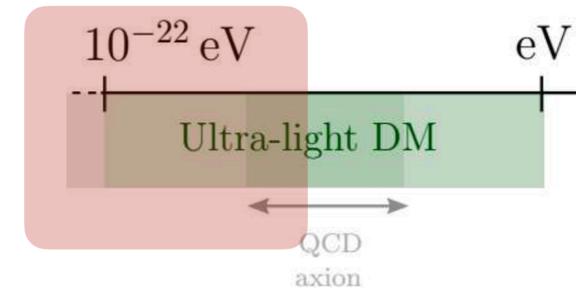
Evolution and suppression: CMB and LSS

Observational implications and constraints

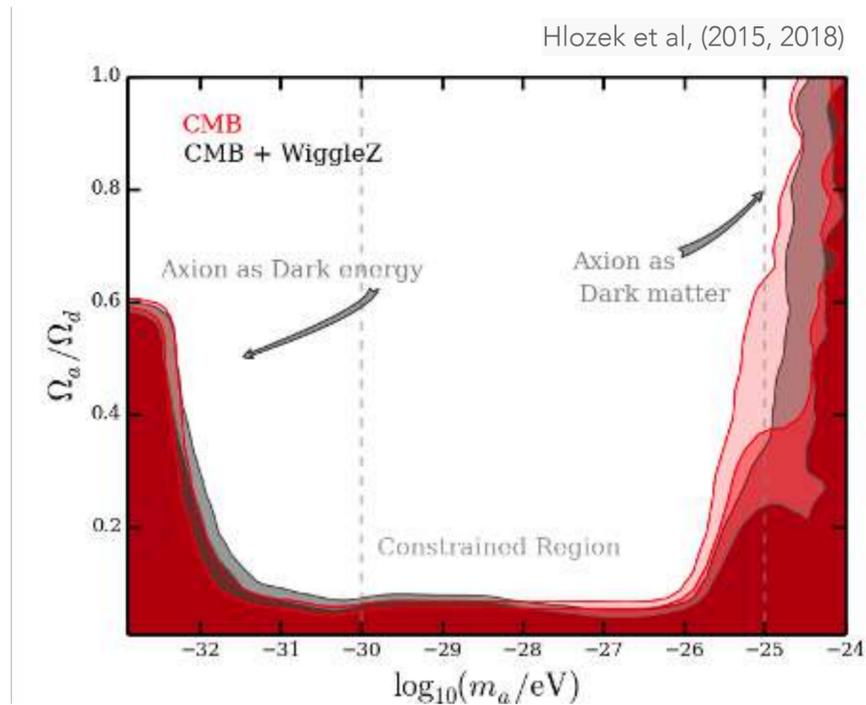
Fuzzy Dark Matter - bounds on the mass

Suppression of small structures + evolution

Extremely light dark matter or axion DE

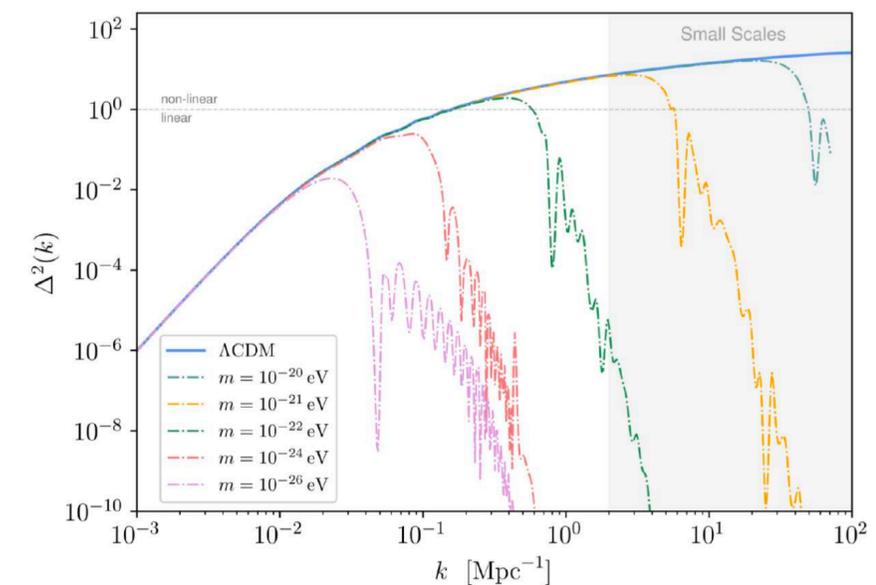
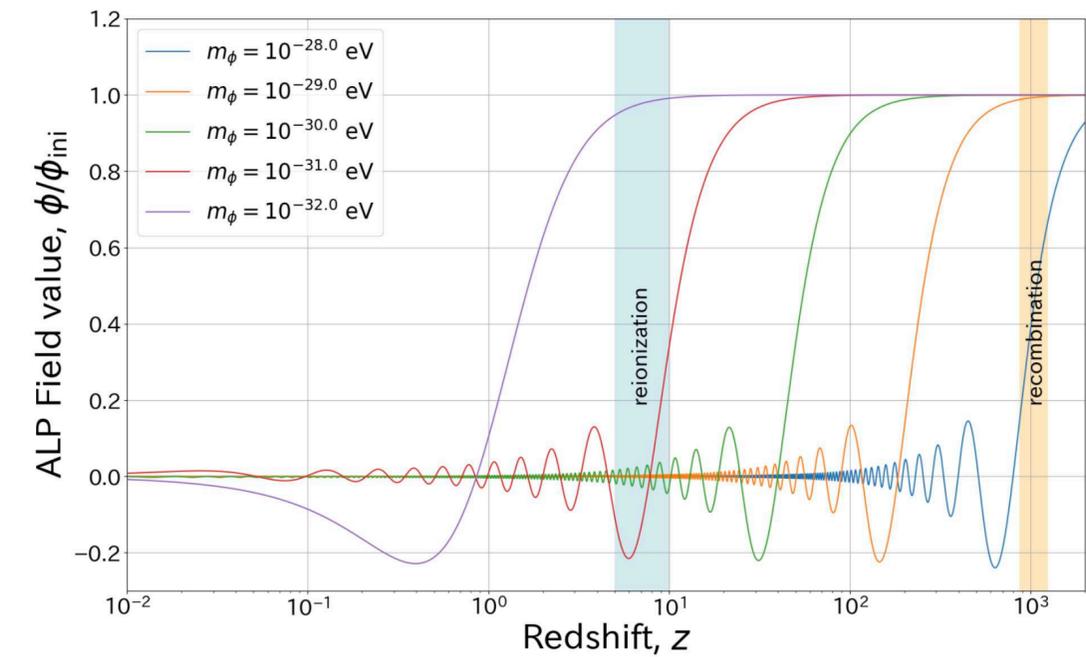


CMB/LSS



$$m \gtrsim 10^{-24} \text{ eV}$$

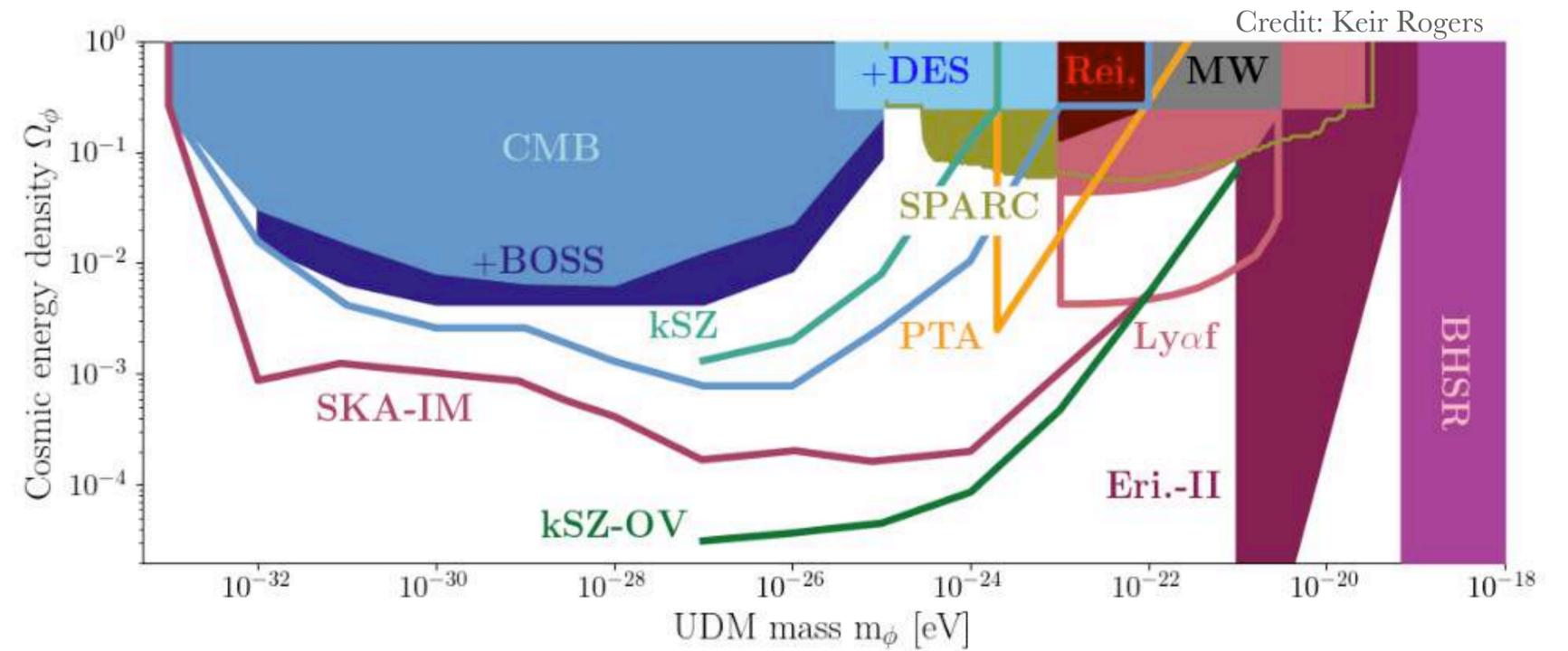
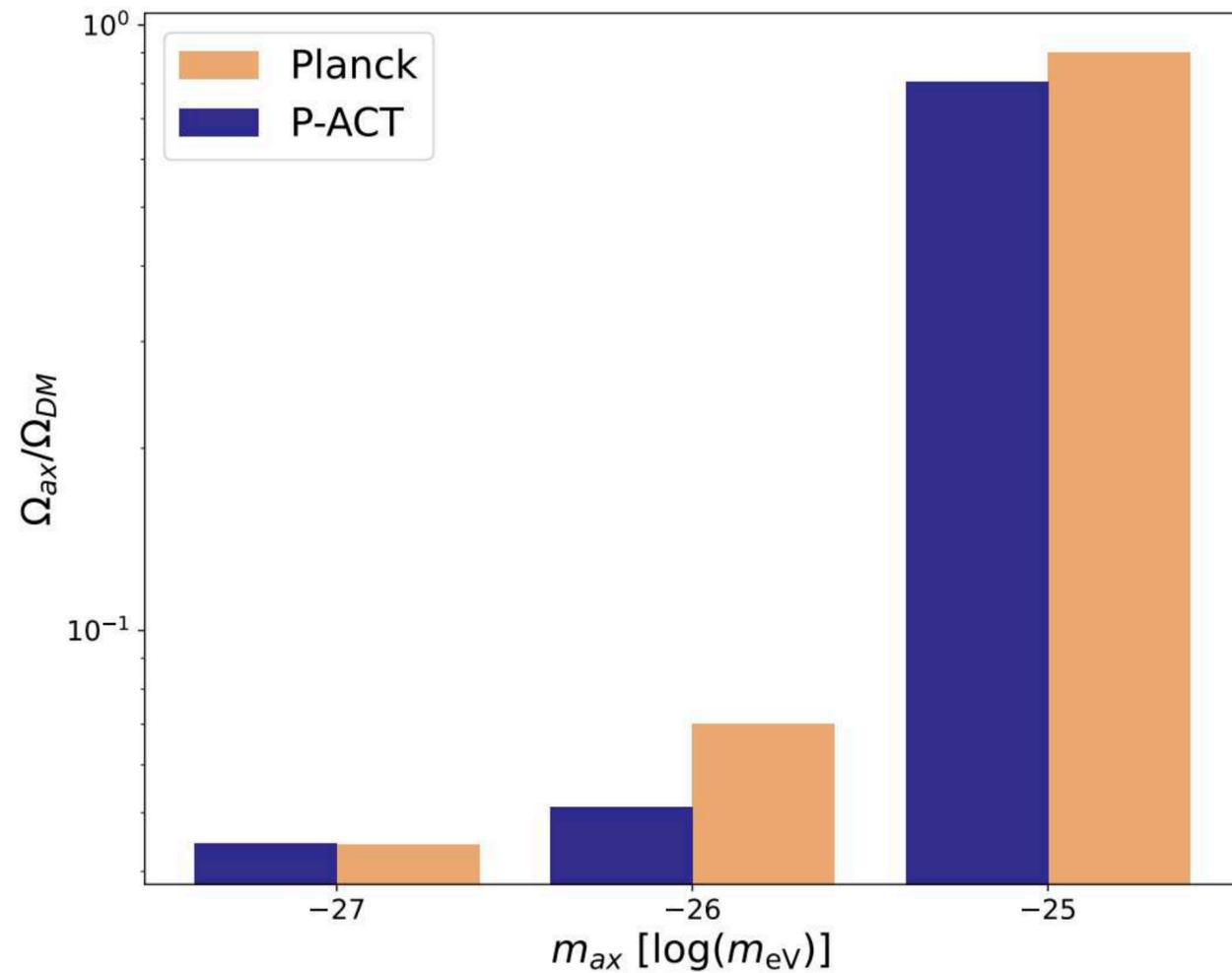
Atacama Cosmology Telescope (ACT) Data Release 6 (DR6) (2025) improved over these bounds



CMB and LSS

Evolution and shape of PS

Atacama Cosmology Telescope (ACT) Data Release 6 (DR6) (2025) improved over these bounds

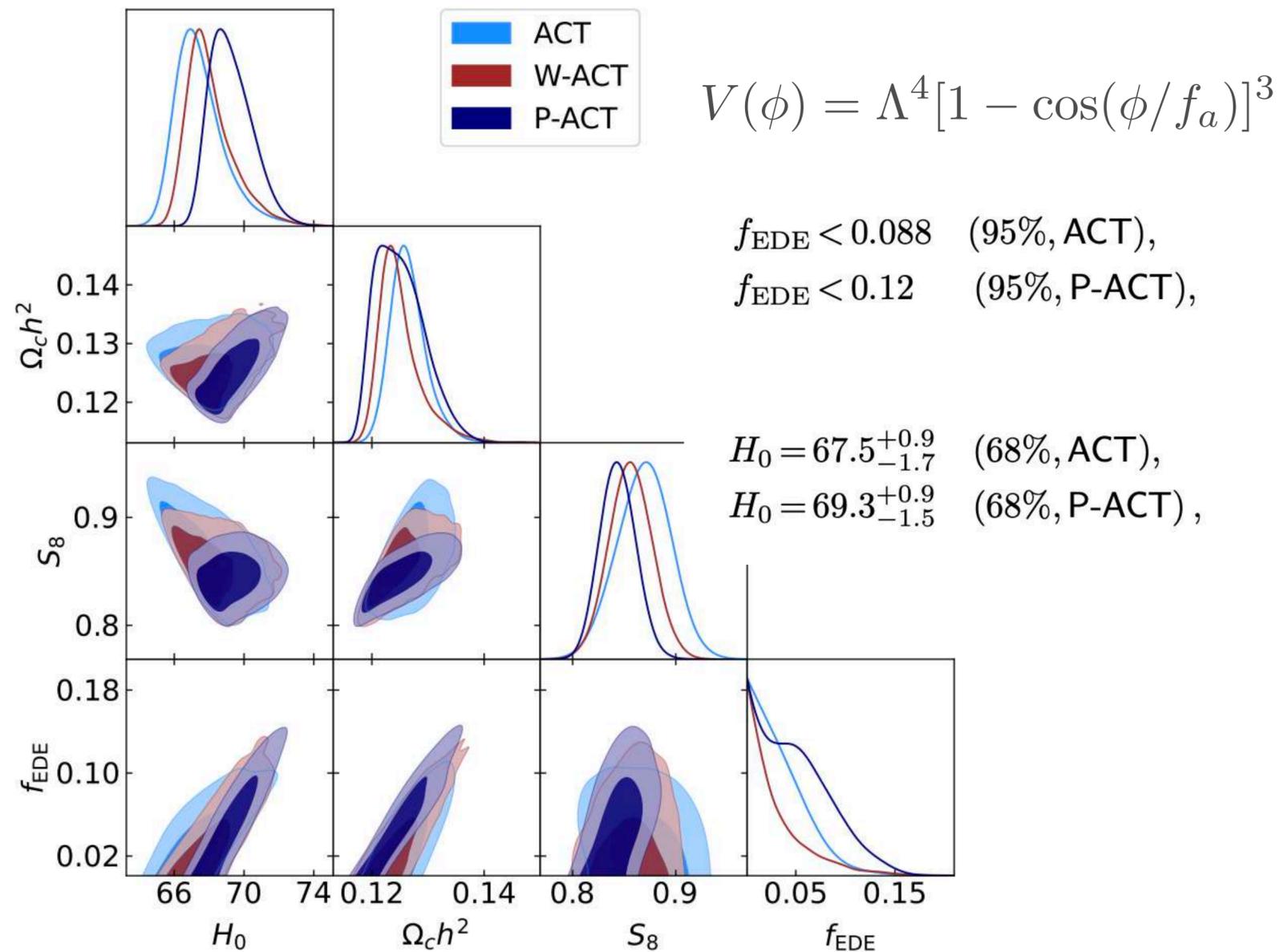


$m_{ax} = 10^{-26}$ eV :

$$\begin{aligned} \Omega_{ax}/(\Omega_{ax} + \Omega_c) &< 0.070 \quad (95\%, \text{Planck}) \\ &< 0.052 \quad (95\%, \text{P-ACT}). \end{aligned} \quad (51)$$

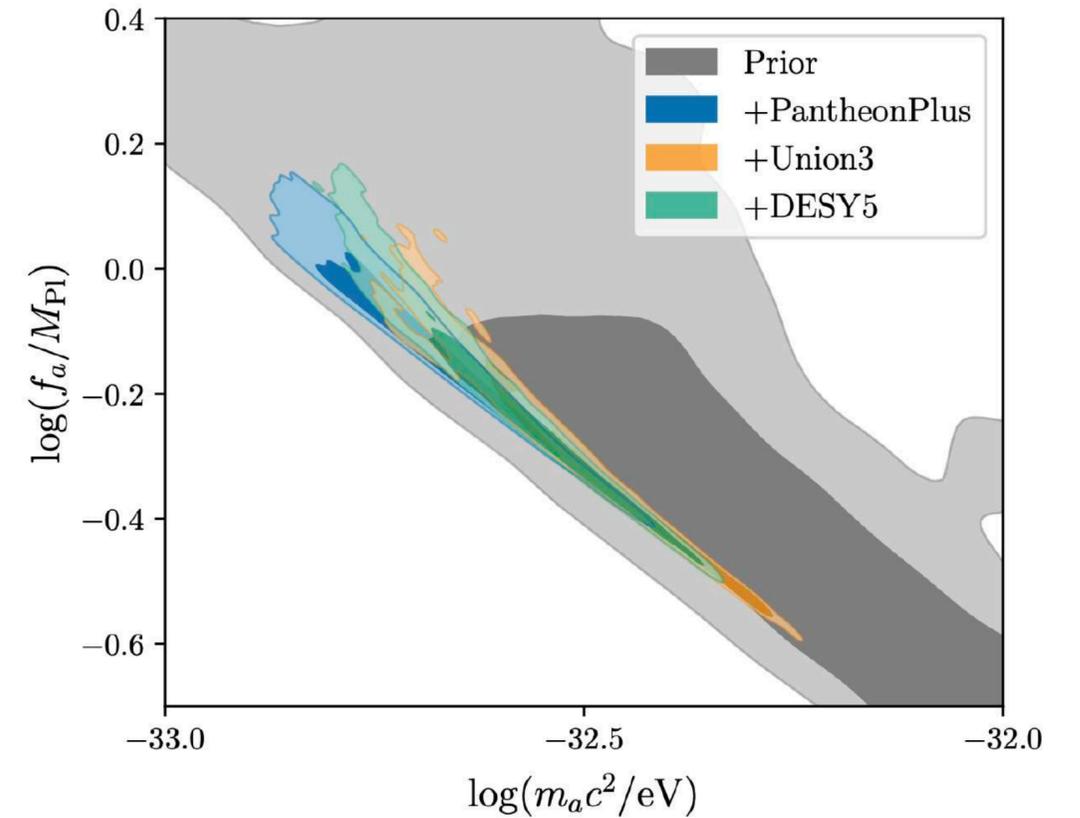
ACT DR6

Early dark energy



DESI

Axion dark energy



DESI

$$\log(m_a c^2 / \text{eV}) \simeq -32.6$$

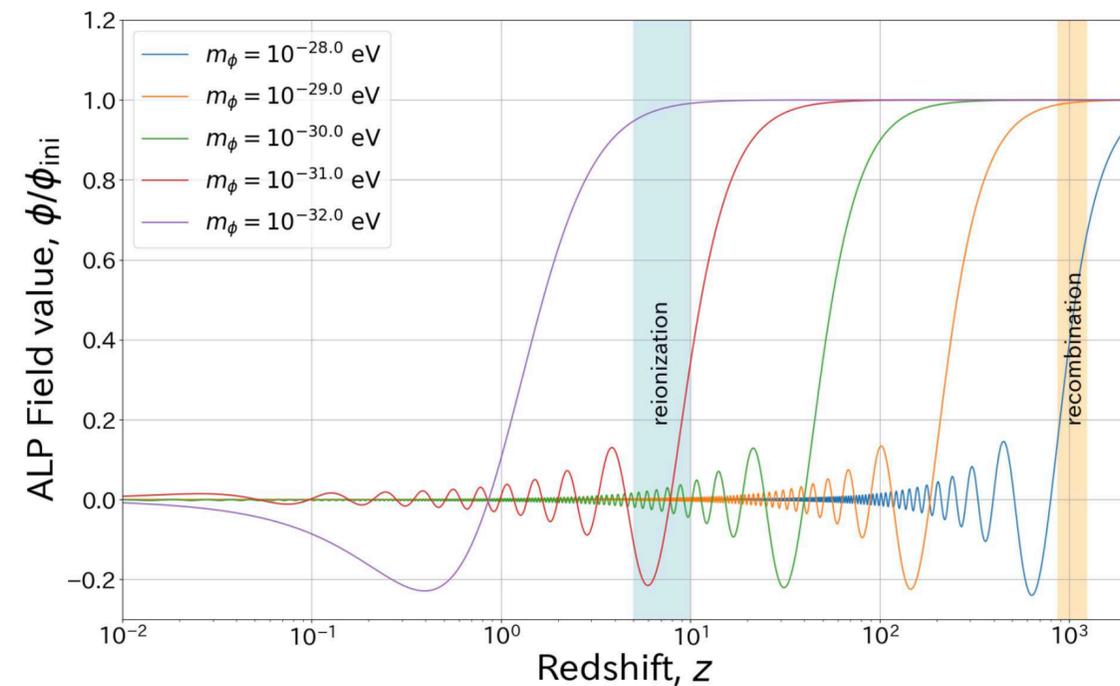
$$\log(f_a / M_{\text{Pl}}) \simeq -0.22$$

Previous: Planck

$$m_a^2 f_a^2 \simeq 2.3 \times 10^{-11} \text{eV}^4$$

$$f_a / M_{\text{Pl}} > 0.67$$

Emulator for *FDM*



Linear predictions:

Boltzmann codes: axionCAMB, AxionECAMB, AxiCLASS

Very slow!! 1 - 8 min per spectrum

Parameter inference → very hard!

New emulator (to appear) **(Work in progress)** with *Fernanda Matos*

Phase 1 - linear emulator

Most complete ULDM emulator in the market!

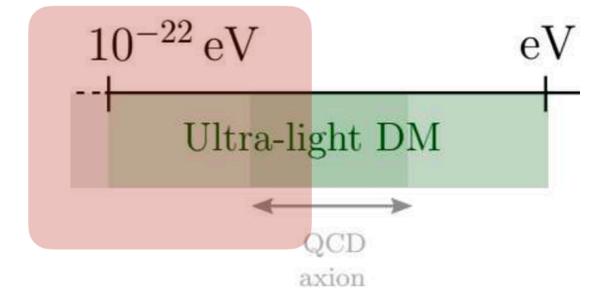
Phase 2 - non-linear emulator



Observational implications and constraints

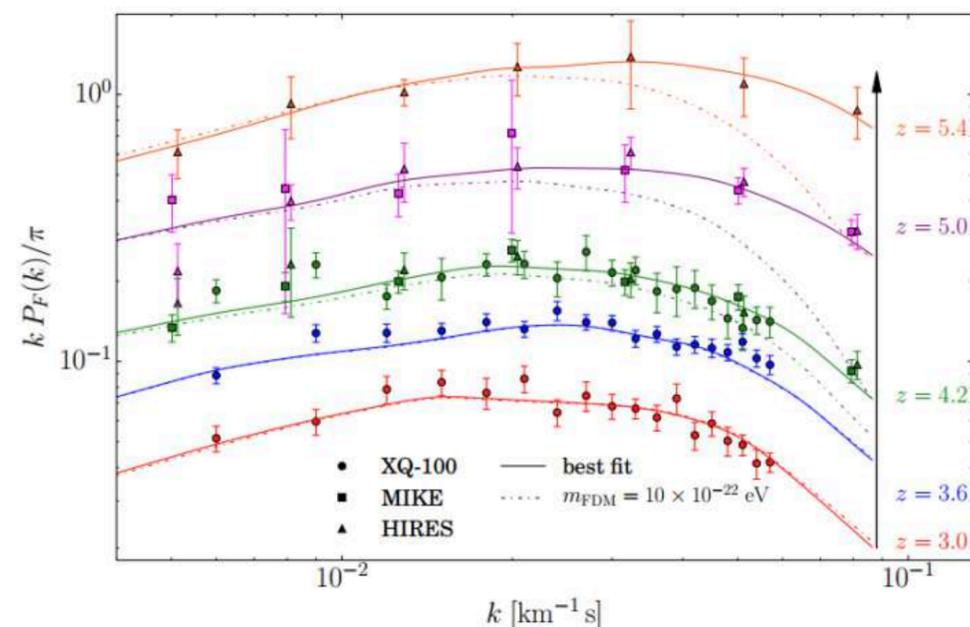
Fuzzy Dark Matter - bounds on the mass

Suppression of small structures + evolution



Lyman alpha

Armengaud et al. (2017); Iršič et al. (2017);
Rogers et al. (2020)



$$m \gtrsim 2 \times 10^{-20} \text{ eV}$$

so enough Mpc-scale power in Ly- α forest at $z = 5$.

One of the **strongest** bounds on ULDM!

Constraints depends on:

- IGM modelling - simplifying assumptions
- Trusts on IC sims

(Work in progress) with Simon May

New cosmological fuzzy dark matter simulations including baryons, using the IllustrisTNG galaxy formation model

Revise these bounds + study the evolution of IGM as a way of constraining FDM.
IGM properties not so influenced by feedback
Filaments and interference patterns important here!

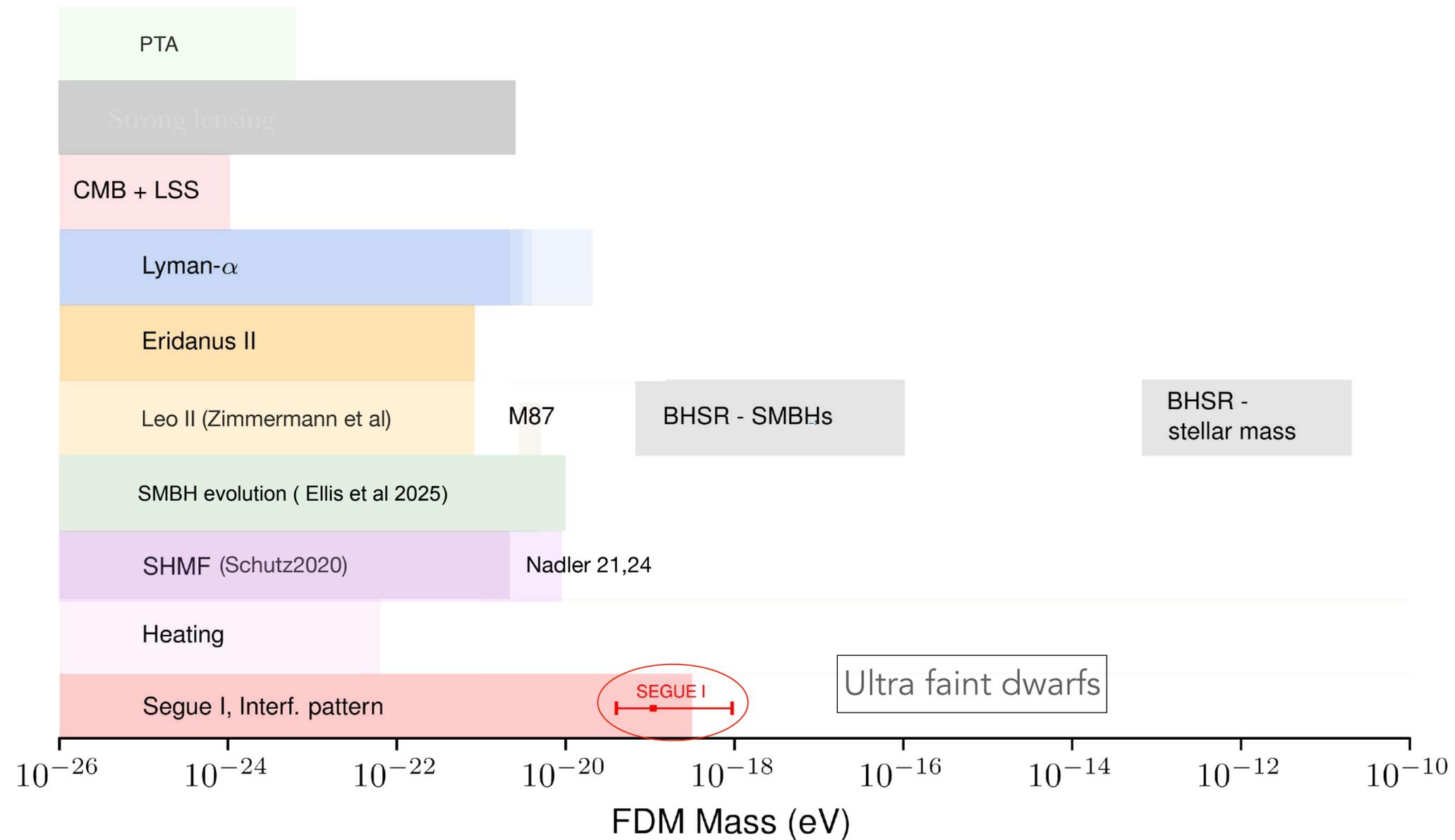
How to probe these?

*Presence of a **core***

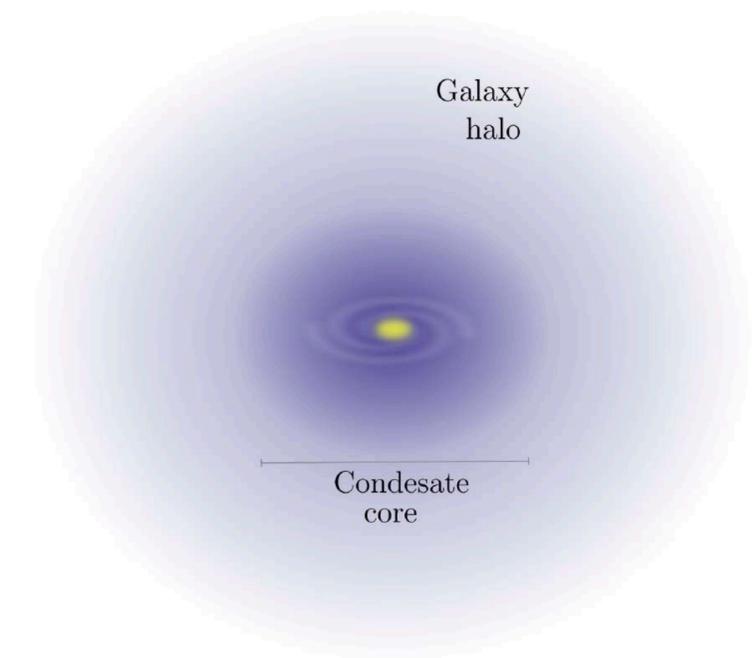
Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass

“Narrowing the mass range of Fuzzy Dark Matter with Ultra-faint Dwarfs”, J. Chan, E.F., K. Hayashi, 2021.



Presence of a core



Ultra-light Dark Matter

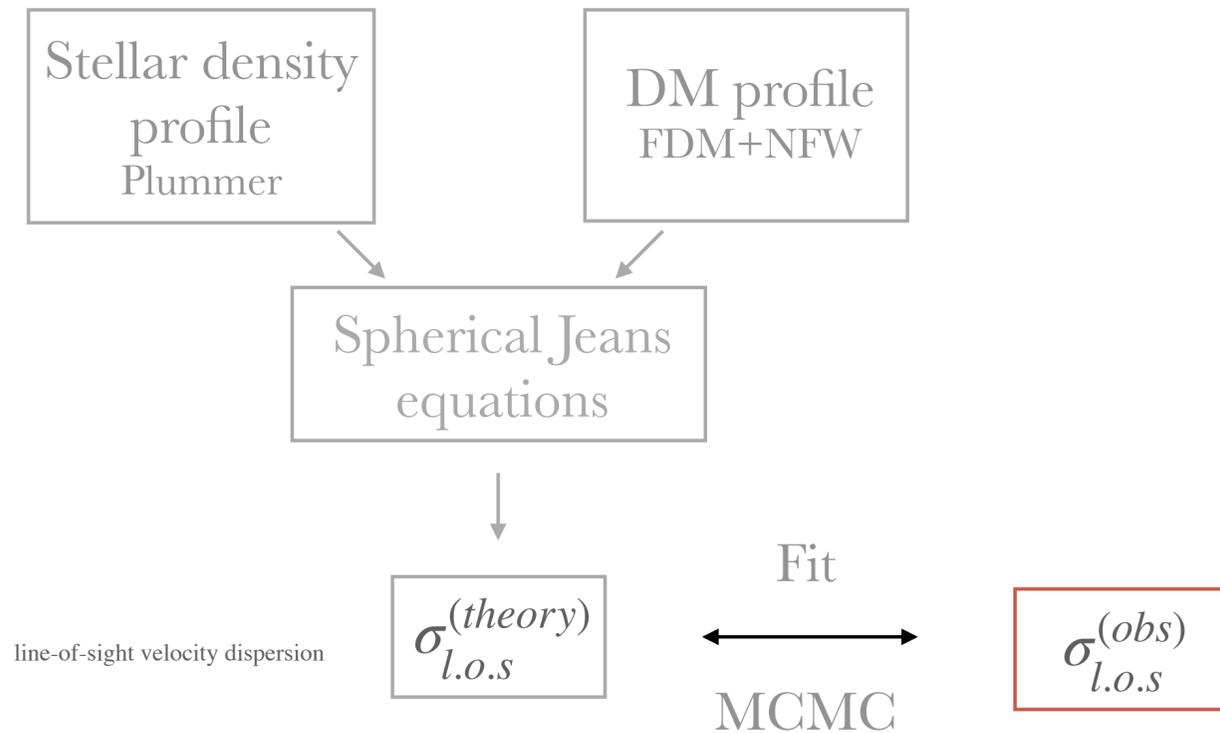
FDM mass from Ultra-faint dwarfs

Hayashi, E.F, Chan, 2021.

Ultra-faint dwarfs (UFD): ideal laboratory to study DM

Stellar kinematic data from 18 UFDs to fit the FDM profile:

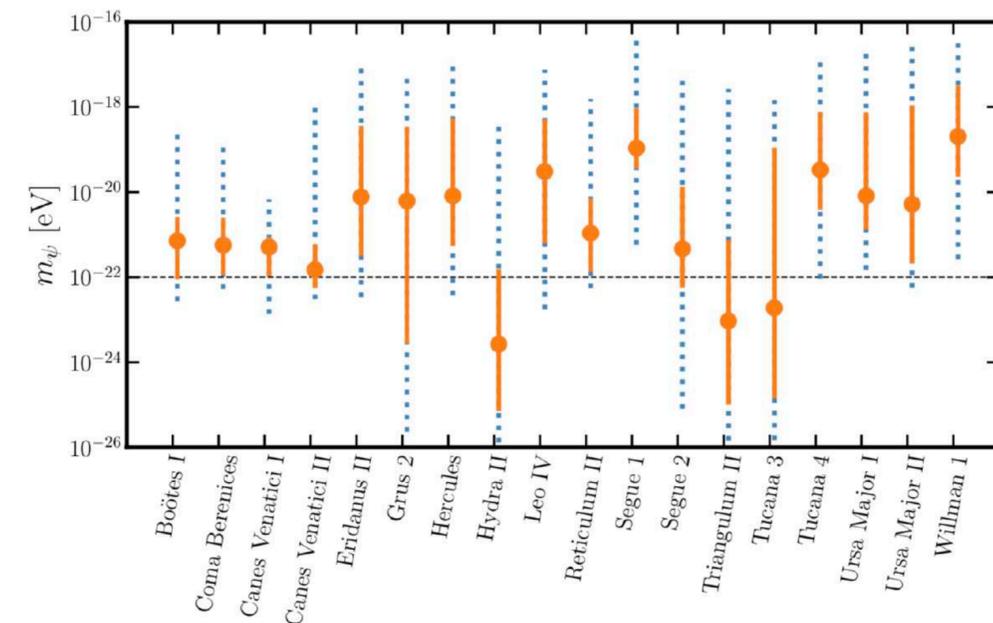
FDM SIMULATIONS



$$\rho(r) = \begin{cases} \rho_{\text{soliton}} \simeq \frac{\rho_c}{[1 + 0.091(r/r_c)^2]^8}, & r < r_e \\ \rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, & r > r_e \end{cases}$$

$$\rho_c(r) = 1.9 \times 10^{12} \left(\frac{m}{10^{-23} \text{ eV}} \right)^{-2} \left(\frac{r_c}{\text{pc}} \right)^{-4} [M_\odot \text{ pc}]$$

$$r_c \simeq 1600 \left(\frac{m}{10^{-23} \text{ eV}} \right)^{-1} \left(\frac{M_{\text{halo}}}{10^{12} M_\odot} \right)^{-1/3} [\text{pc}]$$



Parameter space (10): $\left\{ m, M_{\text{halo}}, r_e, r_s, r_\beta, \beta_0, \beta_\infty, \eta, r_h, v_{\text{sys}} \right\}$

Stellar velocity anisotropy

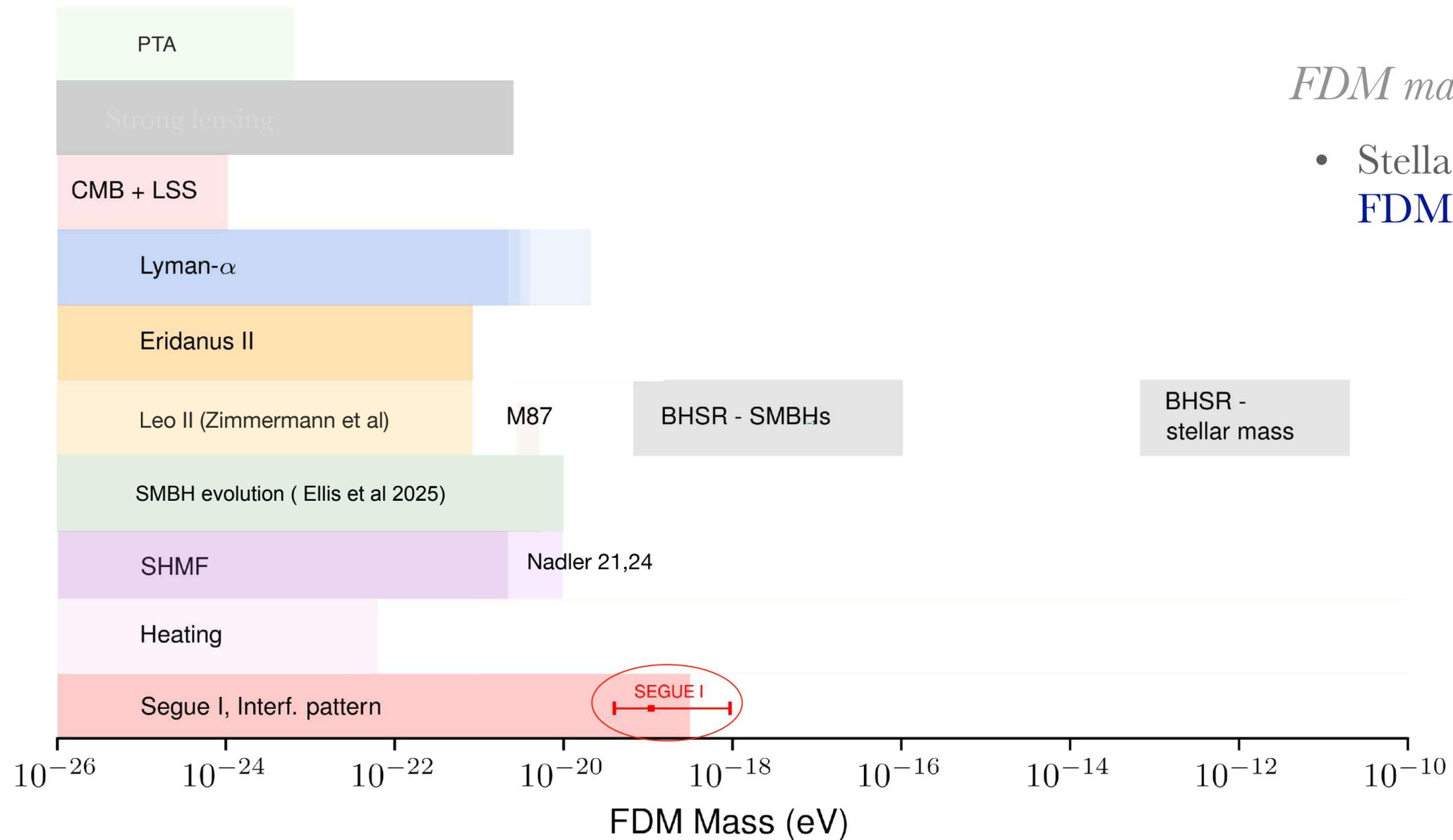
Strongest constraint on m_{FDM} to date!

Ultra-light Dark Matter

Fuzzy Dark Matter - bounds on the mass

Ultra faint dwarfs

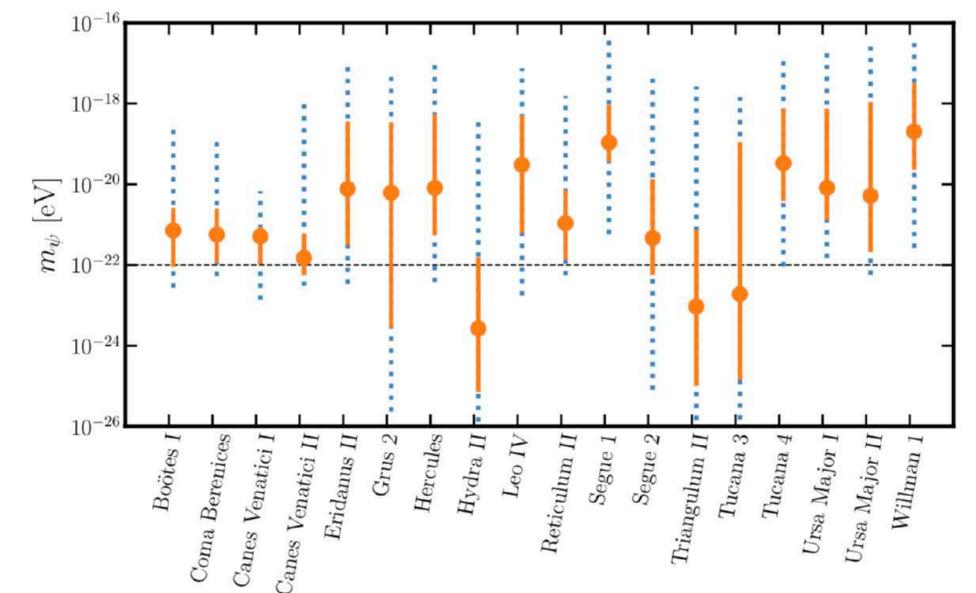
Hayashi, E.F, Chan, 2021.



FDM mass from Ultra-faint dwarfs

- Stellar kinematic data from 18 UFDs to fit the FDM profile from simulations

$$m_{\text{FDM}}^{(\text{Seg1})} = 1.1^{+8.3}_{-0.7} \times 10^{-19} \text{ eV}$$



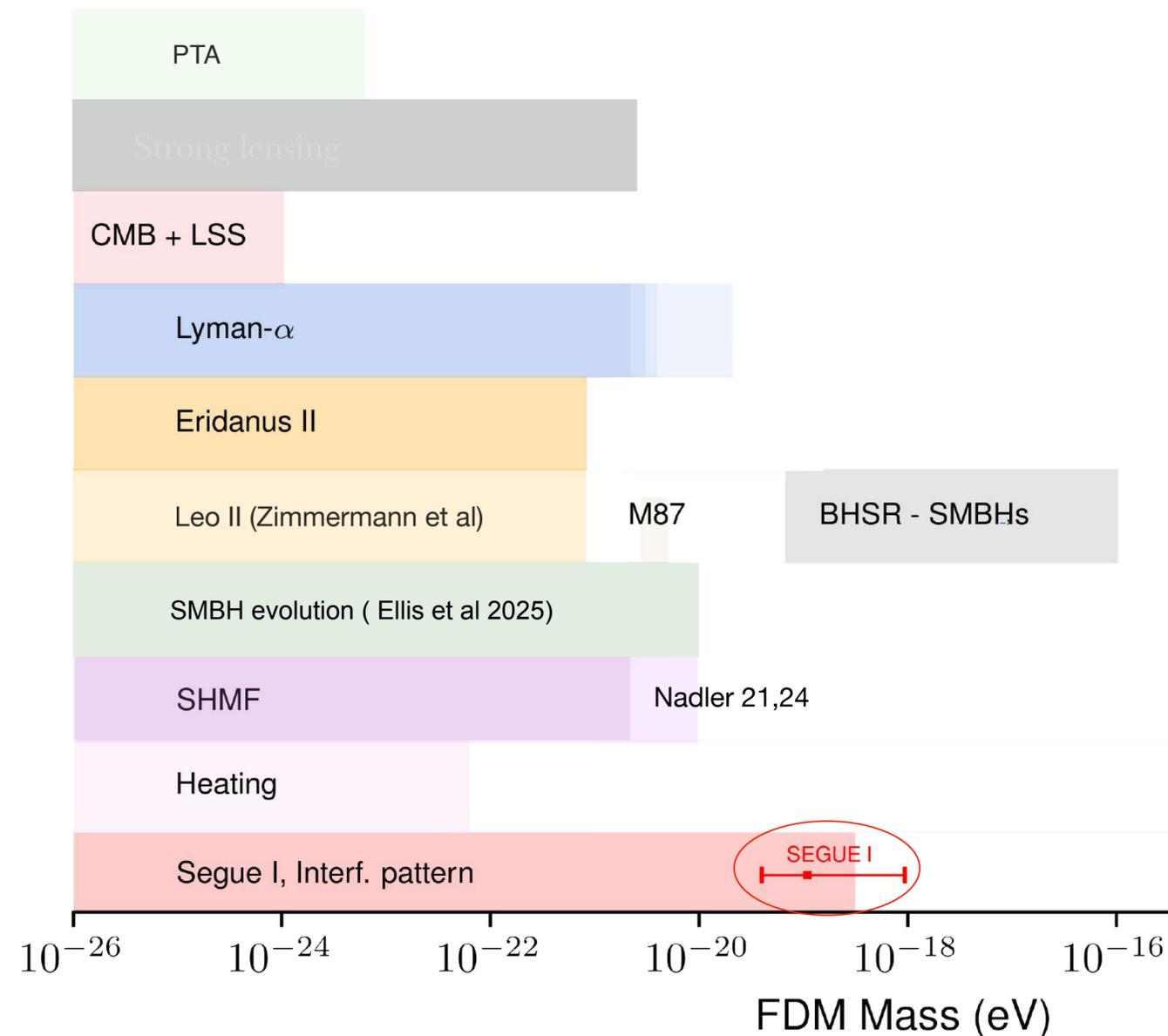
Preference for higher mass

Ultra-light Dark Matter

Fuzzy Dark Matter - bounds on the mass

Ultra faint dwarfs

Hayashi, E.F, Chan, 2021.



FDM mass from Ultra-faint dwarfs

- Stellar kinematic data from 18 UFDs to fit the FDM profile from simulations

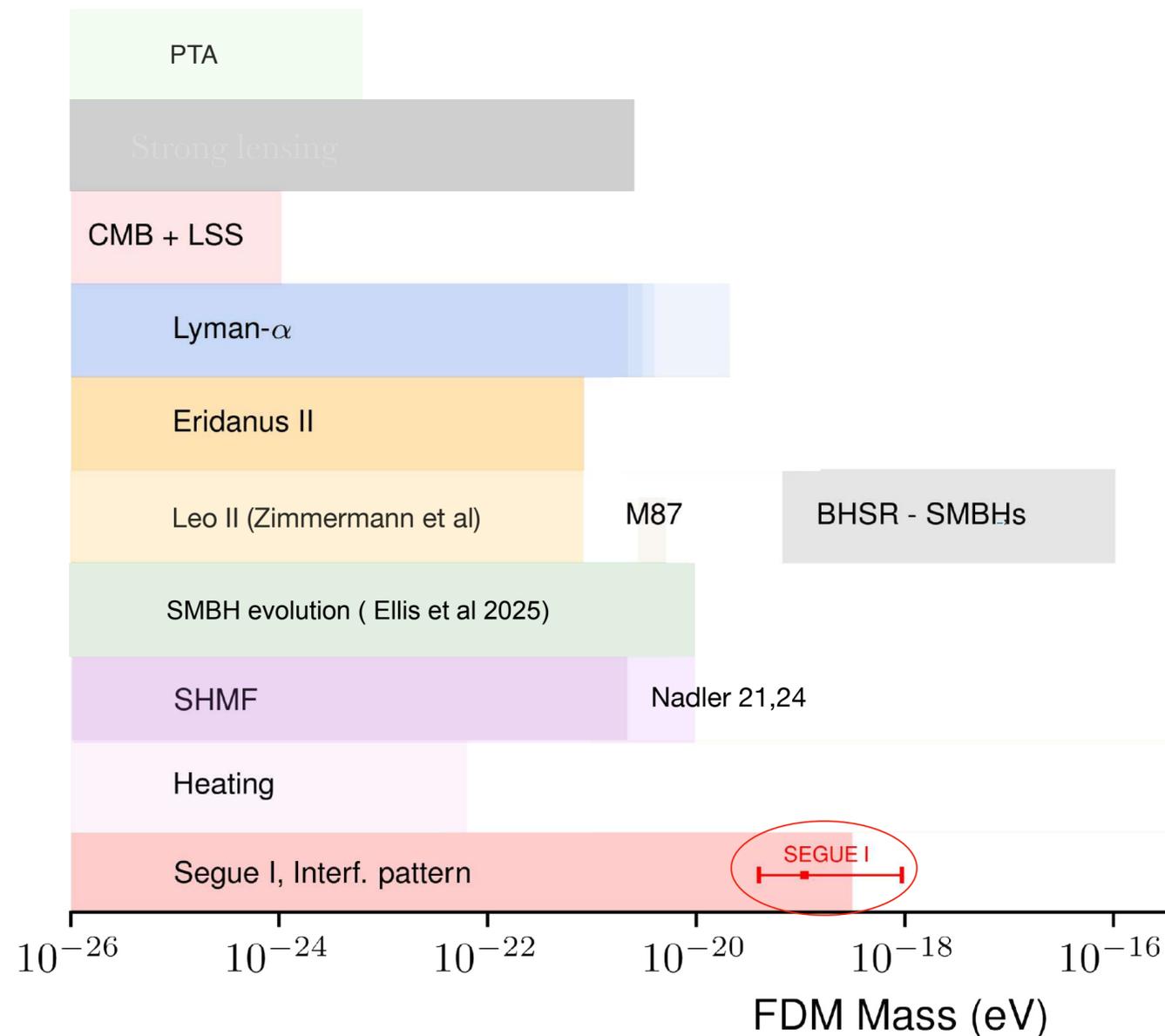
$$m_{\text{FDM}}^{(\text{Seg1})} = 1.1_{-0.7}^{+8.3} \times 10^{-19} \text{ eV}$$

Important:

- Bayesian analysis - reason for a constraint
- 'Bad' assumption
- Systematic effects !

Ultra-light Dark Matter

Fuzzy Dark Matter - bounds on the mass



Ultra faint dwarfs

Hayashi, E.F, Chan, 2021.

FDM mass from Ultra-faint dwarfs

- Stellar kinematic data from 18 UFDs to fit the FDM profile from simulations

$$m_{\text{FDM}}^{(\text{Seg1})} = 1.1_{-0.7}^{+8.3} \times 10^{-19} \text{ eV}$$

Important:

- Bayesian analysis - reason for a constraint
- 'Bad' assumption
- Systematic effects !

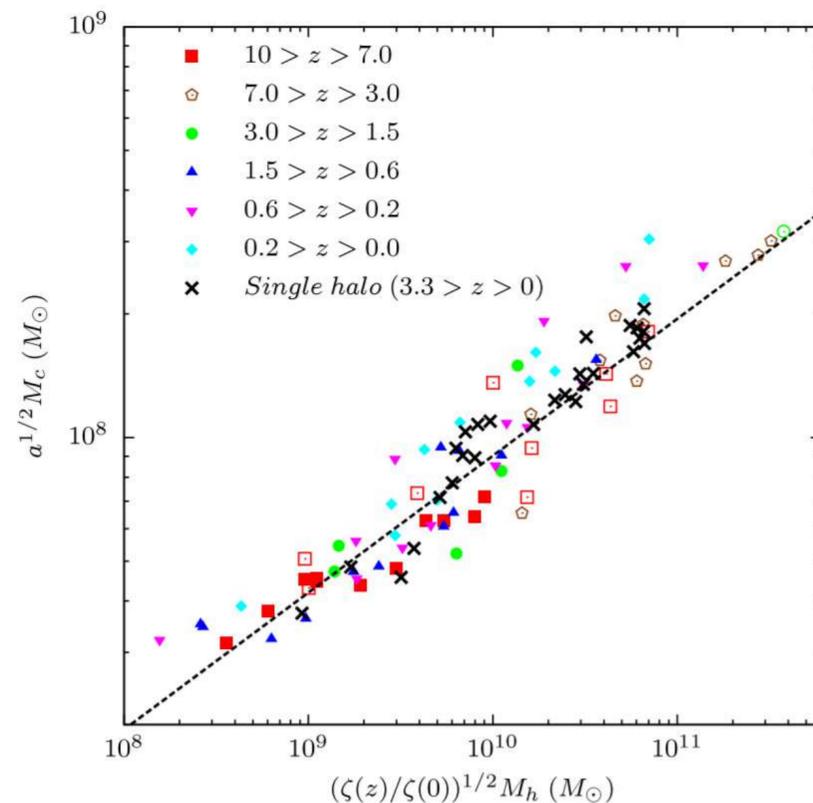
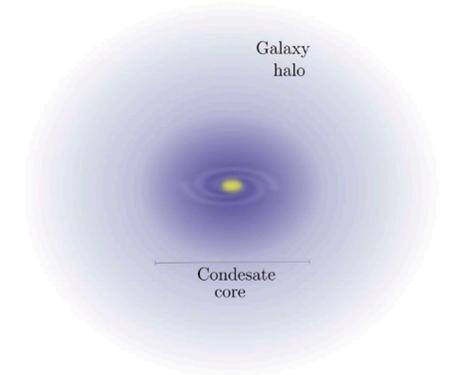
FDM - Core-halo mass relation

J. Chan et al. 2021

We want to study how the core relates to the halo mass - might be one part this puzzle

$$\rho_c \simeq \frac{1.9 \times 10^{-2}}{[1 + 0.091 (r/R_{1/2,c})^2]^8} \left(\frac{m}{10^{-22} \text{ eV}}\right)^{-2} \left(\frac{r_c}{\text{kpc}}\right)^{-4} M_\odot \text{ pc}^{-3},$$

$\xrightarrow{\quad ? \quad} M_h$



Schive et al. 2014

Schive et al 2014

$$M_c \propto M_h^{1/3}$$

Velocity dispersion tracing

$$\sigma_c \sim \sigma_h$$

Mocz et al 2017

$$M_c \propto M_h^{5/9}$$

Energy tracing

$$M_c \sigma_c^2 \sim M_h \sigma_h^2$$

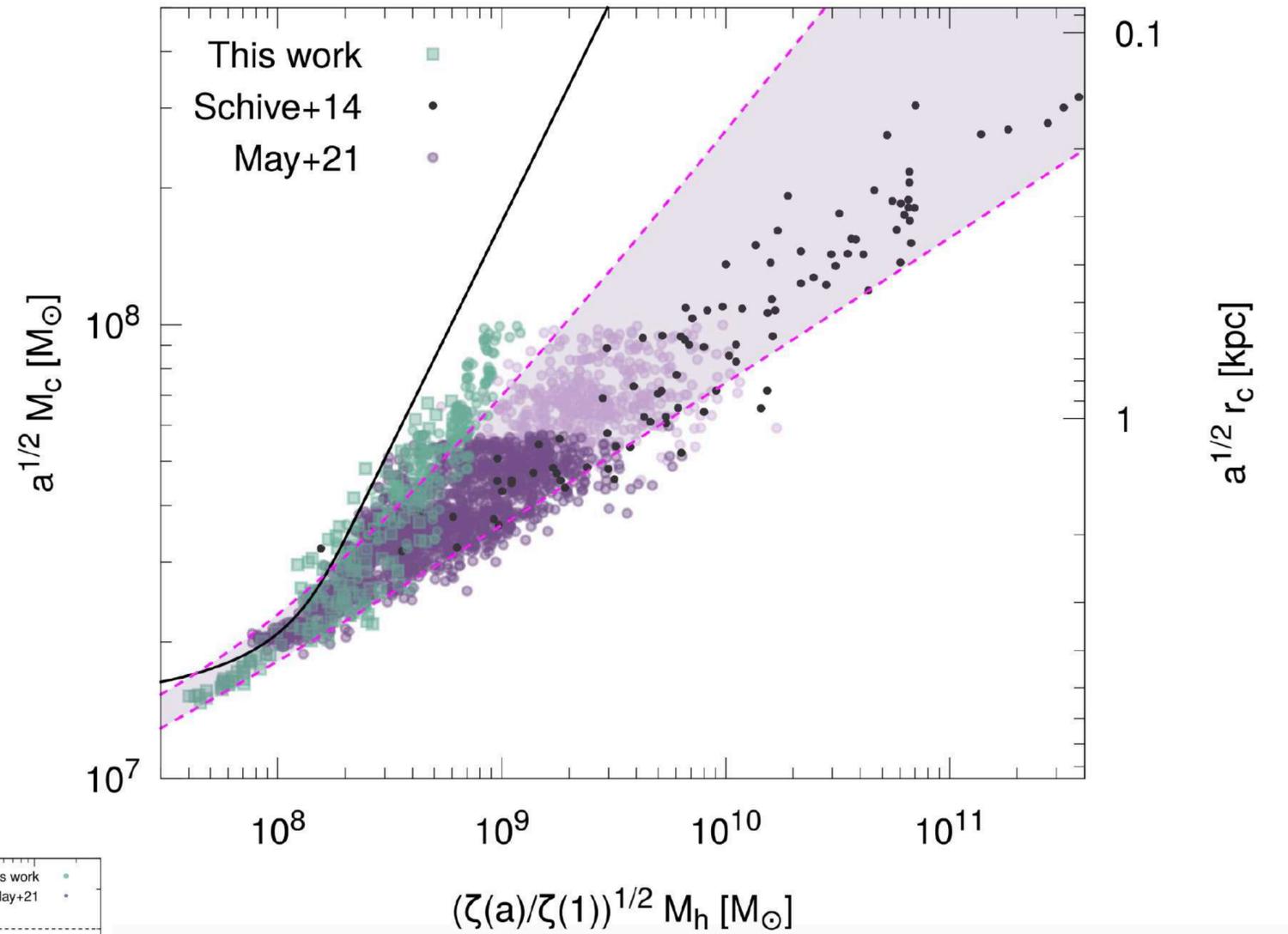
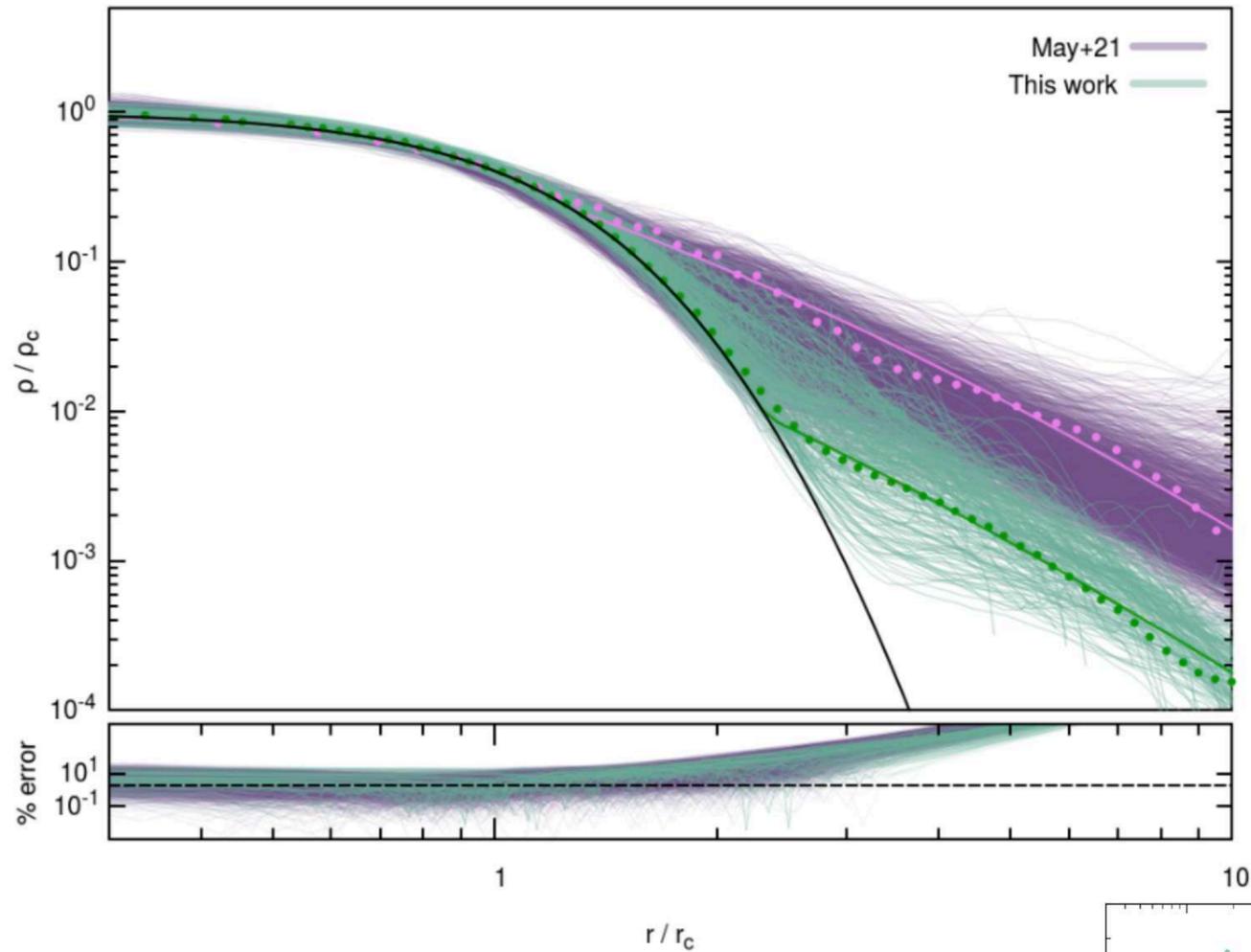
Velmatt et al 2018, Nori et al 2020, Nima et al 2020

= Schive

≠ Schive

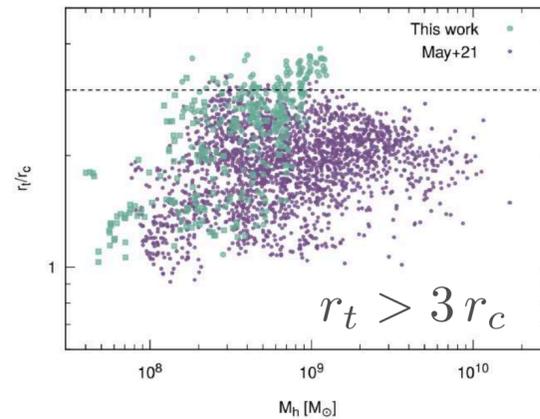
FDM - Core-halo mass relation

J. Chan, EF, S. May, K. Hayashi, M. Chiba 2021



Well fitted by:

$$\rho(r) = \begin{cases} \rho_{\text{soliton}} \simeq \frac{\rho_c}{[1 + 0.091(r/r_c)^2]^8}, & r < r_e \\ \rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, & r > r_e \end{cases}$$



Ultra-light Dark Matter

Fuzzy Dark Matter - bounds on the mass

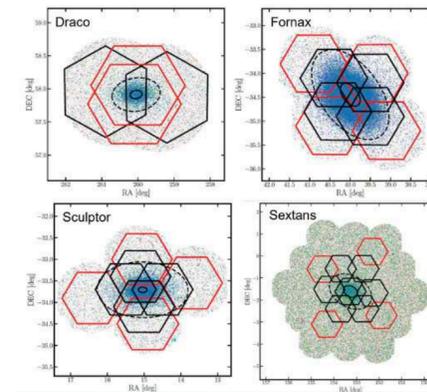
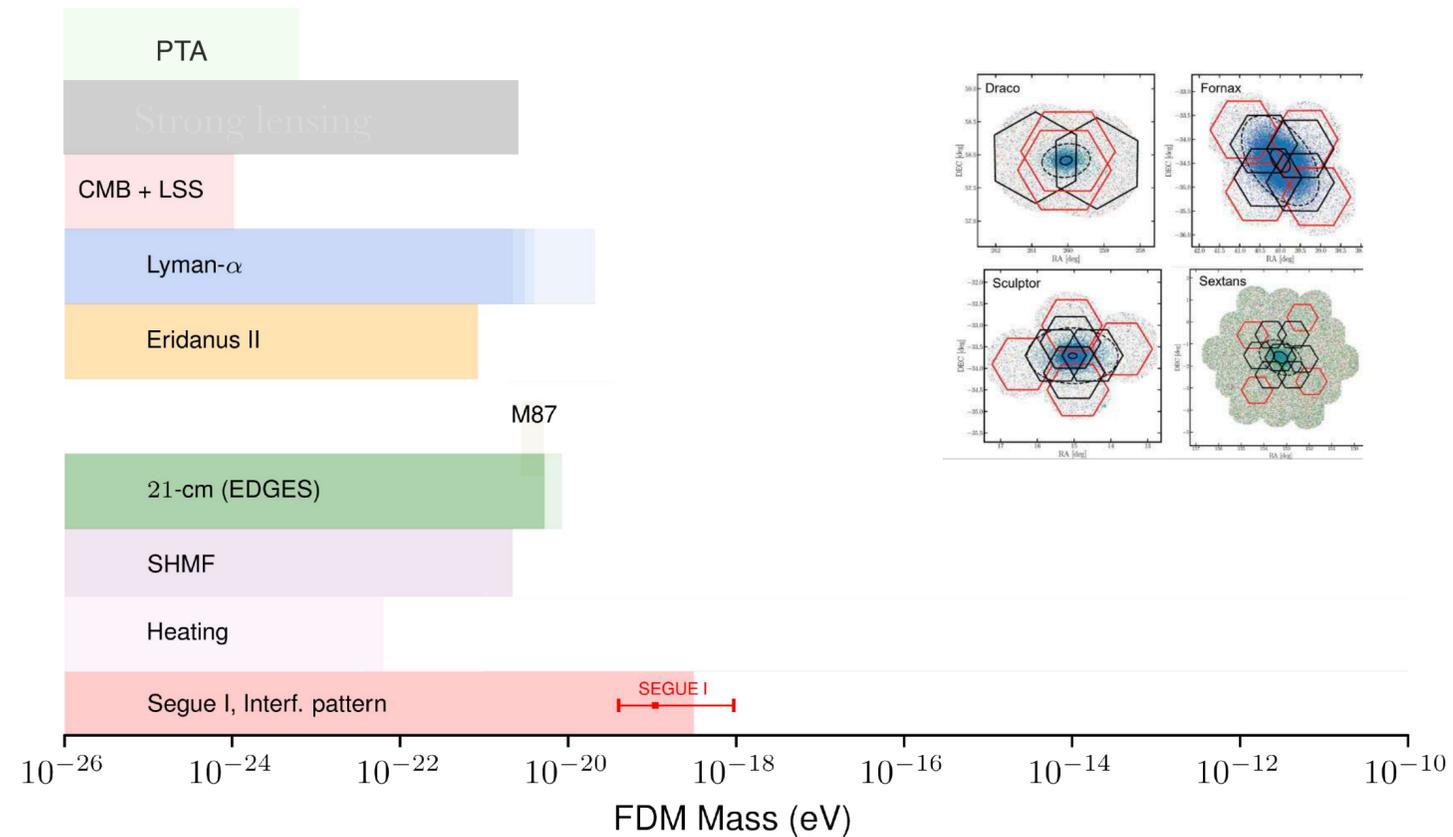
(Work in progress)



Shun'ichi
Horigome



Shin'ichiro
Ando



FDM mass from Ultra-faint dwarfs

- Stellar kinematic data from 18 UFDs + classical dwarfs to fit the **FDM** profile from simulations
- New analysis:
 - Improved modelling of FDM based on previous work and simulation from **our** group
 - Using environmental effects to put informed priors for Bayesian analysis the dwarfs quantities - SASHIMI

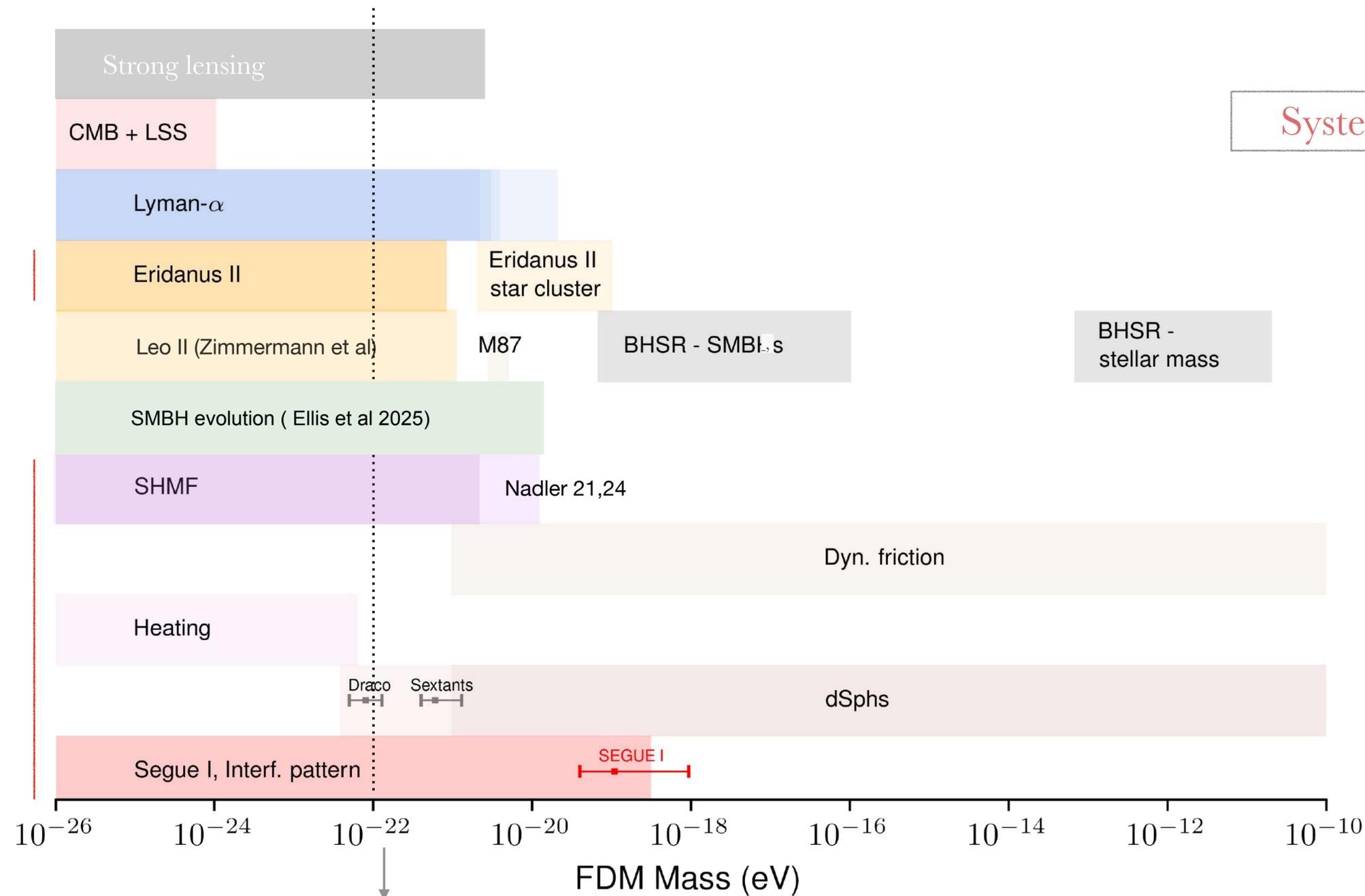


+ Improved **zoom in** simulations to understand sub-halo properties

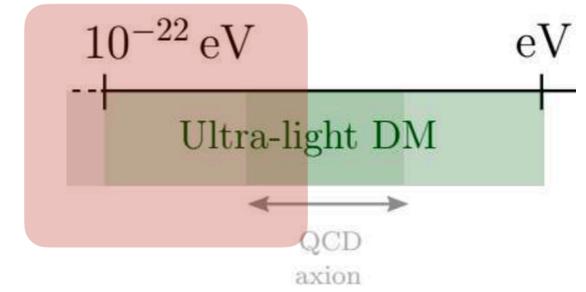
Result: more conservative and improved bounds

Current status

Fuzzy Dark Matter - bounds on the mass



Sweet spot for solving small scale problems



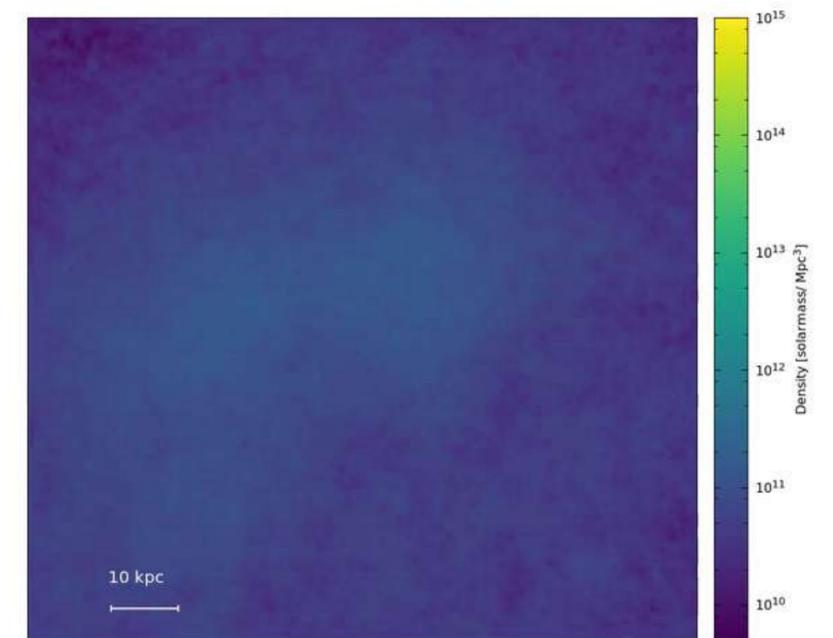
Systematics everywhere!

BUT: - systematic effects!!
- dynamics of FDM not fully understood.

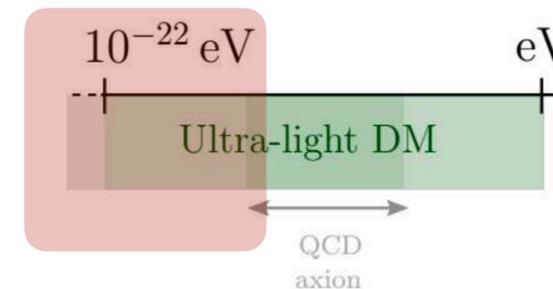
- Need:
- Observations
 - Improve sims
 - New observables
 - New probes

It is not because a bound is here that is correct!

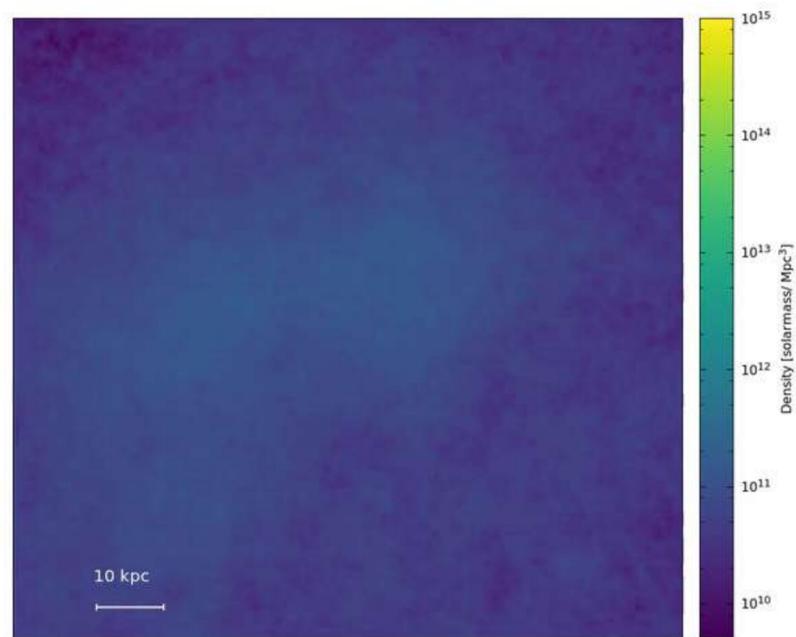
interference patterns



Interference pattern



- PROBES:
- Strong lensing
 - Stellar streams
 - Heating
 - Dynamical friction



Simulation by Jowett Chan

$\mathcal{O}(1)$ fluctuations in density $\rightarrow \sim \lambda_{dB}$

Heating

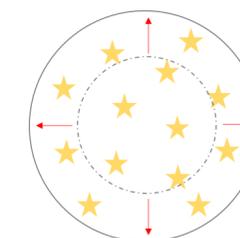
FDM granule



m_{eff}



System (star) gains energy



Friction

FDM granule



m_{eff}

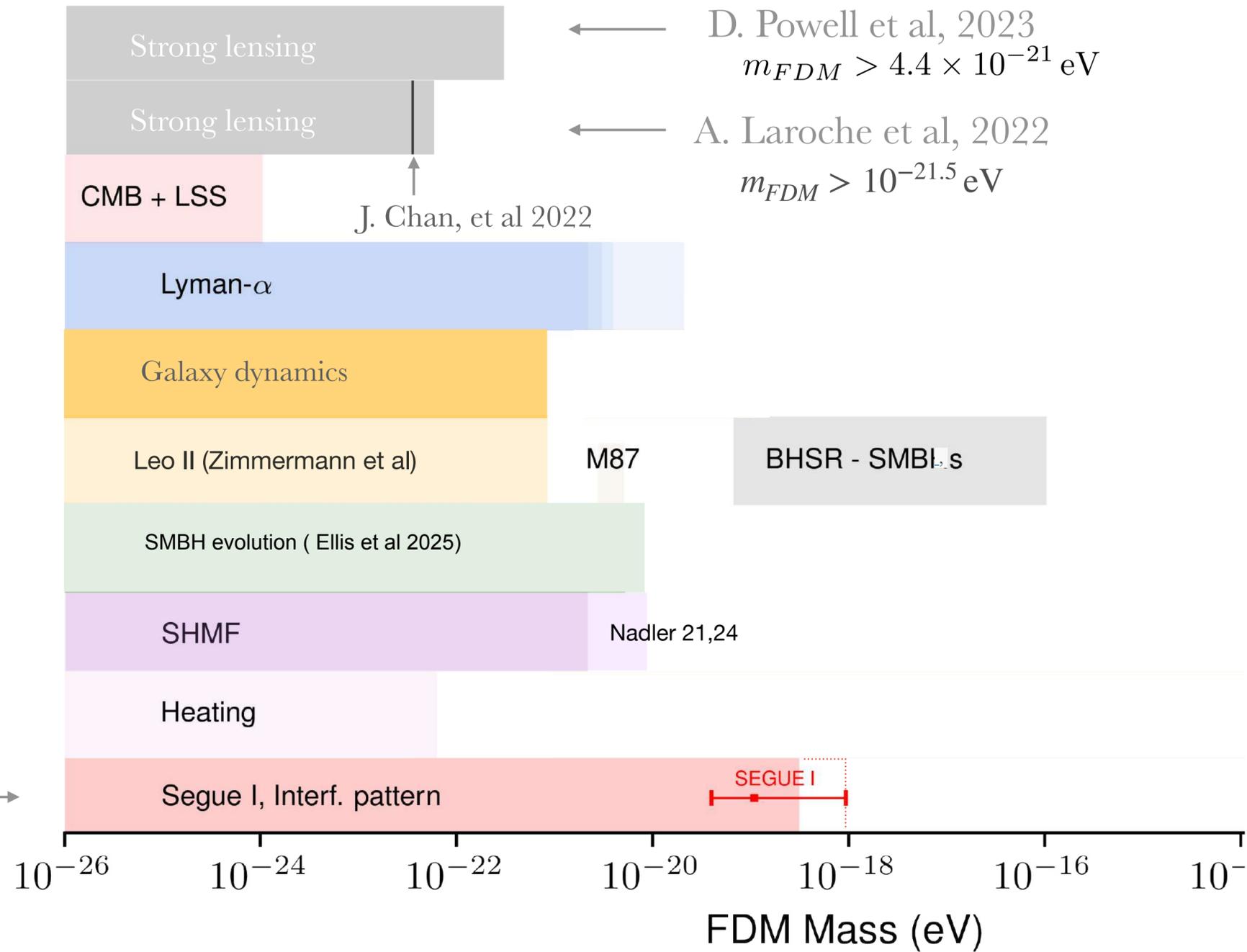
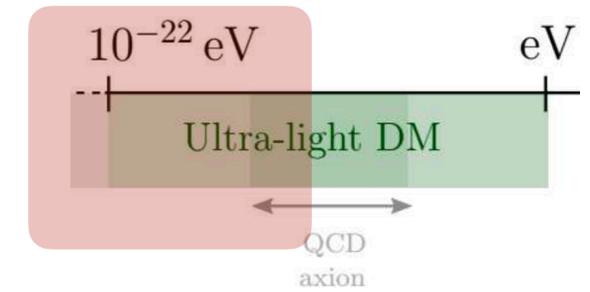


Globular cluster

System (GC or BH) loses energy

Interference patterns - granules

Strong lensing



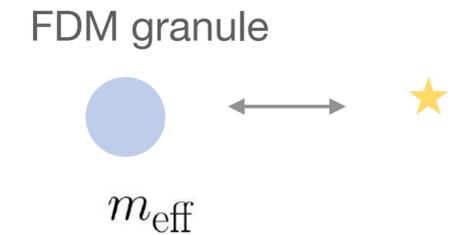
D. Powell et al, 2023
 $m_{FDM} > 4.4 \times 10^{-21}$ eV

A. Laroche et al, 2022
 $m_{FDM} > 10^{-21.5}$ eV

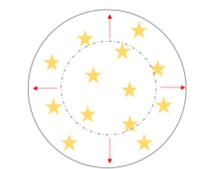
J. Chan, et al 2022

Stellar heating
Dalal et al, 2022
 $m_{FDM} > 3 \times 10^{-19}$ eV

Heating



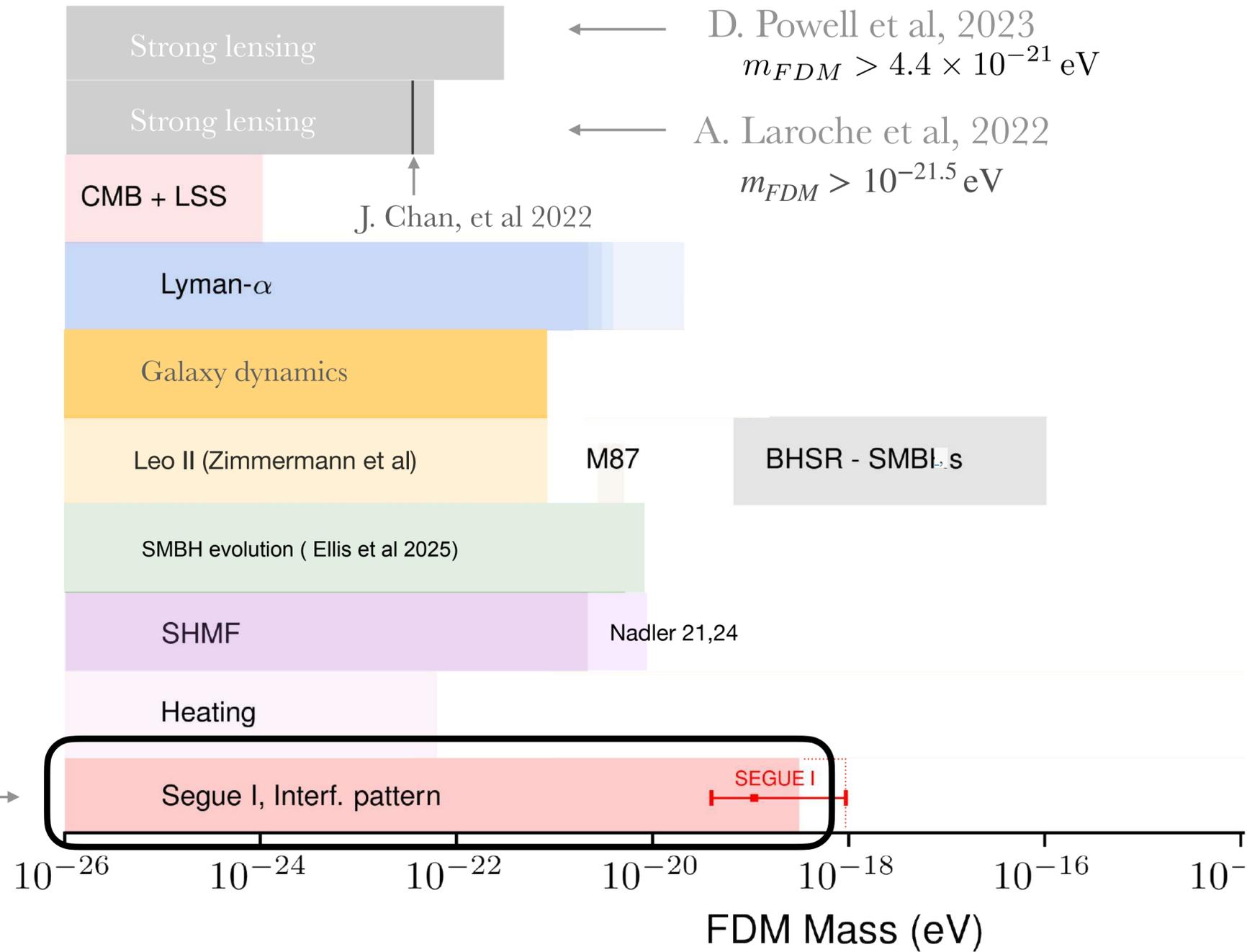
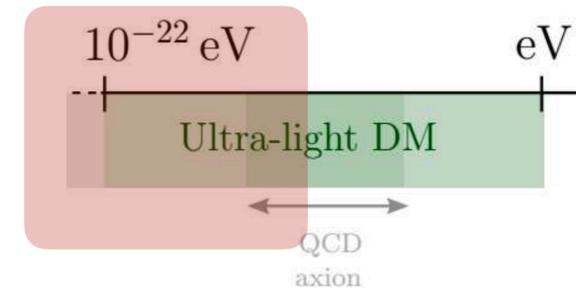
System (star) gains energy



See Peter Graham talk

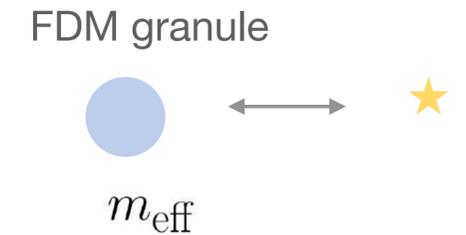
Interference patterns - granules

Strong lensing

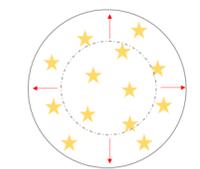


Stellar heating
Dalal et al, 2022
 $m_{FDM} > 3 \times 10^{-19} \text{ eV}$

Heating

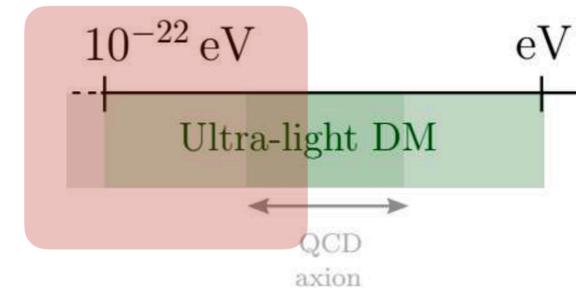


System (star) gains energy



See Peter Graham talk

Stellar heating - *ultra-faint dwarfs*



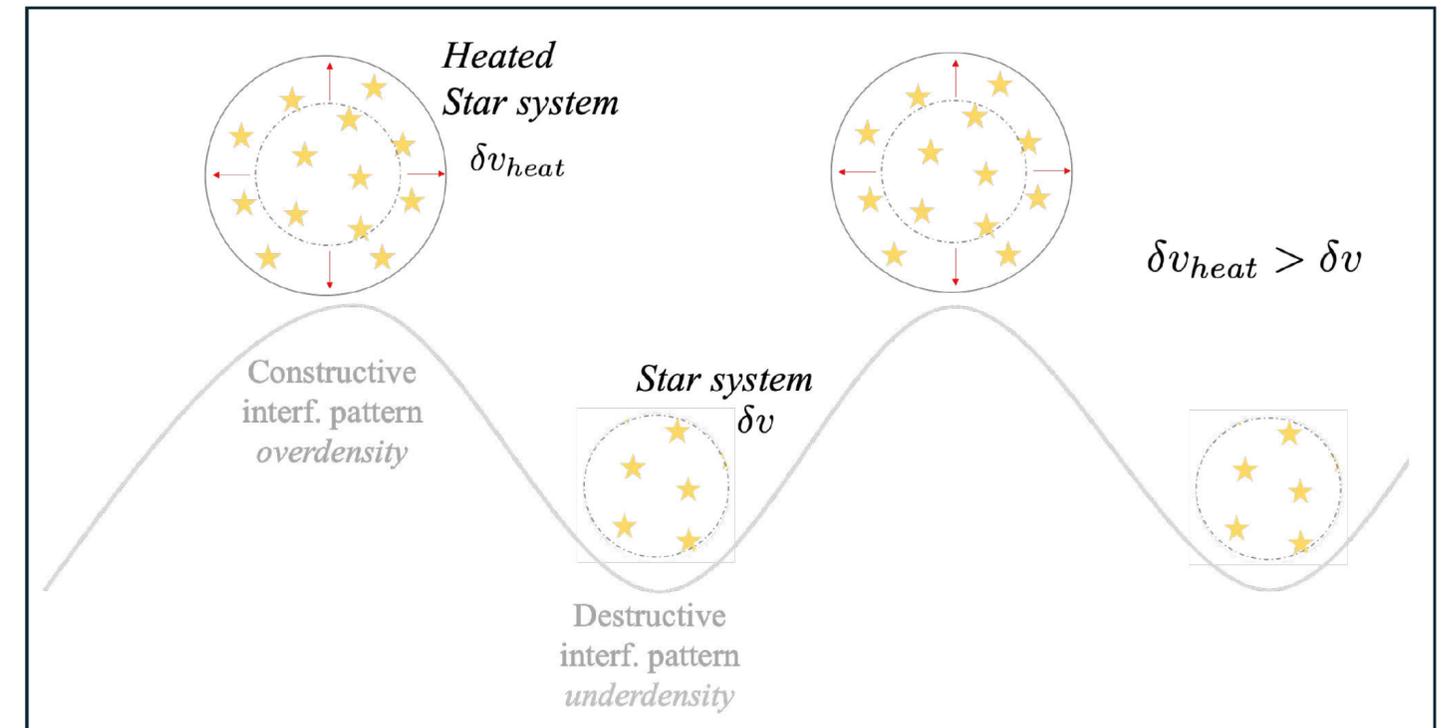
Dalal et al 2022

- Study stellar heating on UFD due to the presence of granules
- Track the half-light radius and stellar dispersion
- Compared with observations of Segue I and II

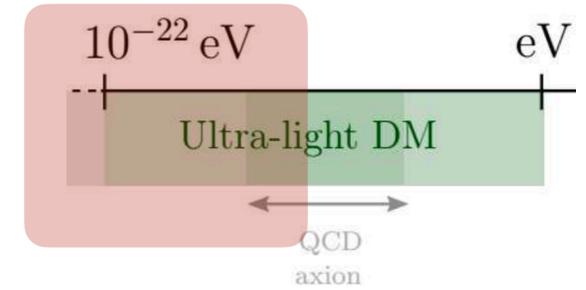
$$m > 3 \times 10^{-19} \text{ eV}$$

Details:

- Soliton excluded (authors claim conservative bounds)
- Tidally stripped halo? Alters the granules



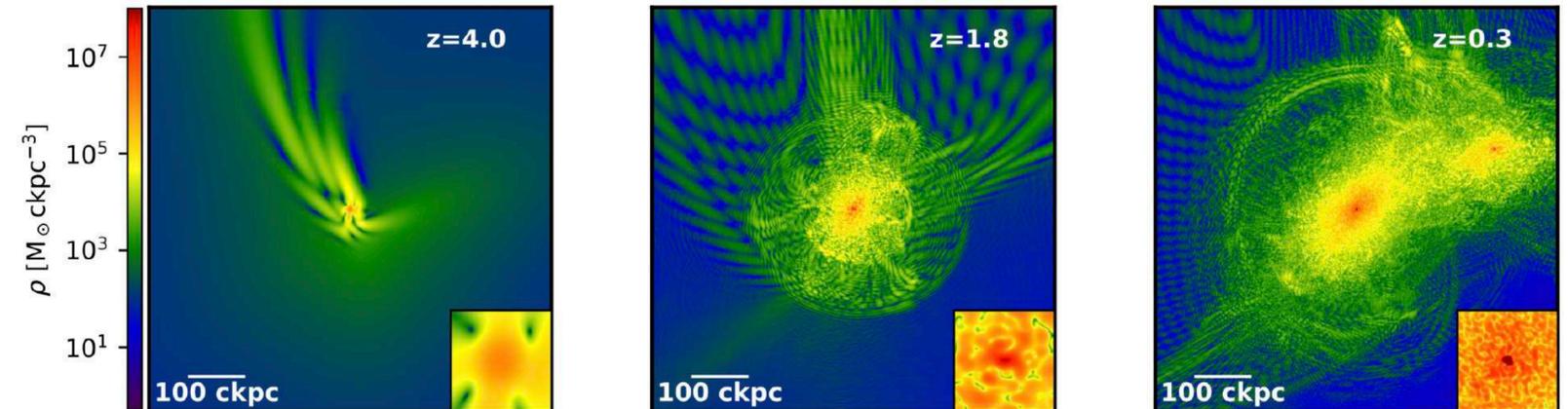
Stellar heating - *ultra-faint dwarfs*



Dalal et al 2022

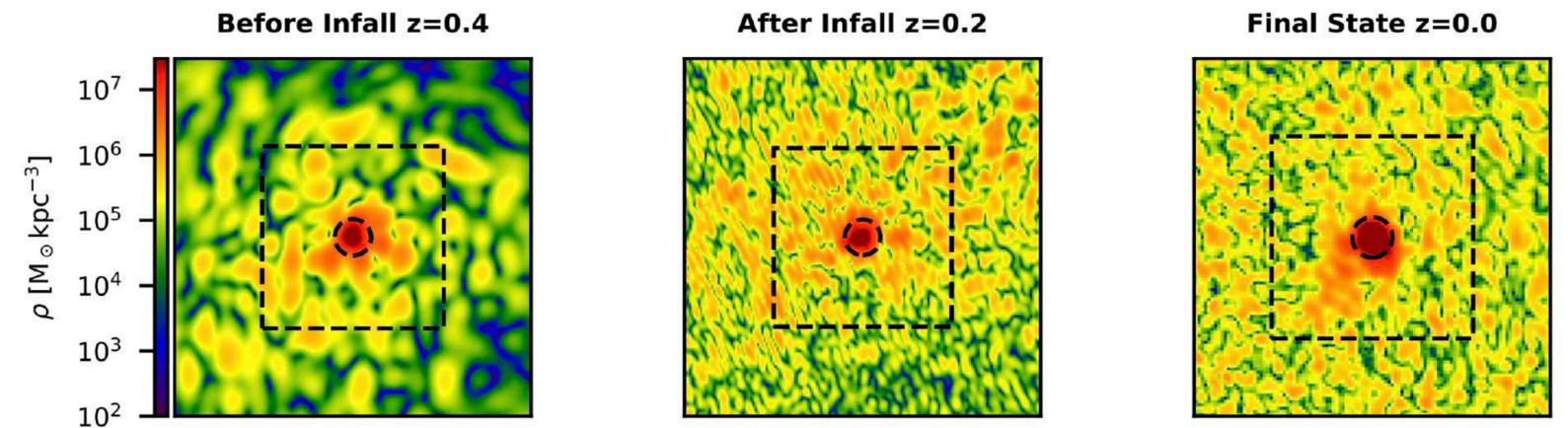
- Study stellar heating on UFD due to the presence of granules
- Track the half-light radius and stellar dispersion
- Compared with observations of Segue I and II

$$m > 3 \times 10^{-19} \text{ eV}$$



Details:

- Soliton excluded (authors claim conservative bounds)
- Tidally stripped halo? Alters the granules

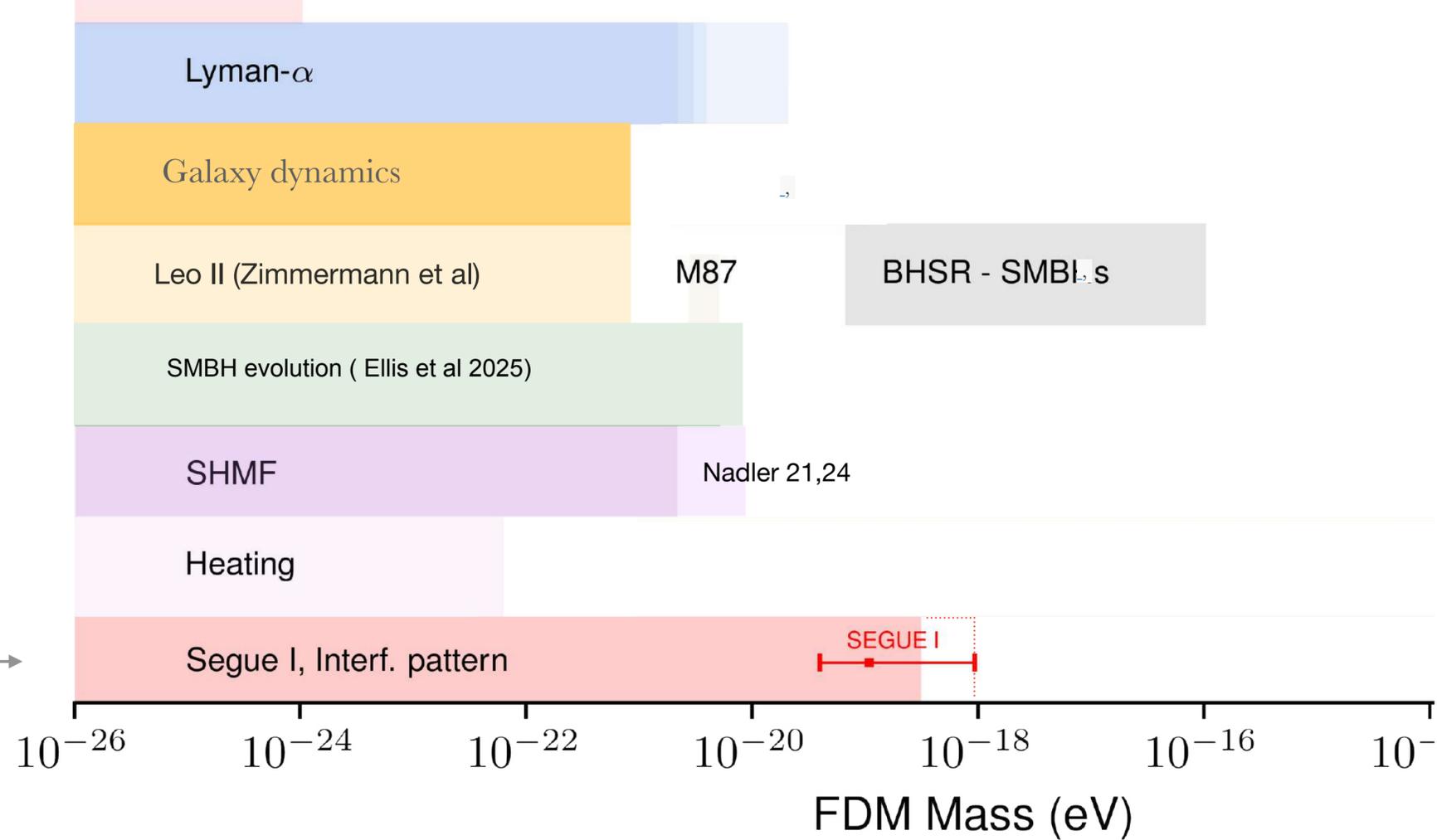
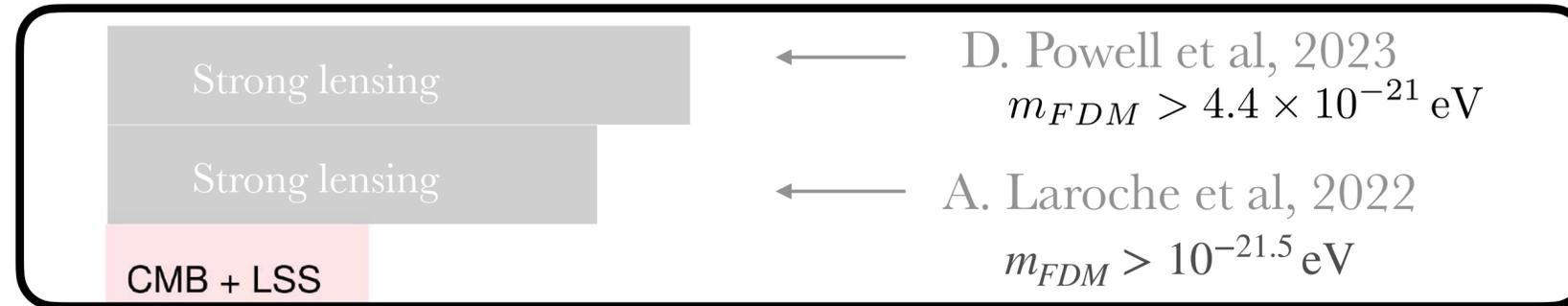
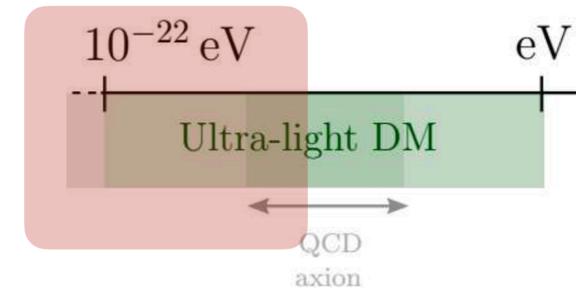


(In progress)

Jowett et al, 2024

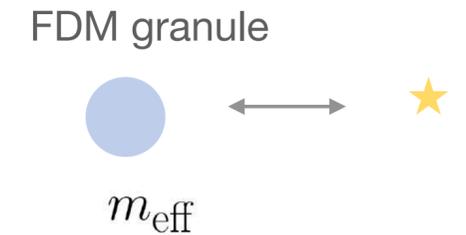
Interference patterns - granules

Strong lensing

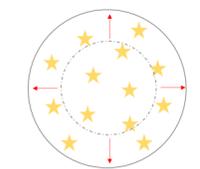


Stellar heating
 Dalal et al, 2022
 $m_{FDM} > 3 \times 10^{-19}$ eV

Heating



System (star) gains energy

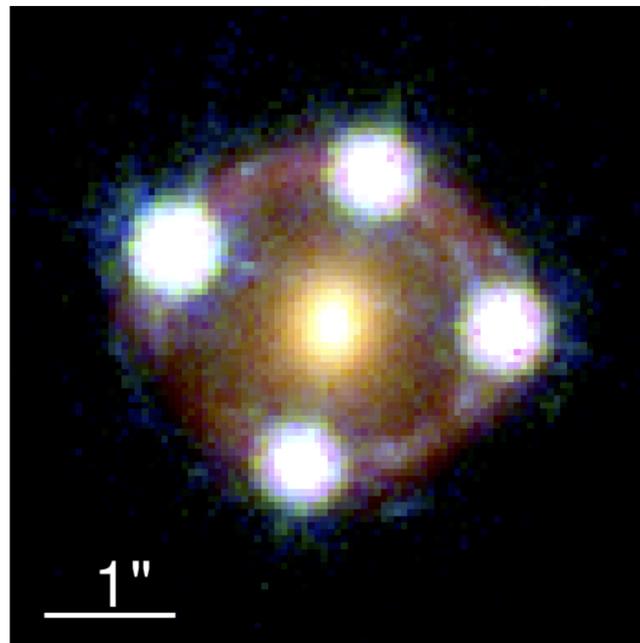


Strong *lensing*

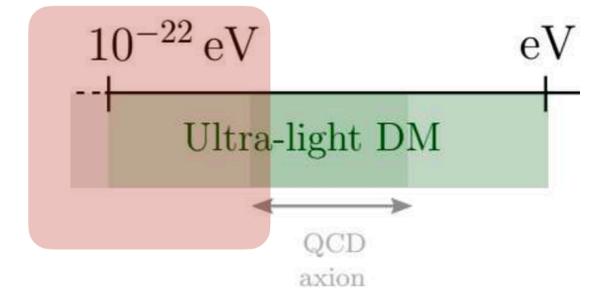
Strong lensing: sensitive to the mass distribution of the total matter in the lens system

Flux anomaly

Unresolved strong lensed system

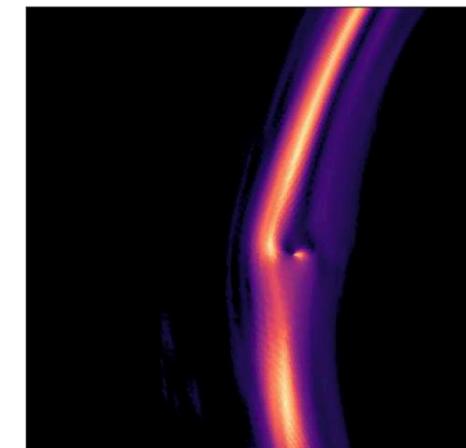
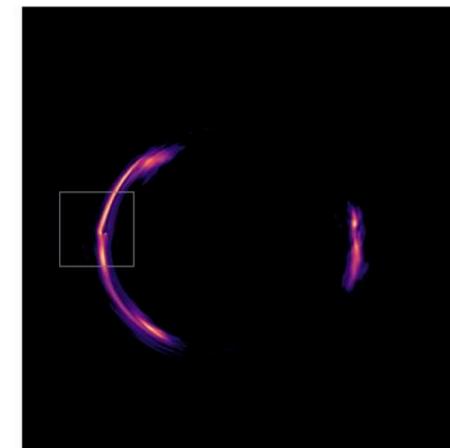
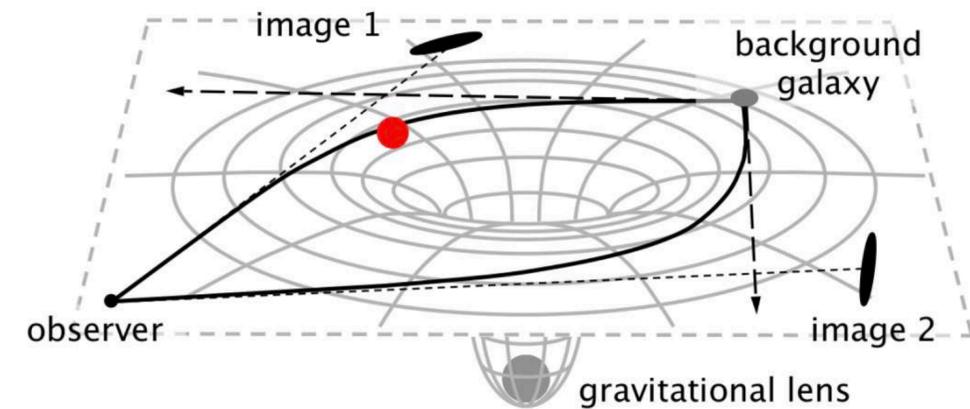


Any asymmetry in the structure in the lens, can break the symmetry that yielded the flux ratio predictions



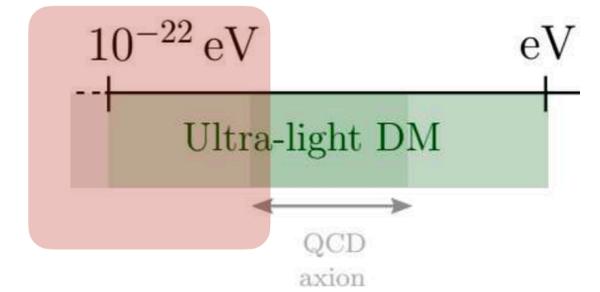
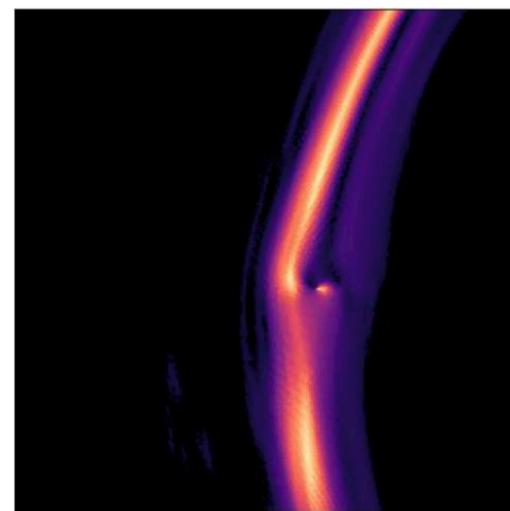
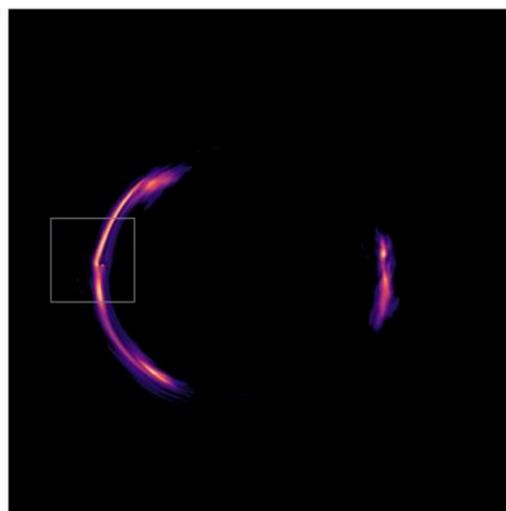
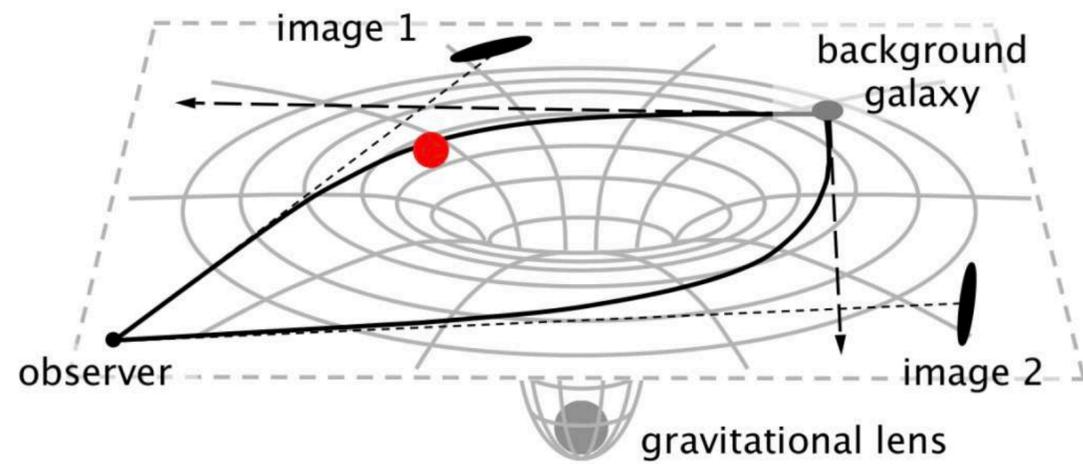
Resolved imaging

Resolved strong lensing from galaxy surface brightness



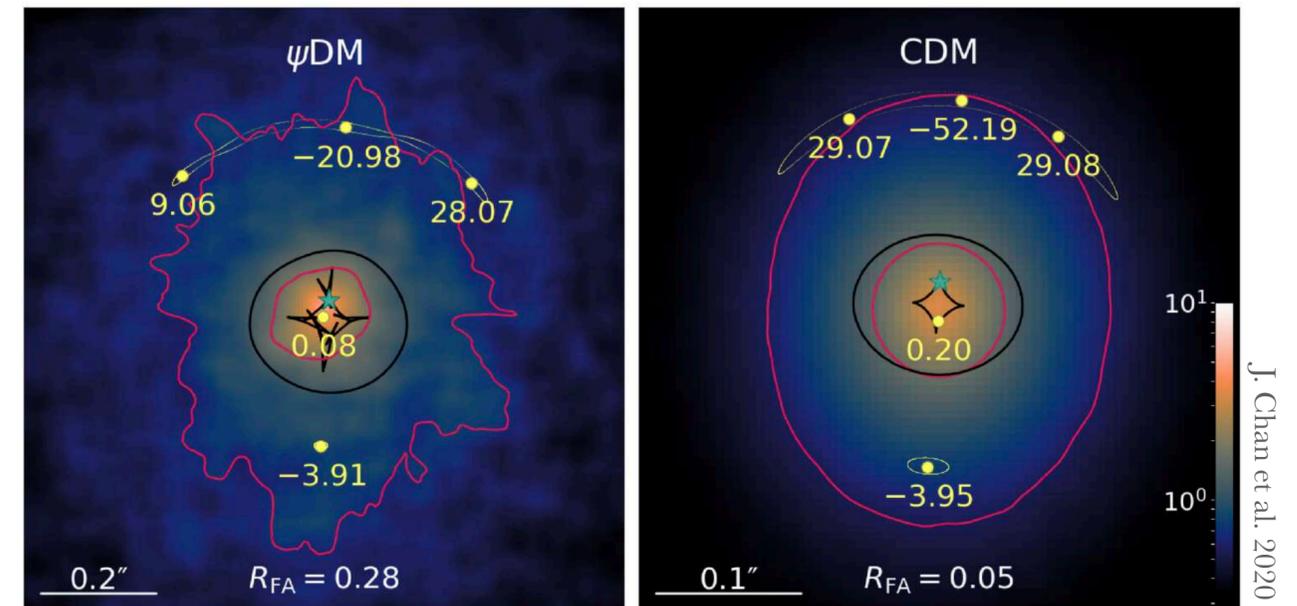
Strong *lensing*

Low mass perturber with lensing



Presence of granules

Surface densities overlaid with sources and quad images for fuzzy and smooth lenses

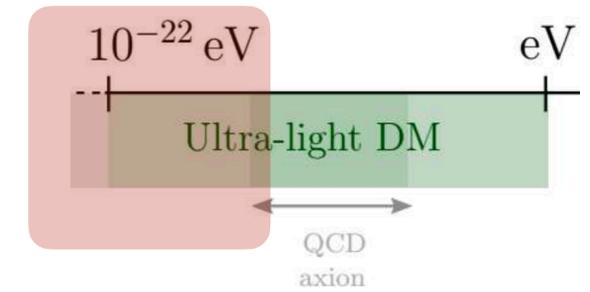


Fuzzy lens: fluctuating tangential critical curve; flux ratio anomalies also sizable.

Previous works:

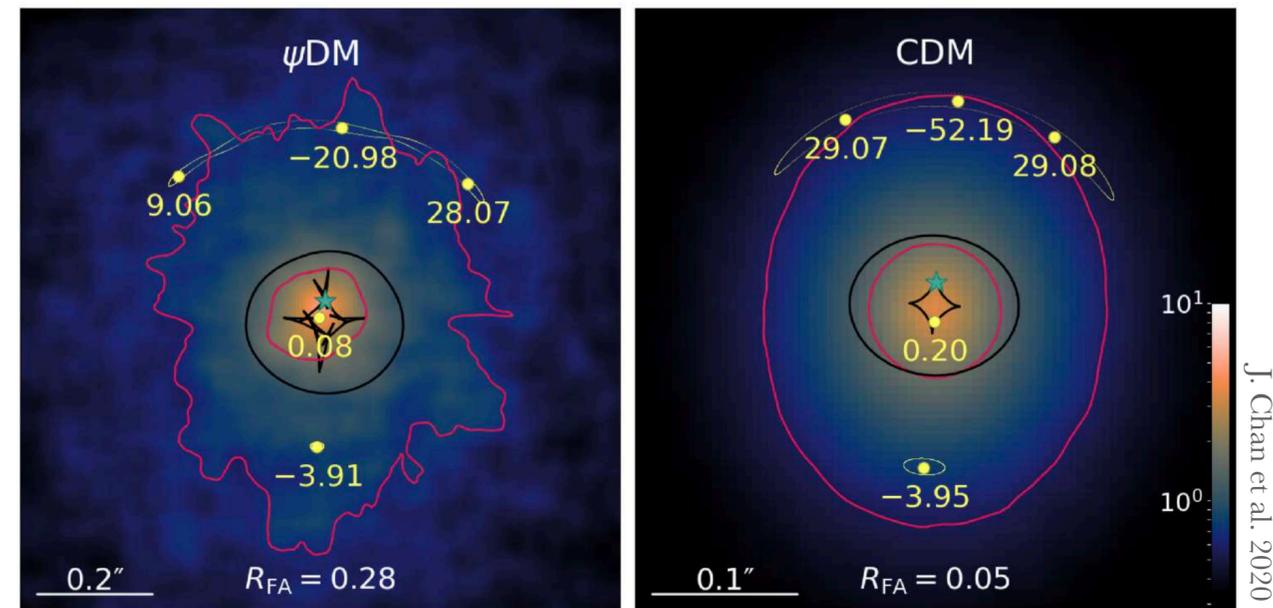
- J. Chan, H. Schive, S.g. Wong, T. Chiueh, T. Broadhurst, 2020
- A. Laroche, Daniel Gilman, X. Li, J. Bovy, X. Du, 2022

Strong lensing



Presence of granules

Surface densities overlaid with sources and quad images for fuzzy and smooth lenses



Fuzzy lens: fluctuating tangential critical curve; flux ratio anomalies also sizable.

Previous works:

J. Chan, H. Schive, S. g. Wong, T. Chiueh, T. Broadhurst, 2020

A. Laroche, Daniel Gilman, X. Li, J. Bovy, X. Du, 2022

Laroche et al

- 11 quadruply imaged quasars
- granularity arising from FDM can significantly affect flux ratios

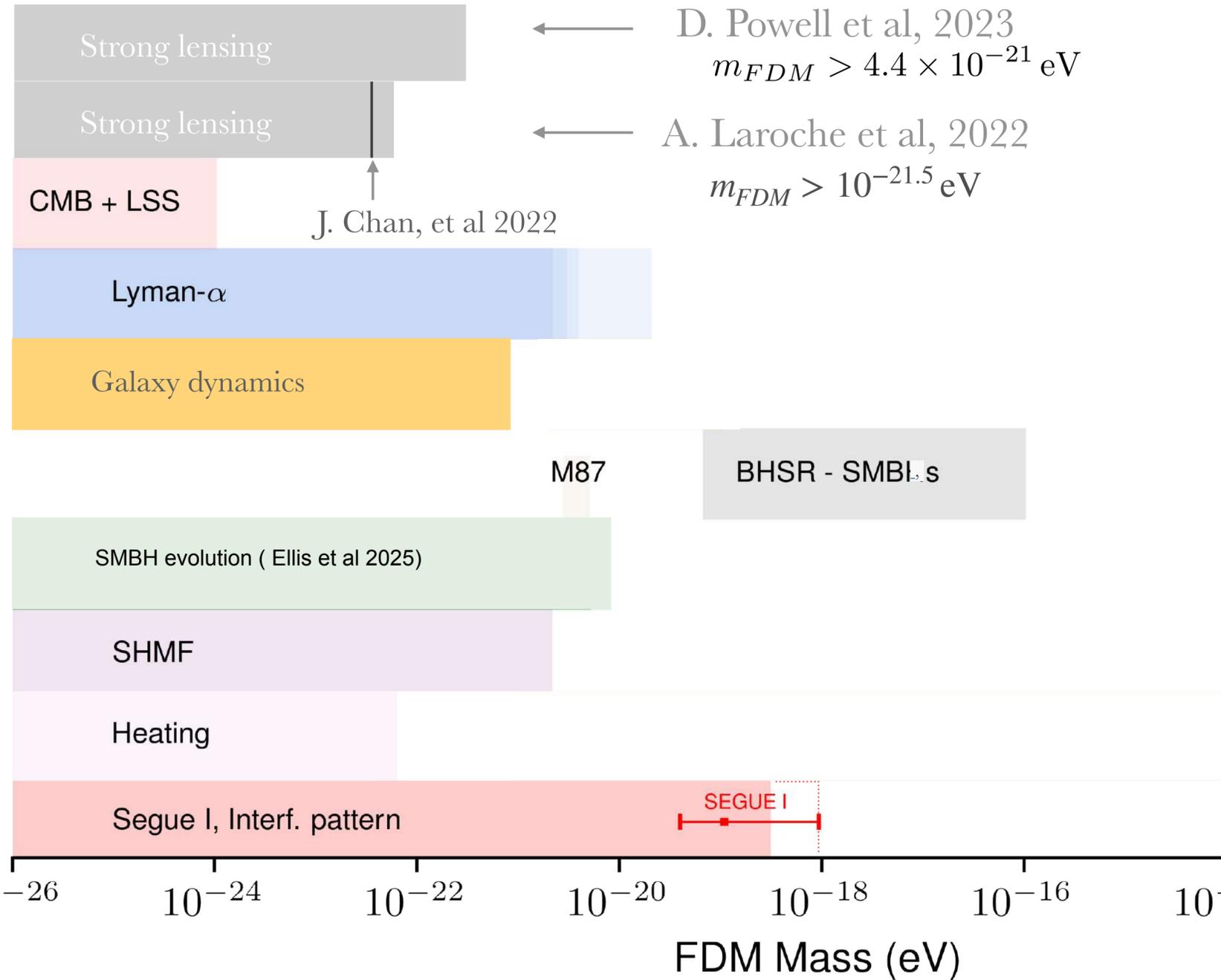
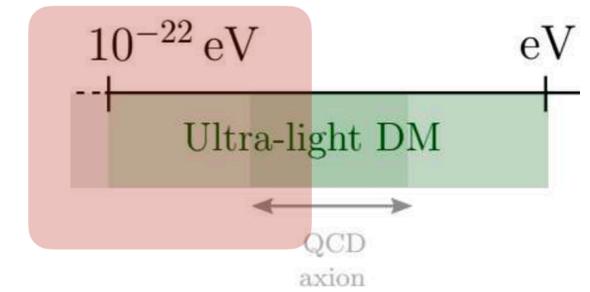
$$m_{FDM} > 10^{-21.5} \text{ eV}$$

Chan et al

- 11 quadruply imaged quasars
- quadruply lensed system HS 0810+2554
- successfully reproduce both the positions and fluxes of the observed images, including anomalies that CDM models fail to explain

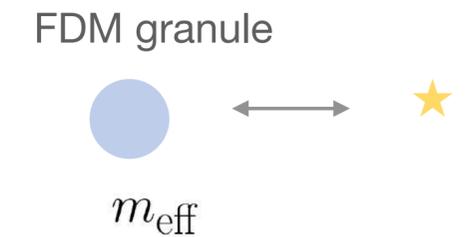
Interference patterns - granules

Strong lensing

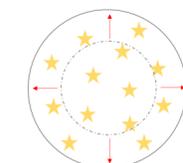


Stellar heating
Dalal et al, 2022
 $m_{FDM} > 3 \times 10^{-19} \text{ eV}$

Heating



System (star) gains energy



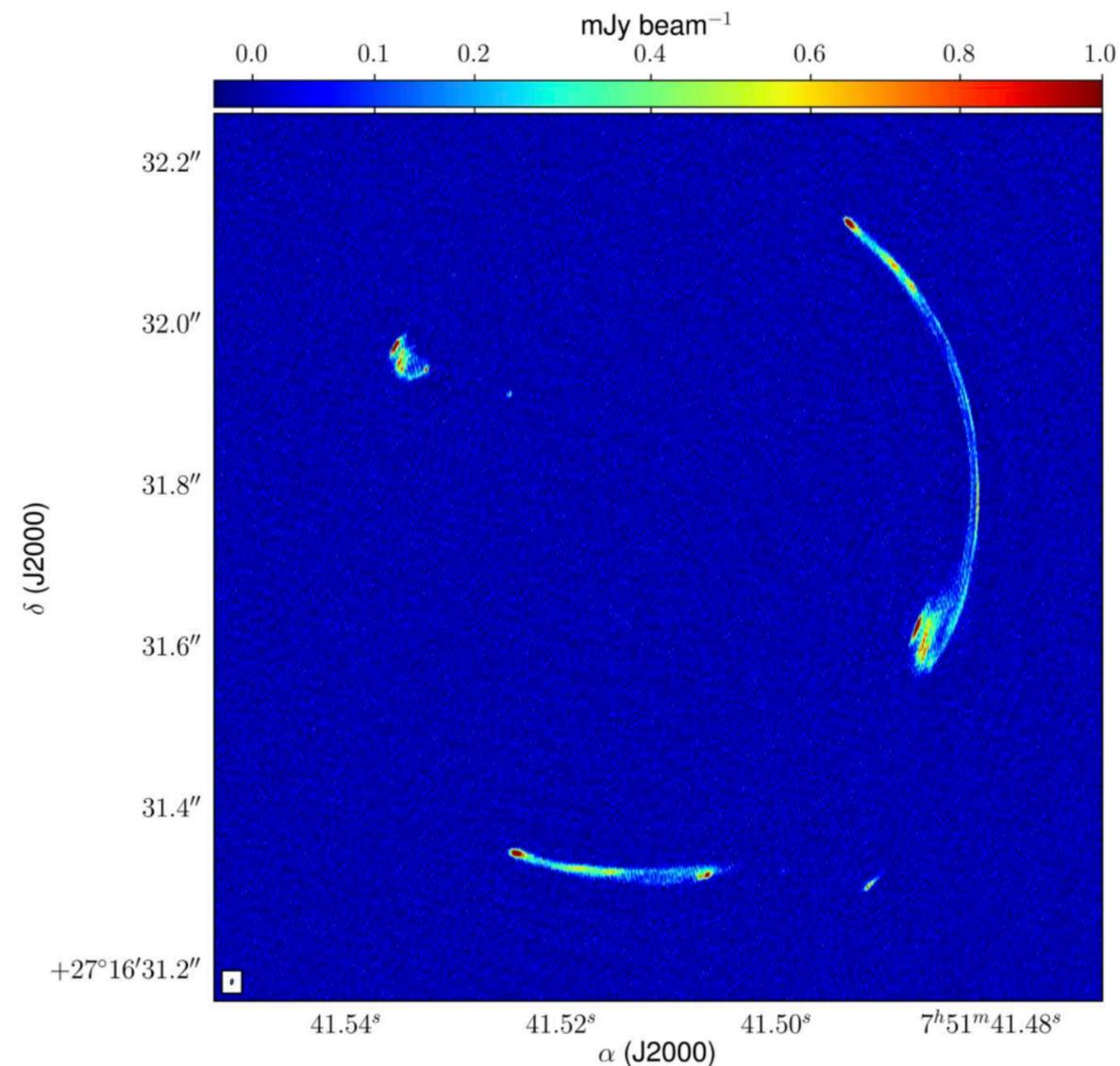
See Peter Graham talk

Strong *lensing*

A lensed radio jet at milli-arcsecond resolution II: Constraints on fuzzy dark matter from an extended gravitational arc

D. Powell, S. Vegetti, J.P. McKean, S. White, EF, S. May, C. Spingola

MG J0751+2716



- Lensed radio jet, observed with global VLBI
- First image of a lensed radio jet!
- Source structure allows us to “image” the lens surface density
- Extended lensed radio arcs and the milli-arcsecond resolution provide direct sensitivity to the presence of **FDM granules** in the halo of the lens galaxy

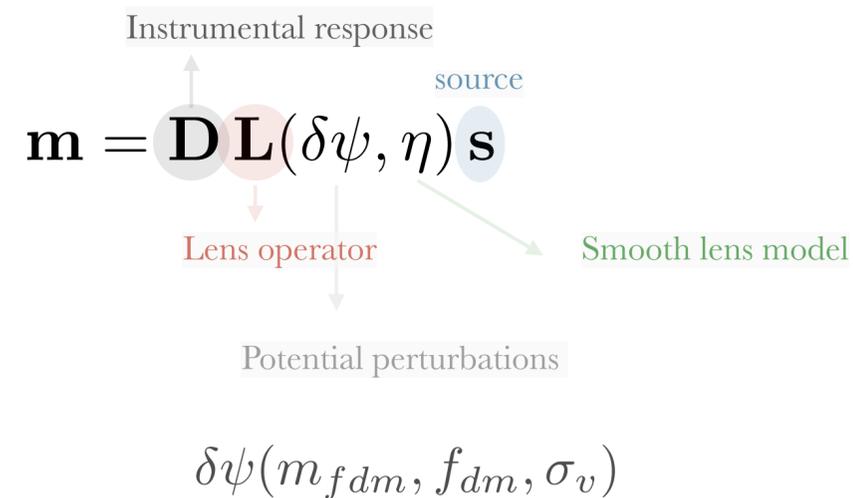
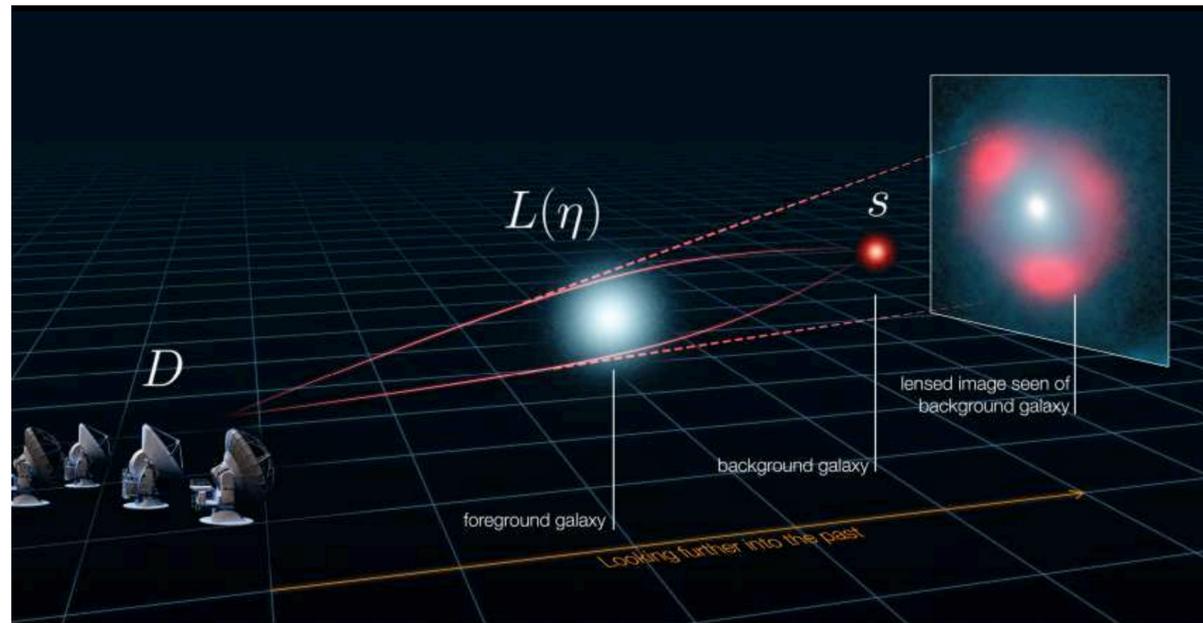
Bayesian approach to jointly inferring the lens mass model and source surface brightness distribution

Data taken at 1.6 GHz using global very long baseline interferometry (VLBI) with an angular resolution, measured as the full width at half maximum (FWHM) of the main lobe of the dirty beam response, of $5.5 \times 1.8 \text{ mas}^2$

(Suyu et al. 2006; Vegetti & Koopmans 2009; Hezaveh et al. 2016; Rizzo et al. 2018)

Strong lensing

Forward modelling



A lensed radio jet at milli-arcsecond resolution II: Constraints on fuzzy dark matter from an extended gravitational arc

D. Powell, S. Vegetti, J.P. McKean, S. White, EF, S. May, C. Spingola

Smooth lensing model: from Powell et al 2022

FDM granules:

Model by Chan et al 2020: statistics of spatially-varying surface mass density fluctuations, given the density profile of the dark matter, as well as some basic assumptions on the behavior of scalar fields in a potential well

$\delta\psi(m_{fdm}, f_{dm}, \sigma_v)$ - is the perturbation of the lensing potential - fluctuations in the projected surface mass density written as perturbations in the lensing convergence due to the presence of the **granules**:

$$\langle \delta\kappa^2 \rangle = \frac{\lambda_{db}}{2\sqrt{\pi}\Sigma_c^2} \int_{los} \rho_{DM}^2 dl$$



We wish to infer a posterior distribution on the dark matter particle mass $\mathcal{P}(m_{fdm})$

We compute likelihoods for 10^4 sample FDM lens realizations with m_{fdm} drawn from the log-uniform prior range $\log(m_{fdm}/\text{eV}) \in [-21.5, -19.0]$.

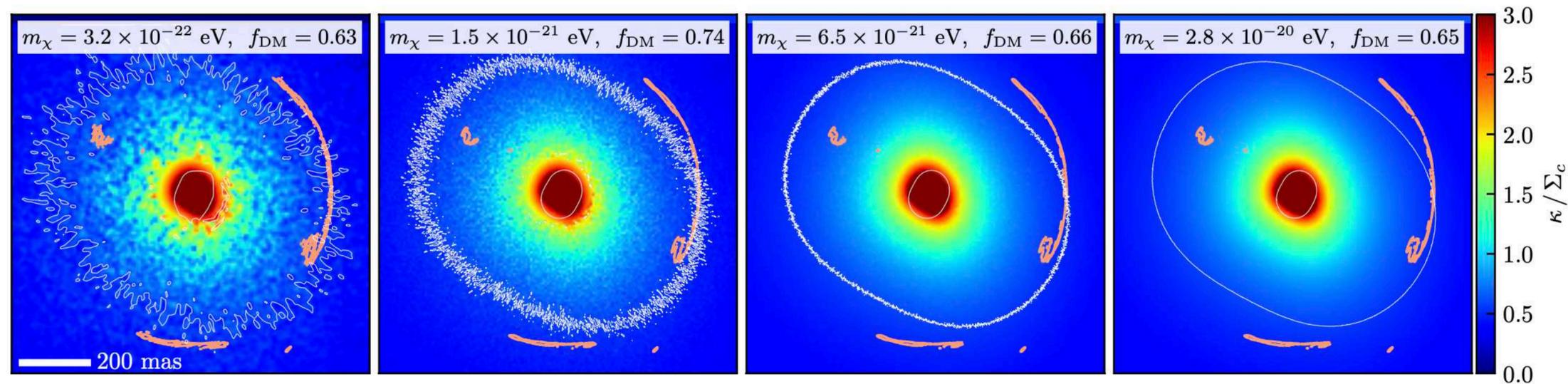
Free parameters: $\{m, f_{DM, \sigma_v, \eta}, \lambda_s\}$

Strong *lensing*

A lensed radio jet at milli-arcsecond resolution II: Constraints on fuzzy dark matter from an extended gravitational arc

D. Powell, S. Vegetti, J.P. McKean, S. White, EF, S. May, C. Spingola

Example convergence maps with corresponding MAP surface mass density maps (κ , in units of the critical density Σ_c) reconstruction for 4 random realizations of MG J0751+2716 in an FDM cosmology - the model lensed images in orange contours



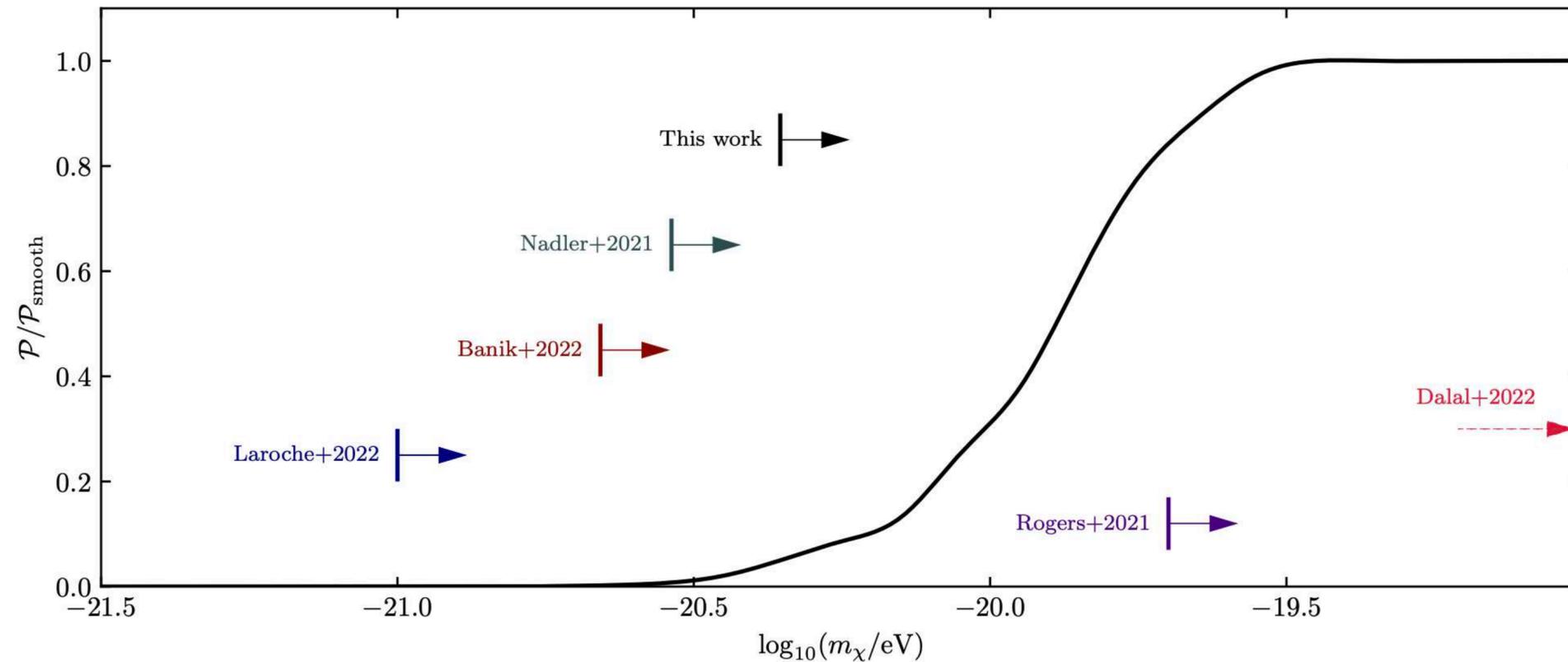
The lensing effect of the FDM granules is apparent: The critical curves wiggle back and forth across the lensed arcs, which would require the presence of multiple images of the same region of the source along the arc.

Strong lensing

A lensed radio jet at milli-arcsecond resolution II: Constraints on fuzzy dark matter from an extended gravitational arc

D. Powell, S. Vegetti, J.P. McKean, S. White, EF, S. May, C. Spingola

Results quoted in terms of posterior odds ratio (POR) between FDM with a particle mass m_{fdm} and the smooth model, $\mathcal{P}/\mathcal{P}_{smooth}$



Fuzzy dark matter
(Single spin-0 particle)

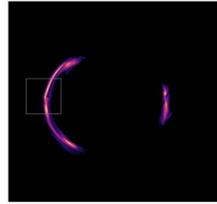
$$m_{fdm} > 4.4 \times 10^{-21} \text{ eV}$$

Vector fuzzy dark matter
(spin-1 particle)
OR 3 same mass FDM

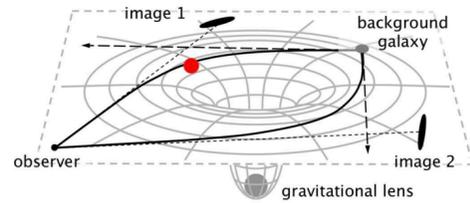
$$m_{vdm} > 1.4 \times 10^{-21} \text{ eV}$$

Spin-2 FDM

$$m_{spin-2} > 8.8 \times 10^{-22} \text{ eV}$$



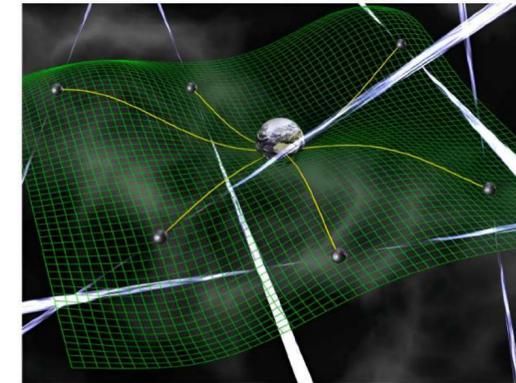
Strong lensing



axion-photon coupling

$$m \sim 10^{-[22-17]} \text{ eV}$$

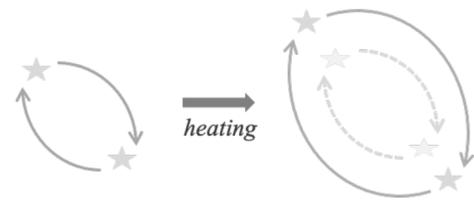
Pulsar Timing Array



Artistic representation of the Pulsar Timing Array concept. Credit: David Champion / MPIfR

$$m \sim 10^{-[22-17]} \text{ eV}$$

Binary stars



$$m \sim 10^{-[16-10]} \text{ eV}$$



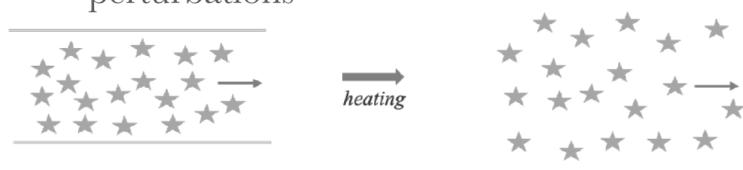
Wave interference

Mass, spin (# particles), fraction self interaction

Stellar streams



Heating + coherent perturbations



$$m \sim 10^{-[23-18]} \text{ eV}$$

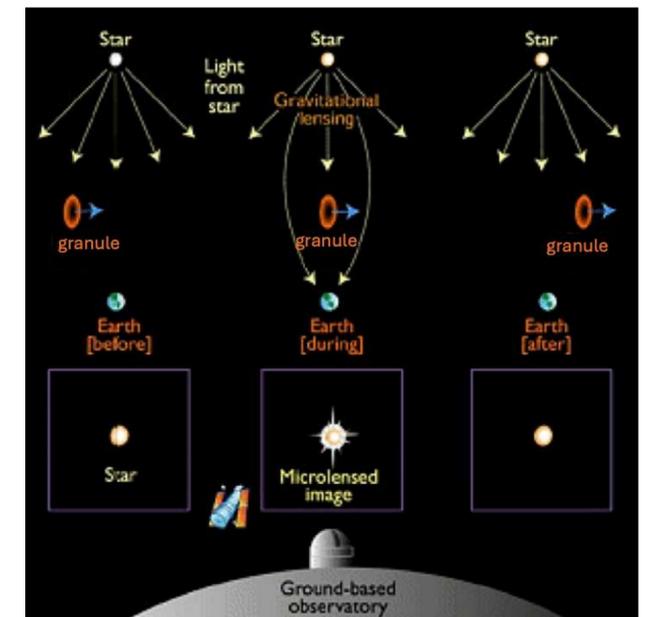
Solar system



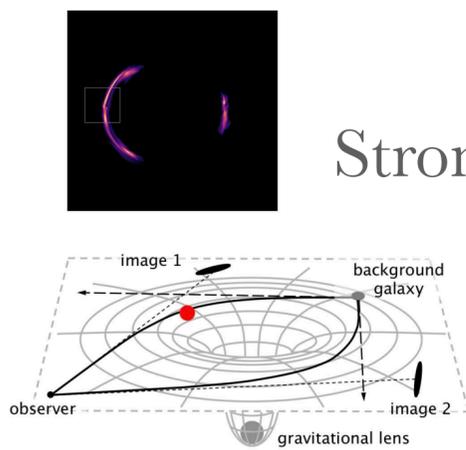
$$m \sim 10^{-[16-10]} \text{ eV}$$

axion-photon coupling

Stochastic lensing



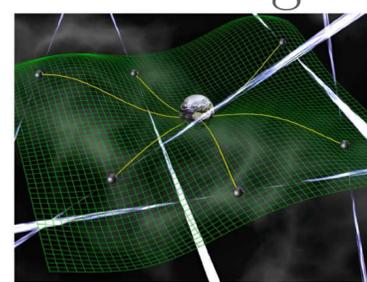
$$m \sim 10^{-[23-18]} \text{ eV}$$



Strong lensing

$m \sim 10^{-[22-17]} \text{ eV}$

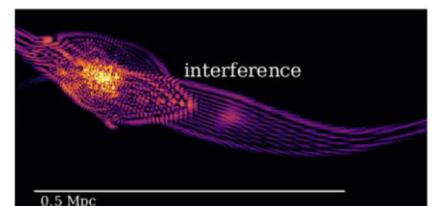
Pulsar Timing Array



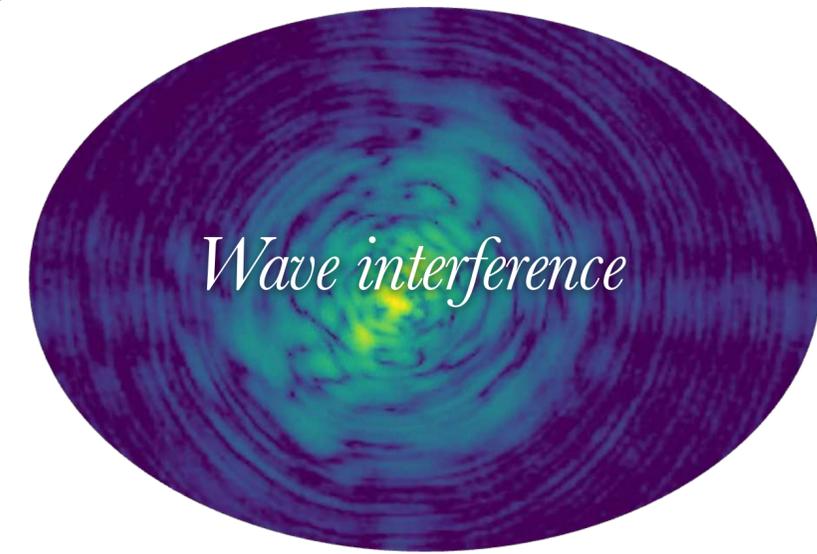
Artistic representation of the Pulsar Timing Array concept. Credit: David Champion / MPIFR

$m \sim 10^{-[22-17]} \text{ eV}$

Filaments



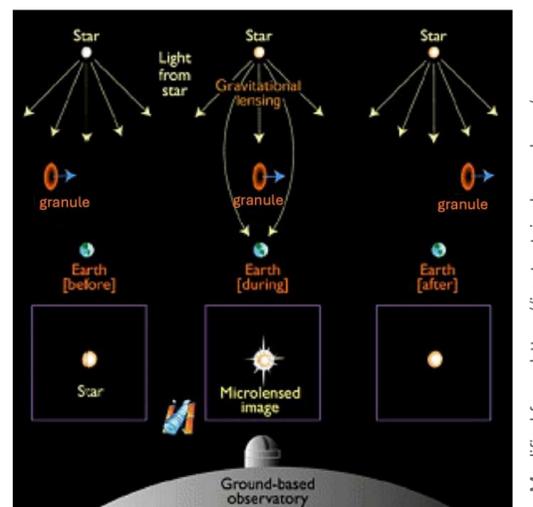
Cosmic filament spin from DM vortices
S. Alexander, C. Capanelli, **EF**, E. McDonough, 2022



Wave interference

*Mass, spin (# particles), fraction self interaction
axion-photon coupling*

Stochastic lensing



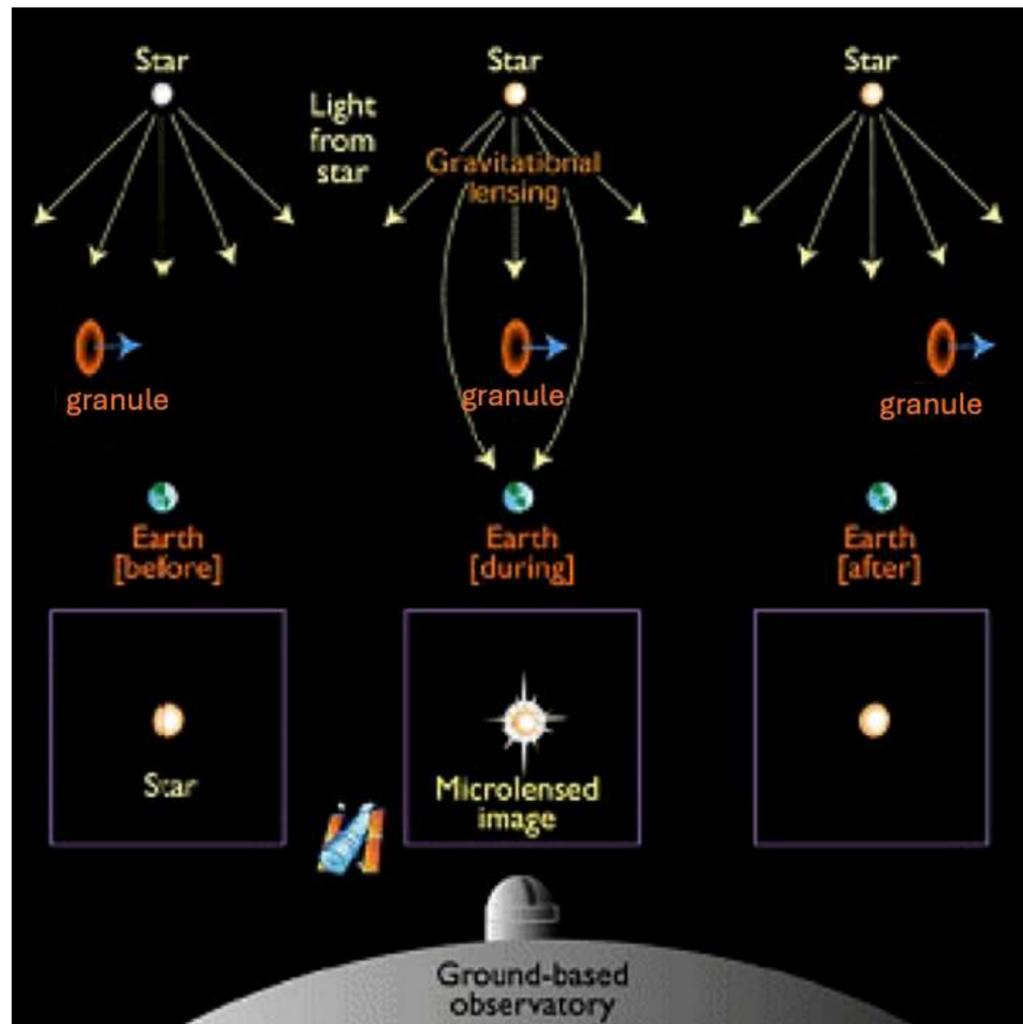
*Modified from: <https://i.astro.tsinghua.edu.cn/>
<https://i.astro.tsinghua.edu.cn/~shh88/contents/microlens.html>*

$m \sim 10^{-[23-18]} \text{ eV}$

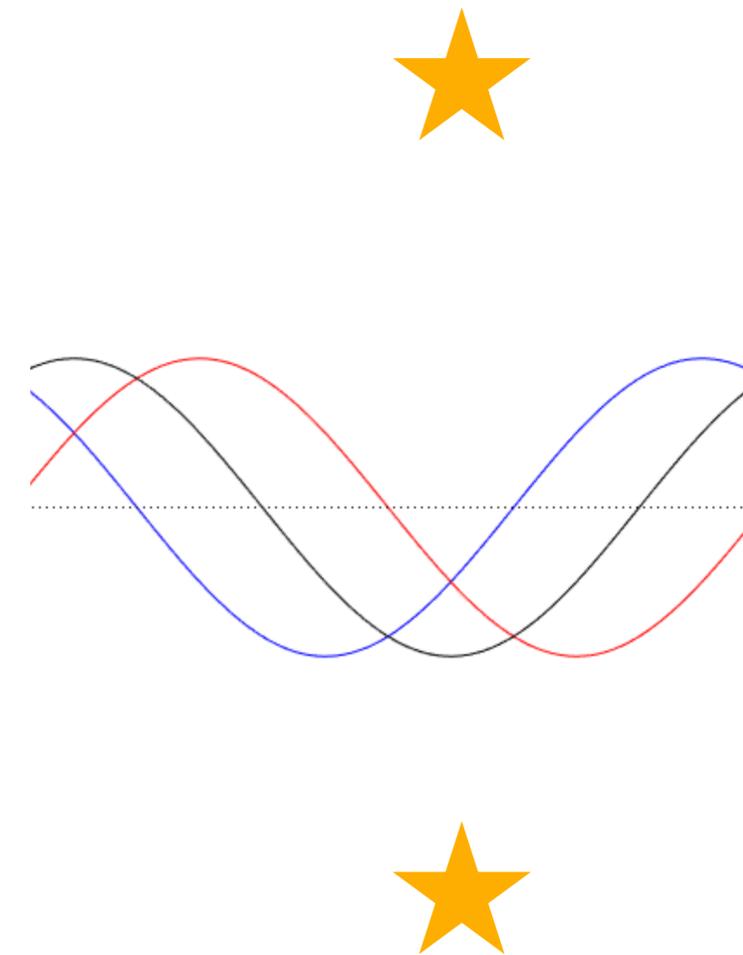
Stochastic lensing

Stochastic lensing of stars by ultralight dark matter halos, A. Eberhardt, **EF**, W. Luo, S. Lin, Y. Li, 2025

Microensing



Stochastic lensing



Every source in the galaxy will flicker with a period given by the mass

$$\tau_{\text{db}} = 2\pi\hbar/m\sigma^2 \sim 30 \left(\frac{10^{-17} \text{ eV}}{m} \right) \left(\frac{200 \text{ km/s}}{\sigma} \right)^2 \text{ yrs,} \quad \text{BUT, very small!}$$

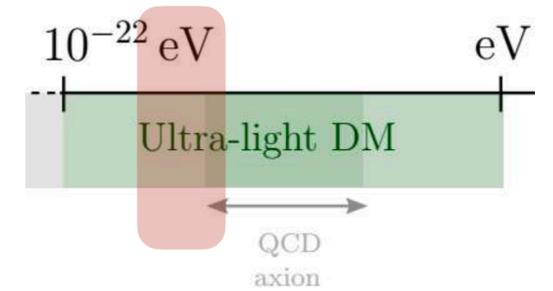
Stochastic lensing

Andrew Eberhardt, Wentao Lui, Yin Li
and Shurui Lin, 2025

ULDM

$$\lambda_{\text{db}} = \hbar/m\sigma \sim 6 \times 10^{-6} \left(\frac{10^{-17} \text{ eV}}{m} \right) \left(\frac{200 \text{ km/s}}{\sigma} \right) \text{ kpc}.$$

$$\tau_{\text{db}} = 2\pi\hbar/m\sigma^2 \sim 30 \left(\frac{10^{-17} \text{ eV}}{m} \right) \left(\frac{200 \text{ km/s}}{\sigma} \right)^2 \text{ yrs},$$



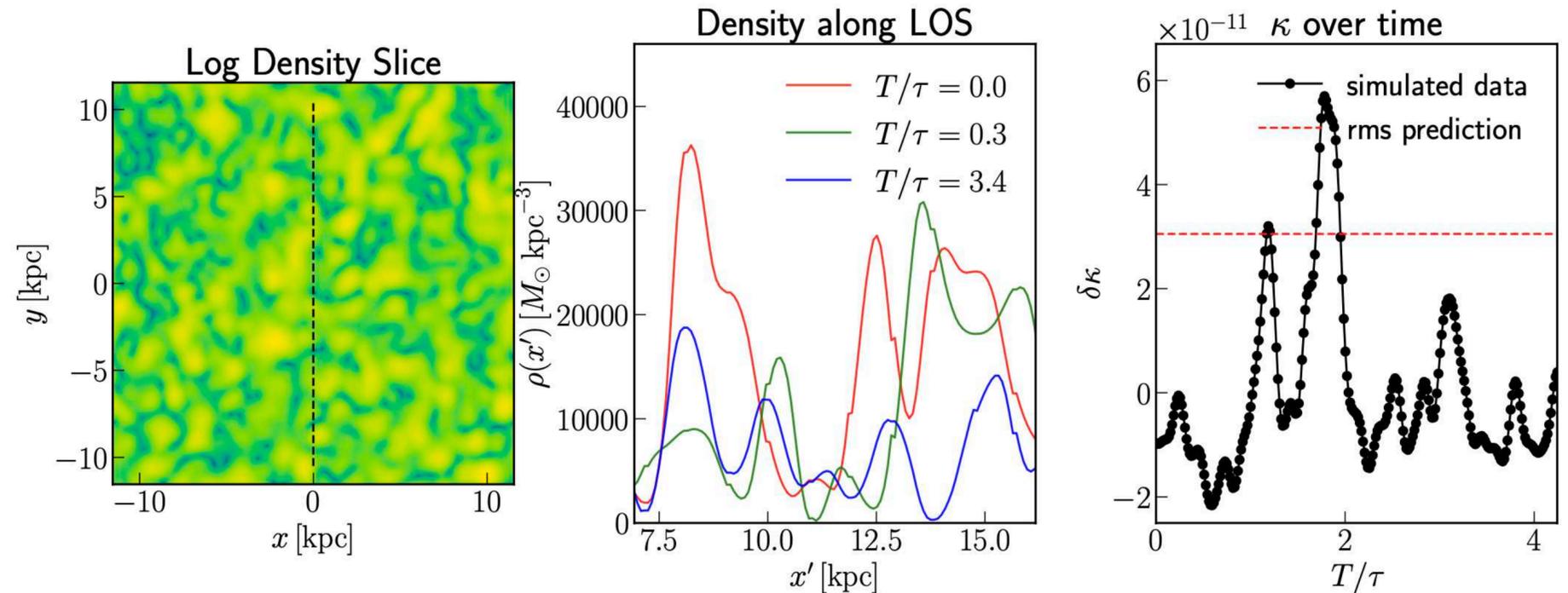
Lensing

Lensing convergence:

$$\delta\kappa_{\text{gr}} = \frac{4\pi G}{c^2} \int_0^D dx \frac{x(D-x)}{D} \delta\rho(x)$$

observer at the origin and source a distance D away along the line of sight

$\rho - \rho_{sm}$



We approximate the dark matter granules as a Gaussian random field with correlation length equal to the de Broglie wavelength, $\lambda = \hbar/m\sigma$, and expectation and variance given

$$\langle \delta\rho \rangle = 0 \text{ and } \langle \delta\rho^2 \rangle = \rho_{sm}^2$$

$$\delta\kappa_{\text{rms}}^{\text{gr}} \sim 3 \times 10^{-12} \left(\frac{m}{10^{-17} \text{ eV}} \right)^{-1/2} \left(\frac{\sigma}{200 \text{ km/s}} \right)^{-1/2} \left(\frac{\rho}{10^7 \text{ M}_\odot/\text{kpc}^3} \right) \left(\frac{D}{\text{kpc}} \right)^{3/4}$$

Stochastic lensing

Andrew Eberhardt, Wentao Lui, Yin Li
and Shurui Lin, 2025

ULDM

$$\lambda_{\text{db}} = \hbar/m\sigma \sim 6 \times 10^{-6} \left(\frac{10^{-17} \text{ eV}}{m} \right) \left(\frac{200 \text{ km/s}}{\sigma} \right) \text{ kpc}.$$

$$\tau_{\text{db}} = 2\pi\hbar/m\sigma^2 \sim 30 \left(\frac{10^{-17} \text{ eV}}{m} \right) \left(\frac{200 \text{ km/s}}{\sigma} \right)^2 \text{ yrs},$$

Lensing

Lensing convergence:

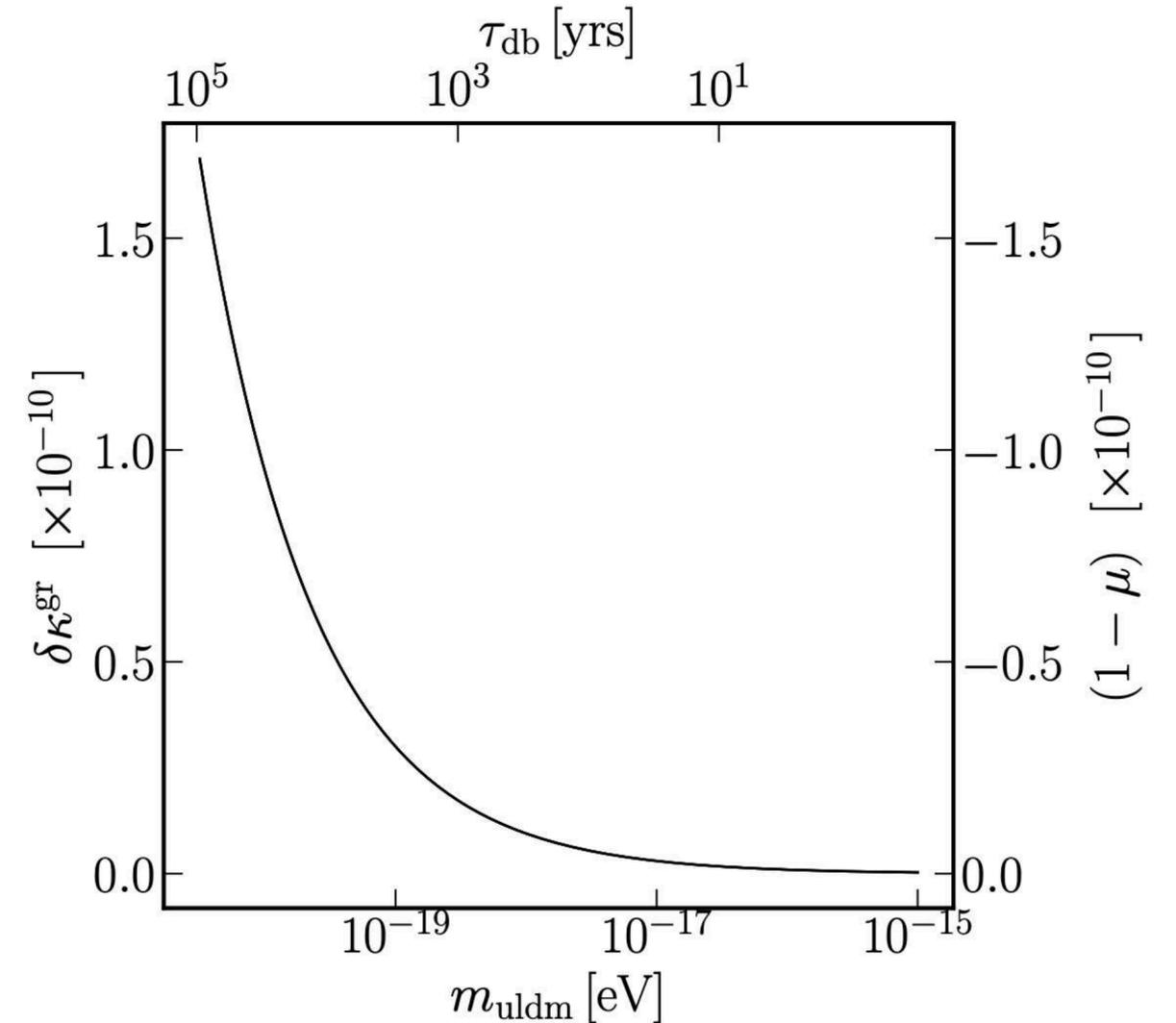
observer at the origin and source a
distance D away along the line of sight

$$\delta\kappa_{\text{gr}} = \frac{4\pi G}{c^2} \int_0^D dx \frac{x(D-x)}{D} \delta\rho(x)$$

$\rho - \rho_{sm}$

We approximate the dark matter granules as a Gaussian random field with correlation length equal to the de Broglie wavelength, $\lambda = \hbar/m\sigma$, and expectation and variance given

$$\langle \delta\rho \rangle = 0 \text{ and } \langle \delta\rho^2 \rangle = \rho_{sm}^2$$



$$\delta\kappa_{\text{rms}}^{\text{gr}} \sim 3 \times 10^{-12} \left(\frac{m}{10^{-17} \text{ eV}} \right)^{-1/2} \left(\frac{\sigma}{200 \text{ km/s}} \right)^{-1/2} \left(\frac{\rho}{10^7 \text{ M}_{\odot}/\text{kpc}^3} \right) \left(\frac{D}{\text{kpc}} \right)^{3/4}$$

Stochastic lensing

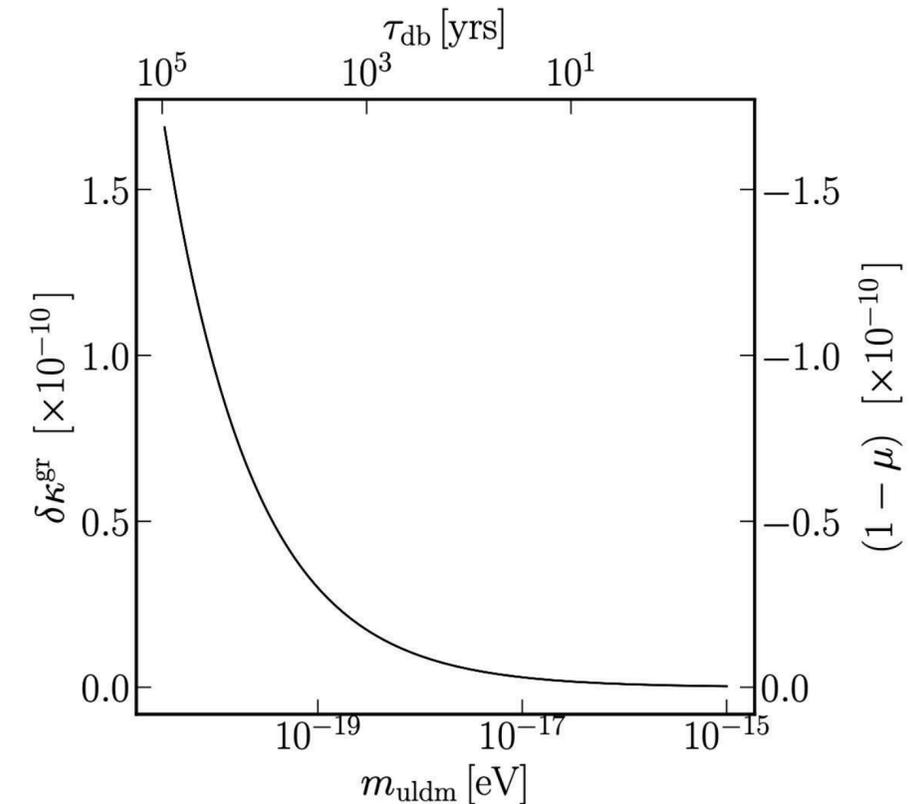
Andrew Eberhardt, Wentao Lui, Yin Li
and Shurui Lin, 2025

Lensing

observer at the origin and source a
distance D away along the line of sight

$$\delta\kappa_{\text{gr}} = \frac{4\pi G}{c^2} \int_0^D dx \frac{x(D-x)}{D} \delta\rho(x)$$

$\rho - \rho_{sm}$



Observational effect

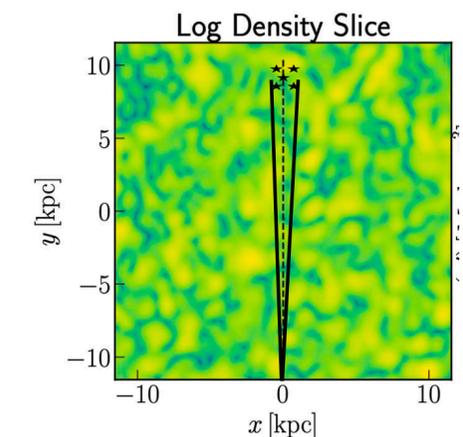
Every source in the galaxy will flicker with a period given by the mass

$$\tau_{\text{db}} = 2\pi\hbar/m\sigma^2 \sim 30 \left(\frac{10^{-17} \text{ eV}}{m} \right) \left(\frac{200 \text{ km/s}}{\sigma} \right)^2 \text{ yrs},$$

Objects to use?

Ex.: globular cluster, star, ...

(Work in progress)
FRB diffraction
W/ Ue-li Pen



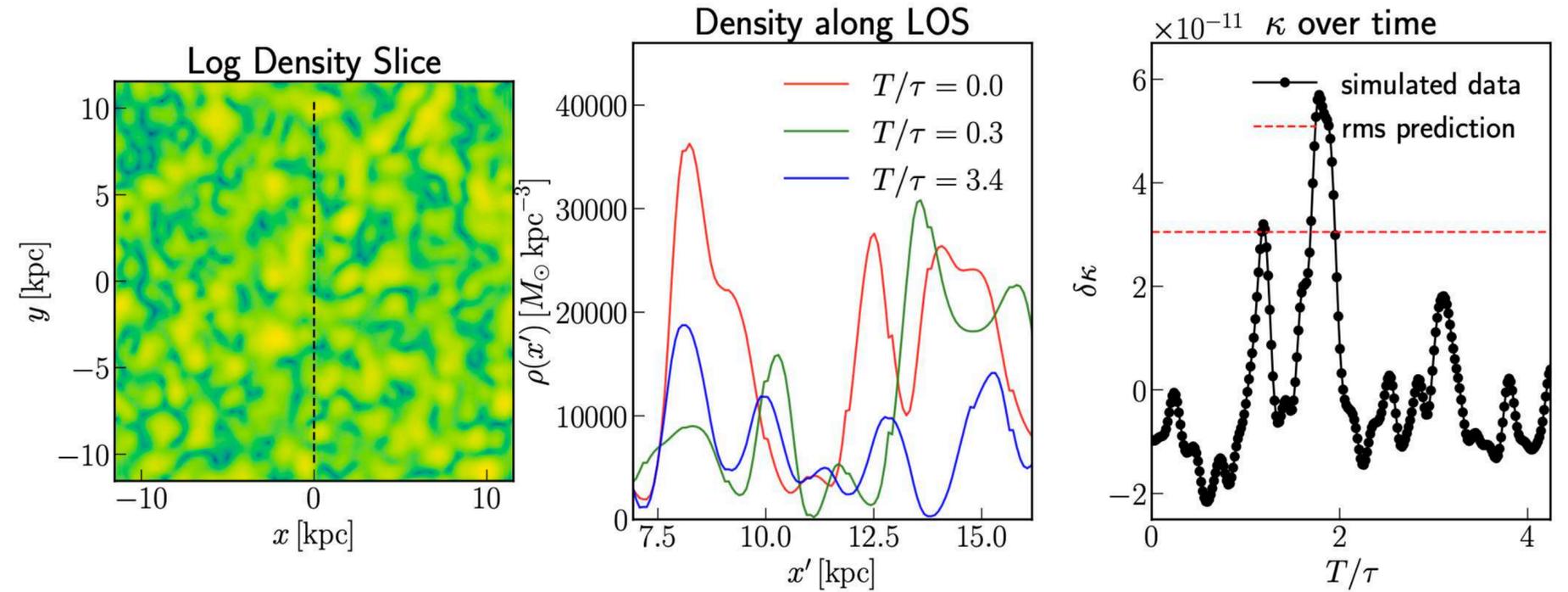
Stochastic lensing

Andrew Eberhardt, Wentao Lui, Yin Li
and Shurui Lin, 2025

Granules

$$\sim \mathcal{O}(10^{-17}) \text{ eV}$$

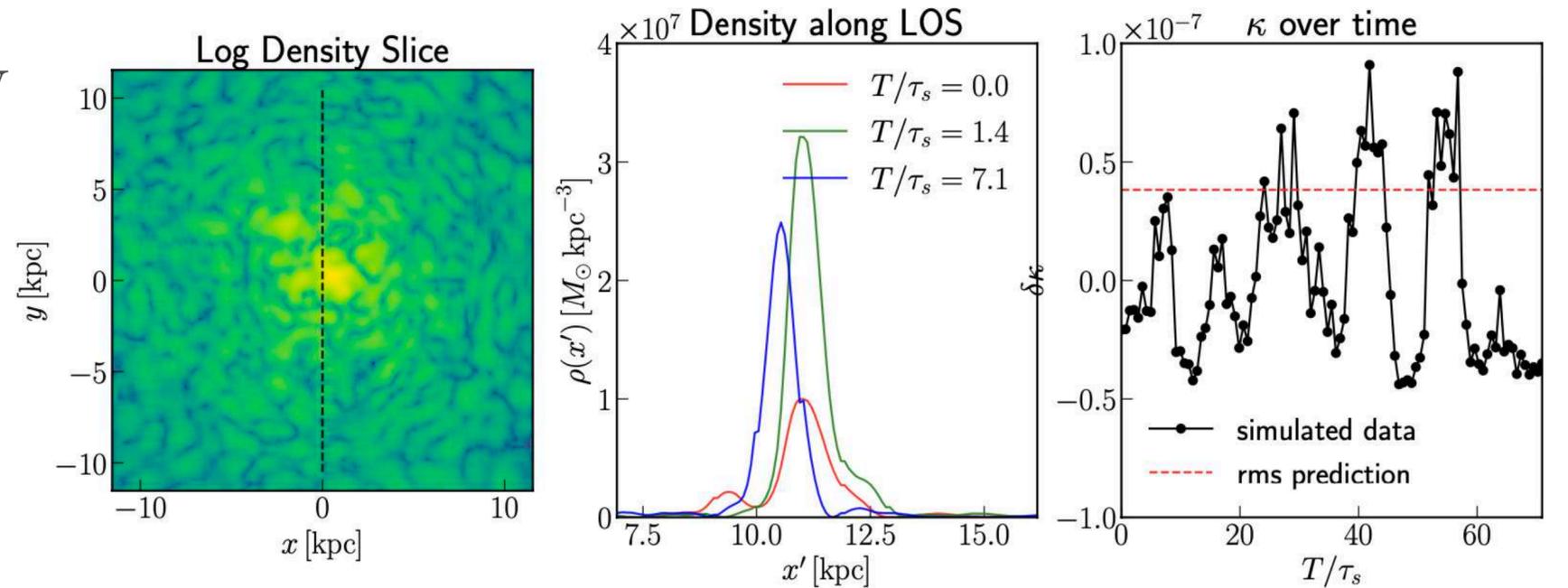
$$\delta\kappa_{\text{rms}}^{\text{gr}} \sim 3 \times 10^{-12} \left(\frac{m}{10^{-17} \text{ eV}} \right)^{-1/2} \left(\frac{\sigma}{200 \text{ km/s}} \right)^{-1/2} \times \left(\frac{\rho}{10^7 M_{\odot}/\text{kpc}^3} \right) \left(\frac{D}{\text{kpc}} \right)^{3/4}$$

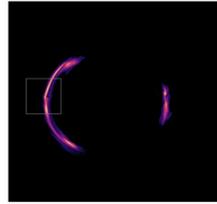


Soliton oscillation

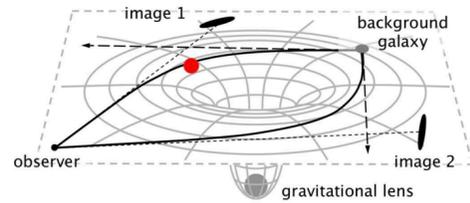
$$\sim \mathcal{O}(10^{-23} - 10^{-22}) \text{ eV}$$

$$\kappa_{\text{rms}}^{\text{s}} \sim 10^{-8} \left(\frac{m}{10^{-23} \text{ eV}} \right)^{-2} \left(\frac{r_c}{\text{kpc}} \right)^{-3} \left(\frac{D_s(D - D_s)/D}{\text{kpc}} \right)$$





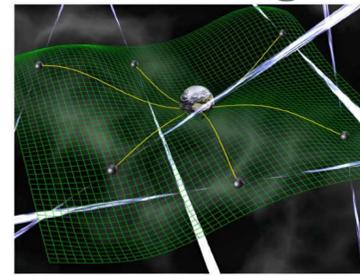
Strong lensing



axion-photon coupling

$$m \sim 10^{-[22-17]} \text{ eV}$$

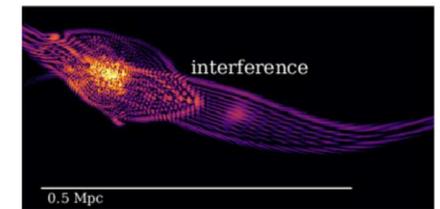
Pulsar Timing Array



Artistic representation of the Pulsar Timing Array concept. Credit: David Champion / MPIFR

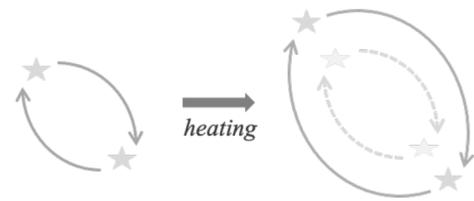
$$m \sim 10^{-[22-17]} \text{ eV}$$

Filaments

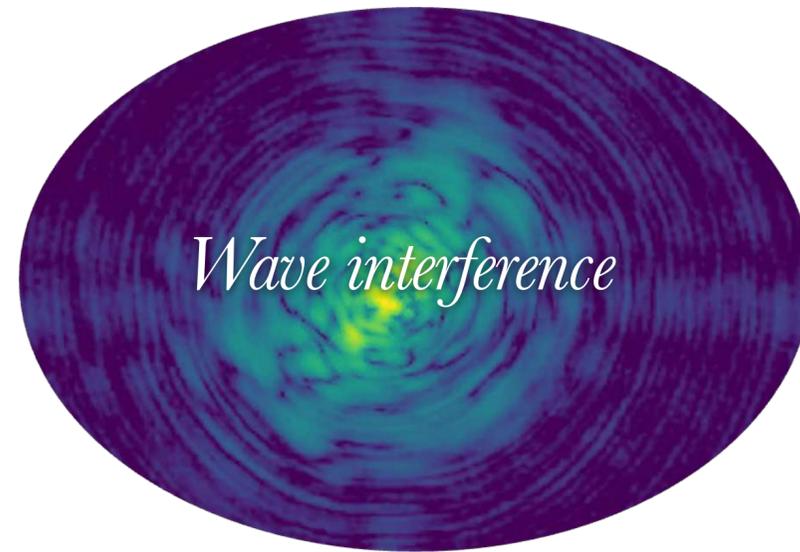


Cosmic filament spin from DM vortices
S. Alexander, C. Capanelli, **EF**, E. McDonough, 2022

Binary stars



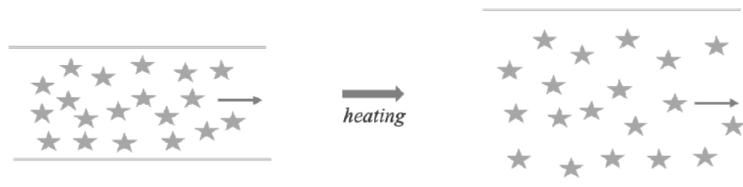
$$m \sim 10^{-[16-10]} \text{ eV}$$



Wave interference

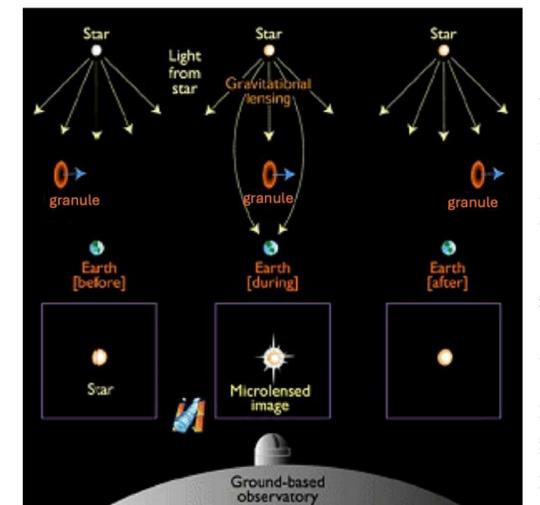
Mass, spin (# particles), fraction self interaction

Stellar streams



$$m \sim 10^{-[23-18]} \text{ eV}$$

Stochastic lensing



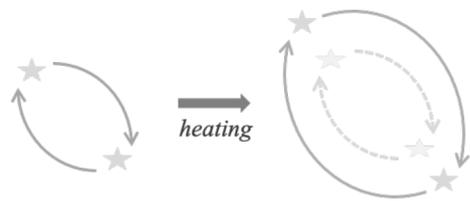
Modified from: <https://i.astro.tsinghua.edu.cn/~smao/contents/microlens.html>

$$m \sim 10^{-[23-18]} \text{ eV}$$

(Work in progress)

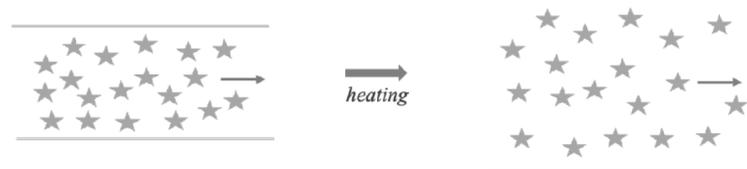
In collaboration with Andrew Eberhardt,
Margot Imbach and Naoki Yoshida

Binary stars



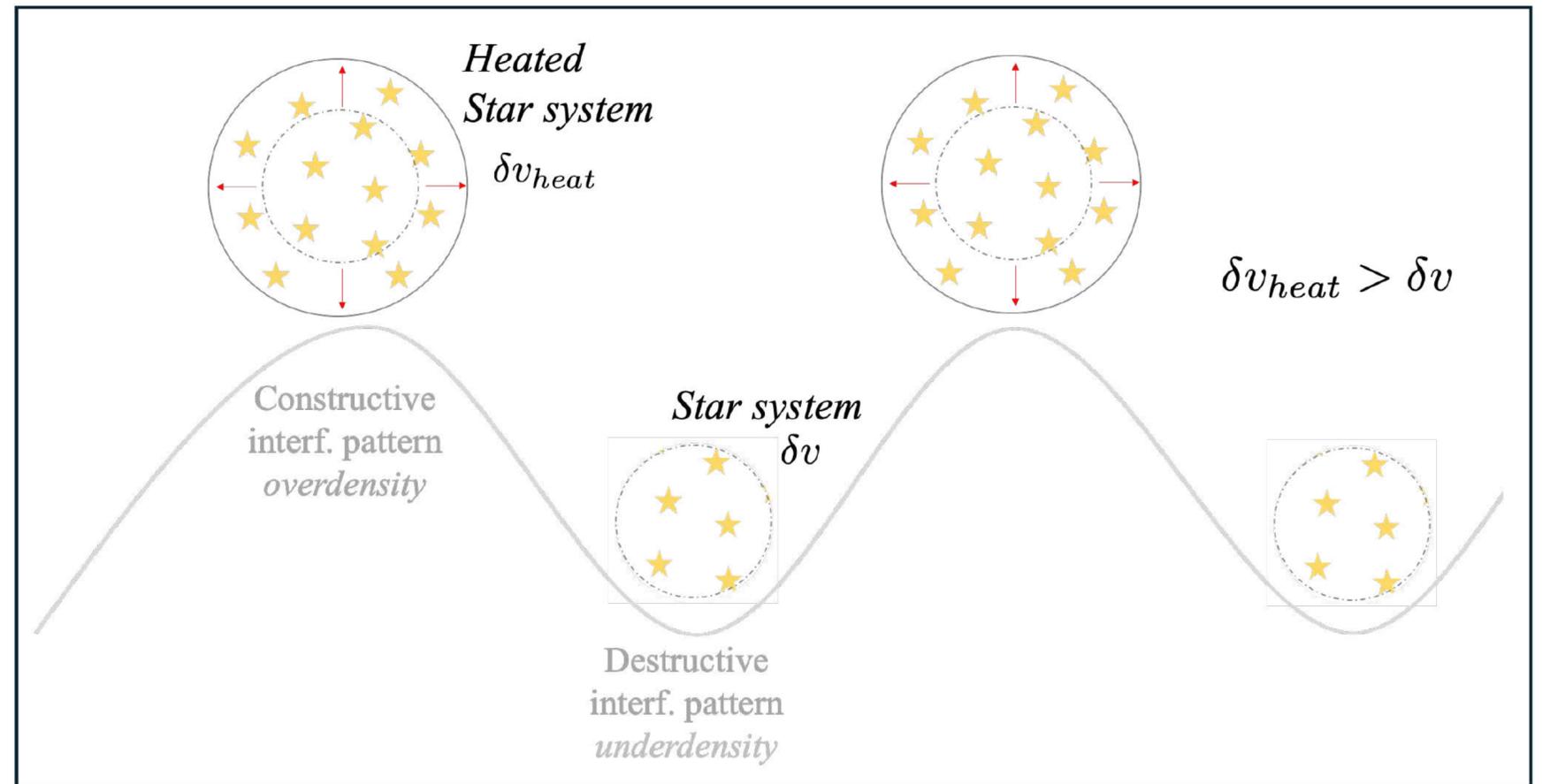
$$m \sim 10^{-[16-10]} \text{ eV}$$

Stellar streams



$$m \sim 10^{-[23-18]} \text{ eV}$$

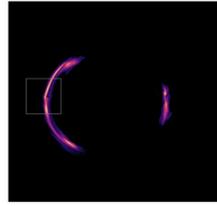
Stellar heating



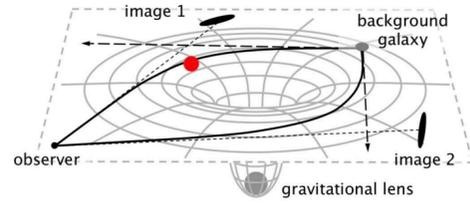
(Work in progress)

In collaboration with Andrew Eberhardt,
and Fabian Schmidt

Preparation for PFS!



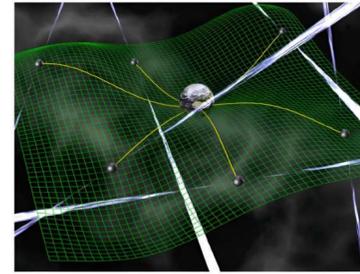
Strong lensing



axion-photon coupling

$$m \sim 10^{-[22-17]} \text{ eV}$$

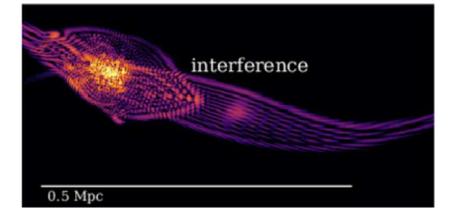
Pulsar Timing Array



Artistic representation of the Pulsar Timing Array concept. Credit: David Champion / MPIFR

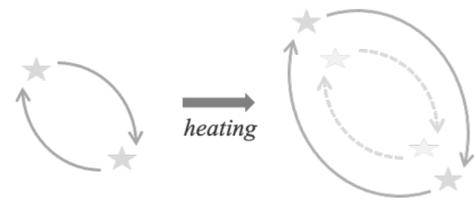
$$m \sim 10^{-[22-17]} \text{ eV}$$

Filaments



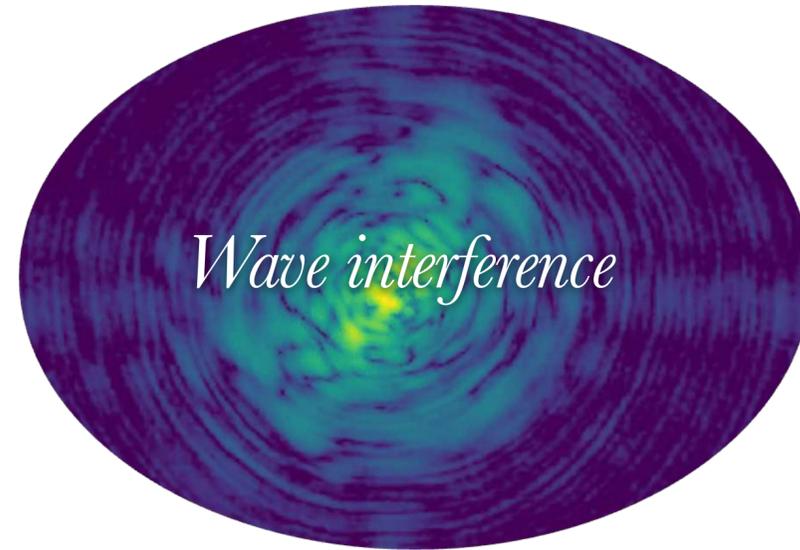
Cosmic filament spin from DM vortices
S. Alexander, C. Capanelli, **EF**, E. McDonough, 2022

Binary stars



$$m \sim 10^{-[16-10]} \text{ eV}$$

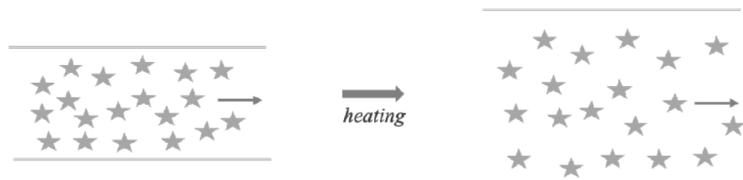
(Work in progress)



Wave interference

Mass, spin (# particles), fraction self interaction

Stellar streams



$$m \sim 10^{-[23-18]} \text{ eV}$$

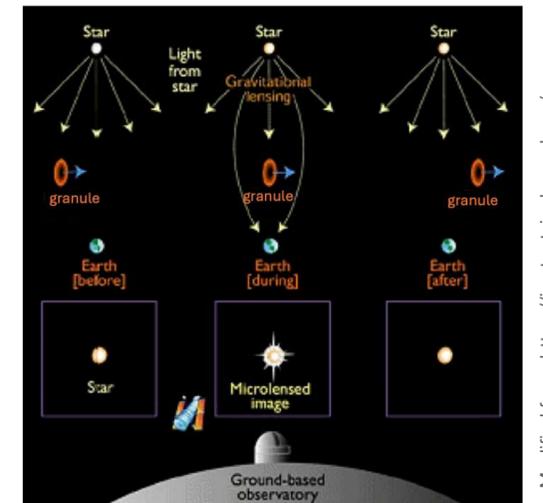
Solar system



$$m \sim 10^{-[16-10]} \text{ eV}$$

axion-photon coupling

Stochastic lensing

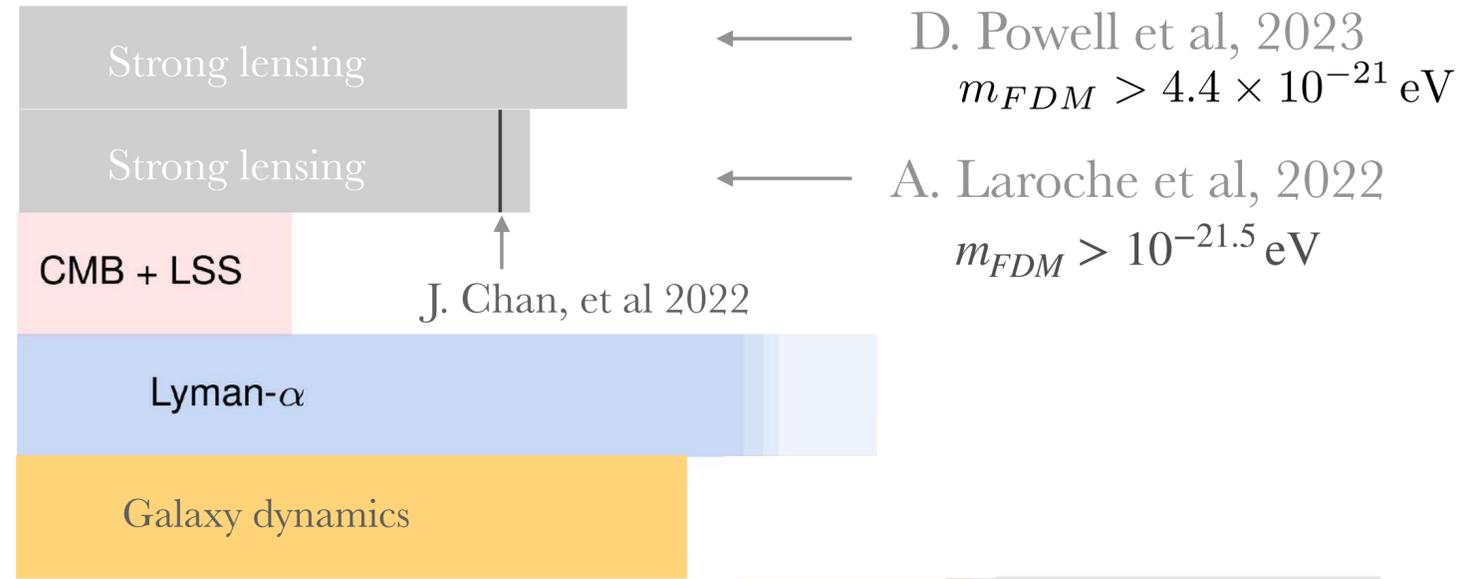
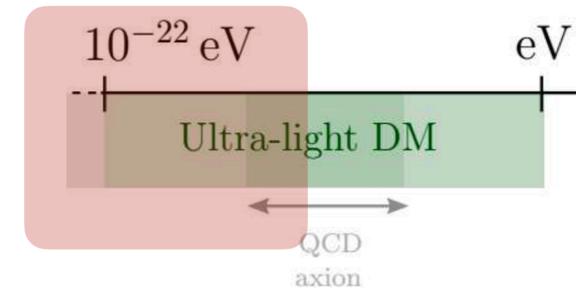


Modified from: <https://i.astro.singhua.edu.cn/~smao/contents/microlens.html>

$$m \sim 10^{-[23-18]} \text{ eV}$$

Interference patterns - granules

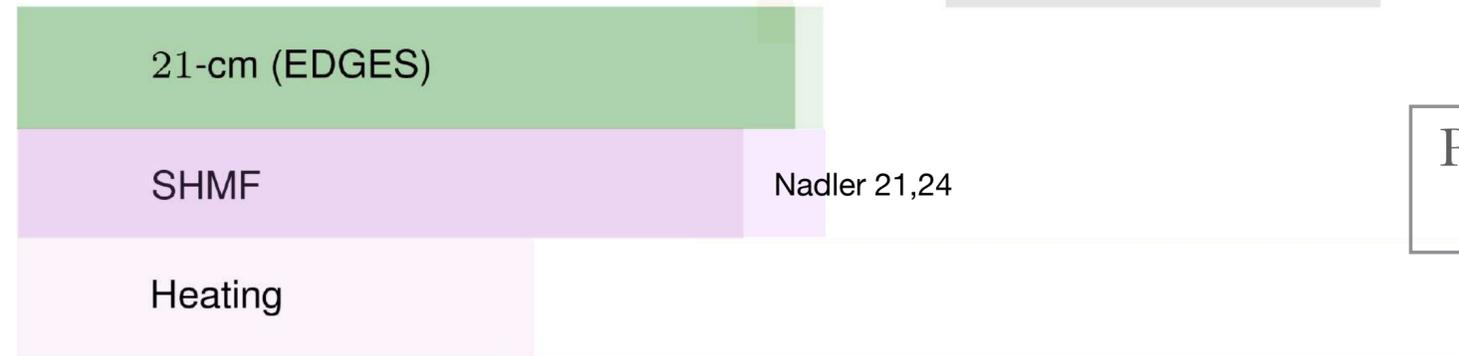
Strong lensing



J. Chan, et al 2022

D. Powell et al, 2023
 $m_{FDM} > 4.4 \times 10^{-21}$ eV

A. Laroche et al, 2022
 $m_{FDM} > 10^{-21.5}$ eV



Nadler 21,24

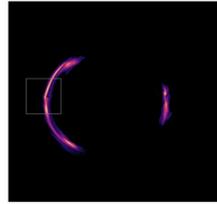
Probing the **fuzziness** on smaller and smaller scales (larger masses) - still wave behavior!

Stellar heating
Dalal et al, 2022
 $m_{FDM} > 3 \times 10^{-19}$ eV

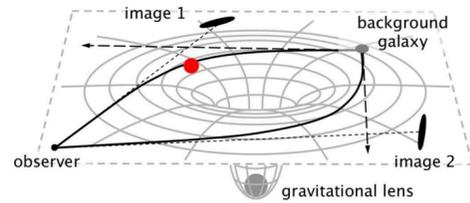


FDM Mass (eV)

10^{-26} 10^{-24} 10^{-22} 10^{-20} 10^{-18} 10^{-16}



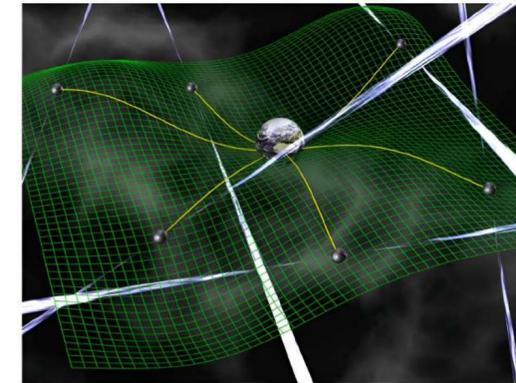
Strong lensing



axion-photon coupling

$$m \sim 10^{-[22-17]} \text{ eV}$$

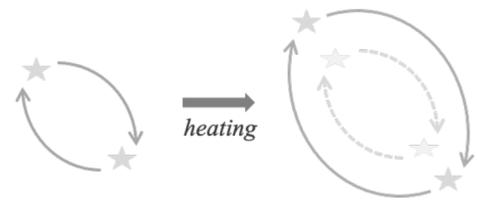
Pulsar Timing Array



Artistic representation of the Pulsar Timing Array concept. Credit: David Champion / MPIfR

$$m \sim 10^{-[22-17]} \text{ eV}$$

Binary stars



$$m \sim 10^{-[16-10]} \text{ eV}$$

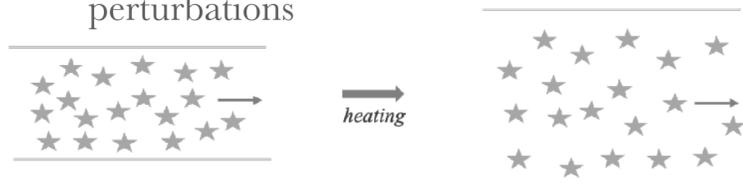


Wave interference

Mass, spin (# particles), fraction self interaction

Stellar streams

Heating + coherent perturbations



$$m \sim 10^{-[23-18]} \text{ eV}$$

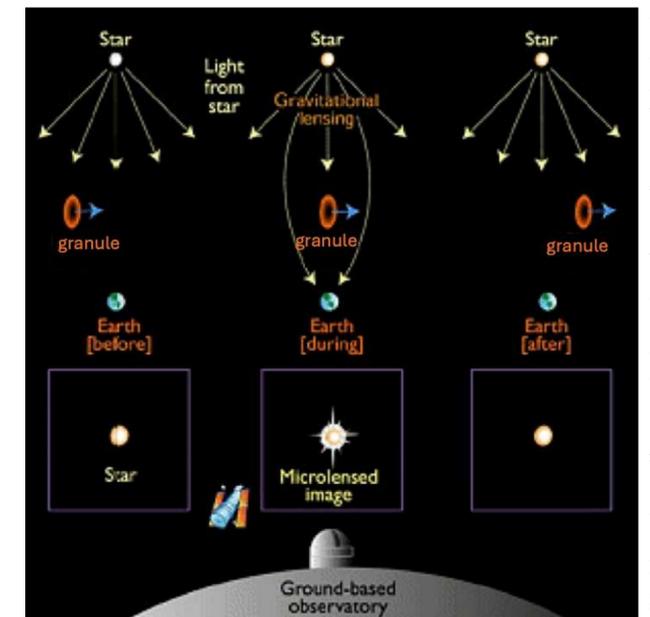
Solar system



$$m \sim 10^{-[16-10]} \text{ eV}$$

axion-photon coupling

Stochastic lensing



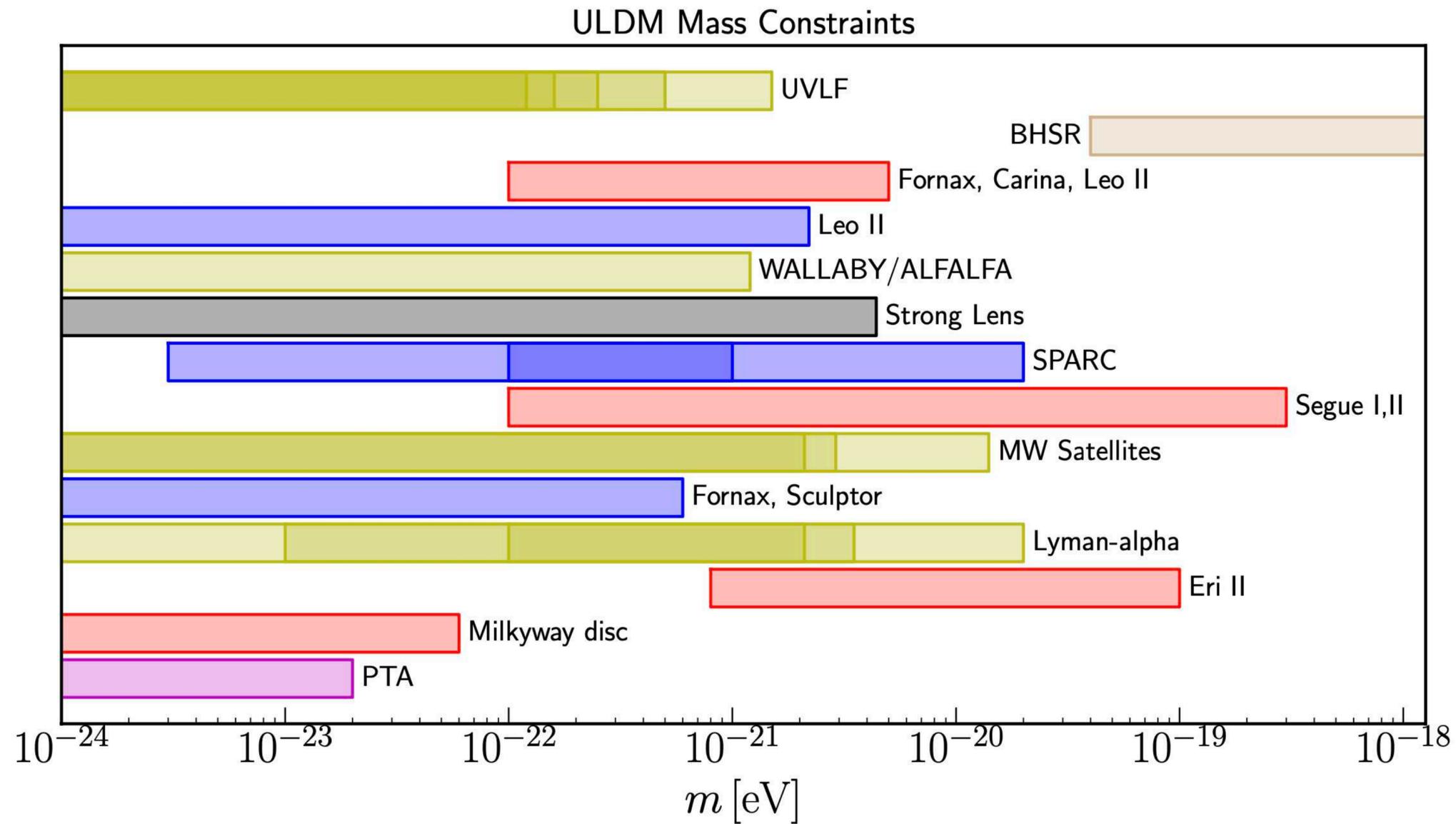
$$m \sim 10^{-[23-18]} \text{ eV}$$

Modified from: <https://i.astro.tsinghua.edu.cn/~smao/contents/microlens.html>

Current status

Fuzzy Dark Matter - bounds on the mass

Review: Eberhardt, EF (to appear)

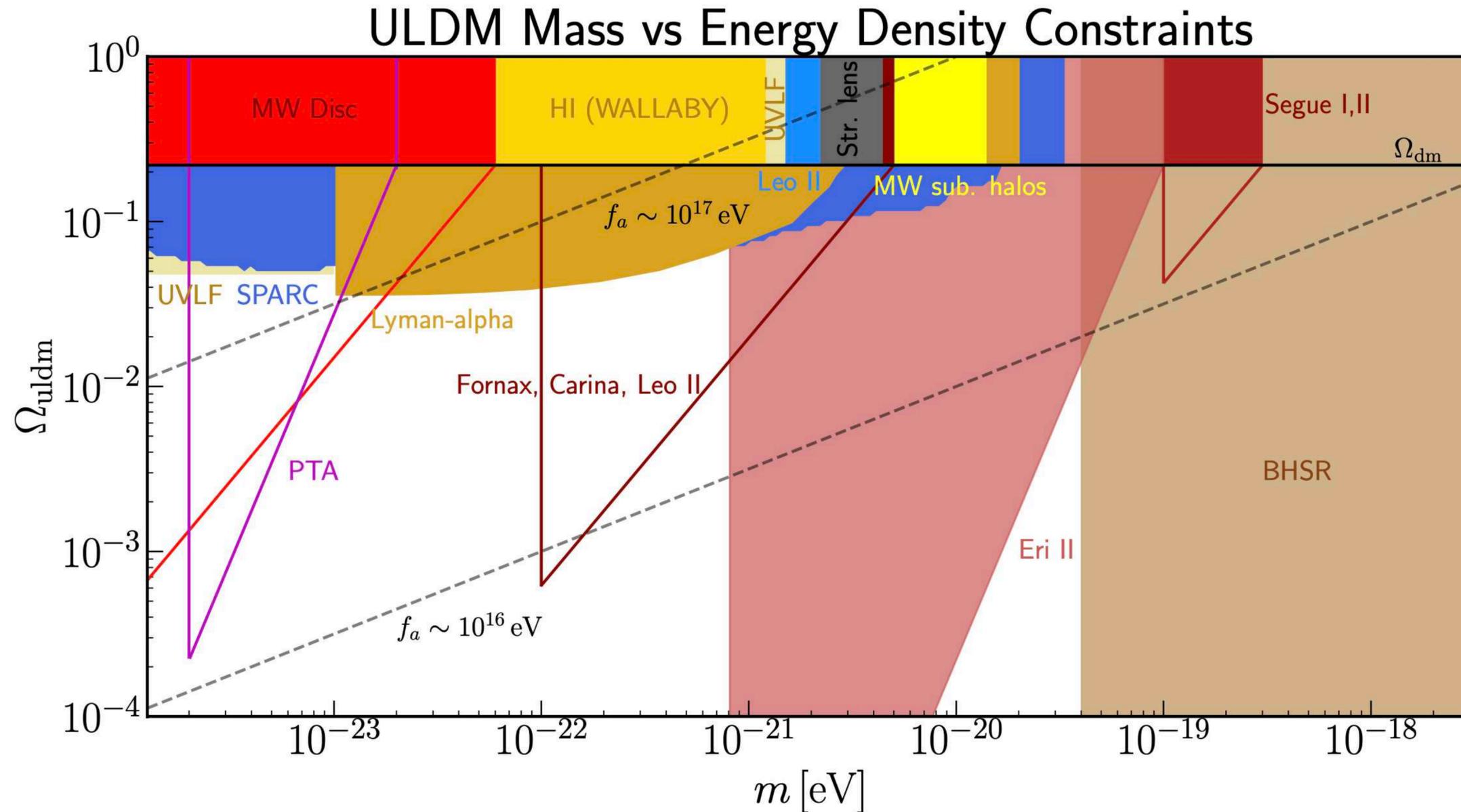


Bounds depend on assumptions,
simplifications, simulations, ...
And can be conservative or best case scenario.
Systematic effects!
Careful when interpreting them!

Current status

Fuzzy Dark Matter - bounds on the mass

Review: Eberhardt, EF (to appear)

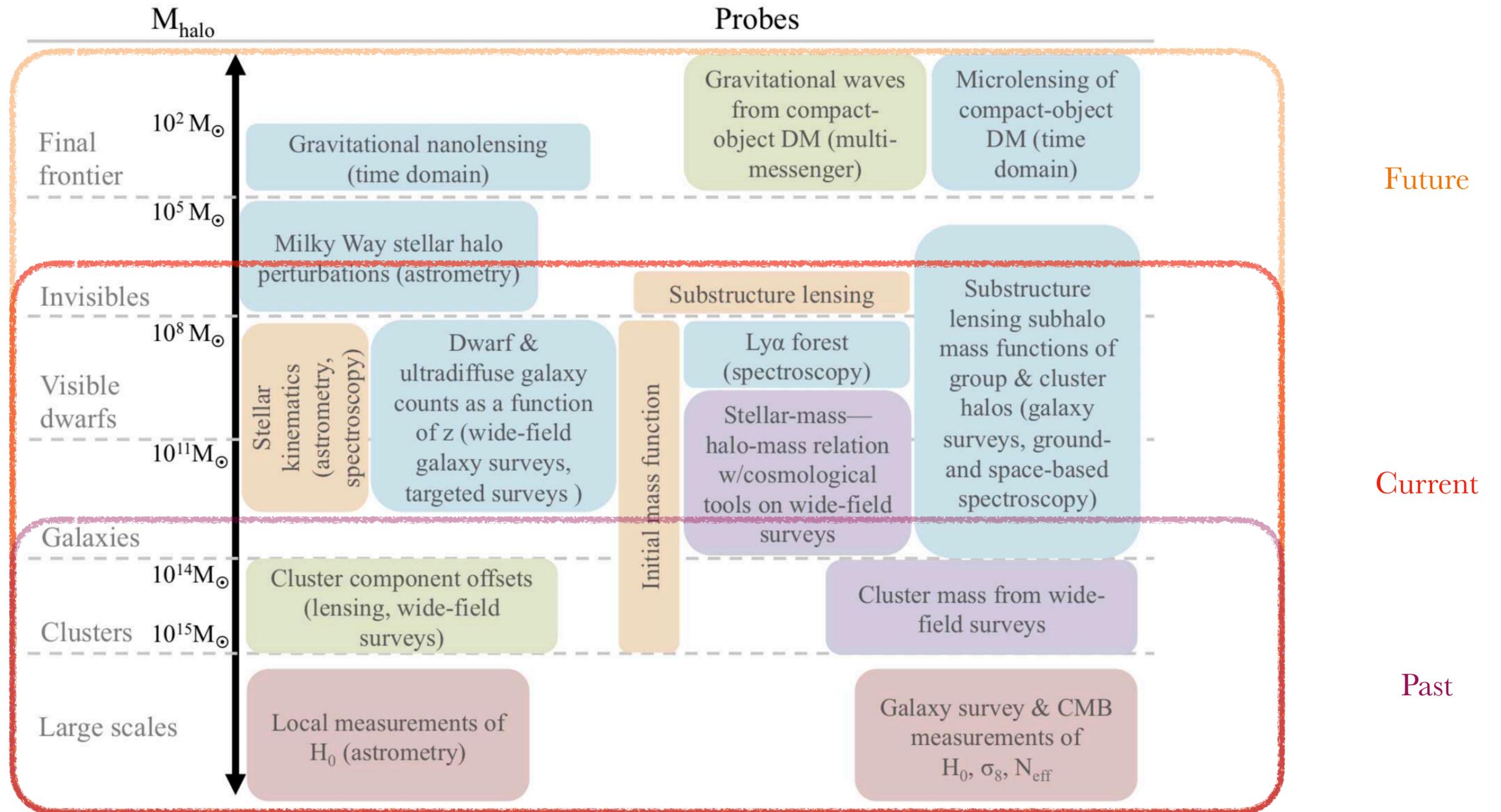


Much more:

- ULDM not 100%
- Multiple axions
- Add self-interaction
- Couplings
- Spin

*The search for **dark matter (ULDM)** is a
multi-probe/multi-scale endeavour...*

Small scales can offer some *hints* of the nature of DM



*The search for **dark matter (ULDM)** is a
multi-probe/multi-scale endeavour...*

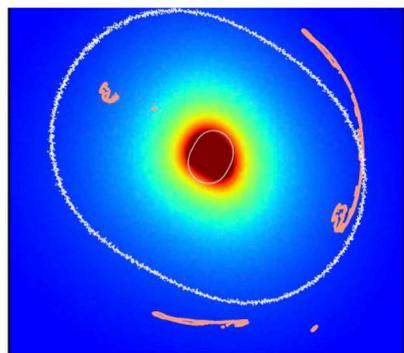
*exciting times for **axion dark matter***

Summary

Ultra-Light Dark Matter

Well motivated DM models
Rich and distinct phenomenology on small scales
Testable prediction

Granules



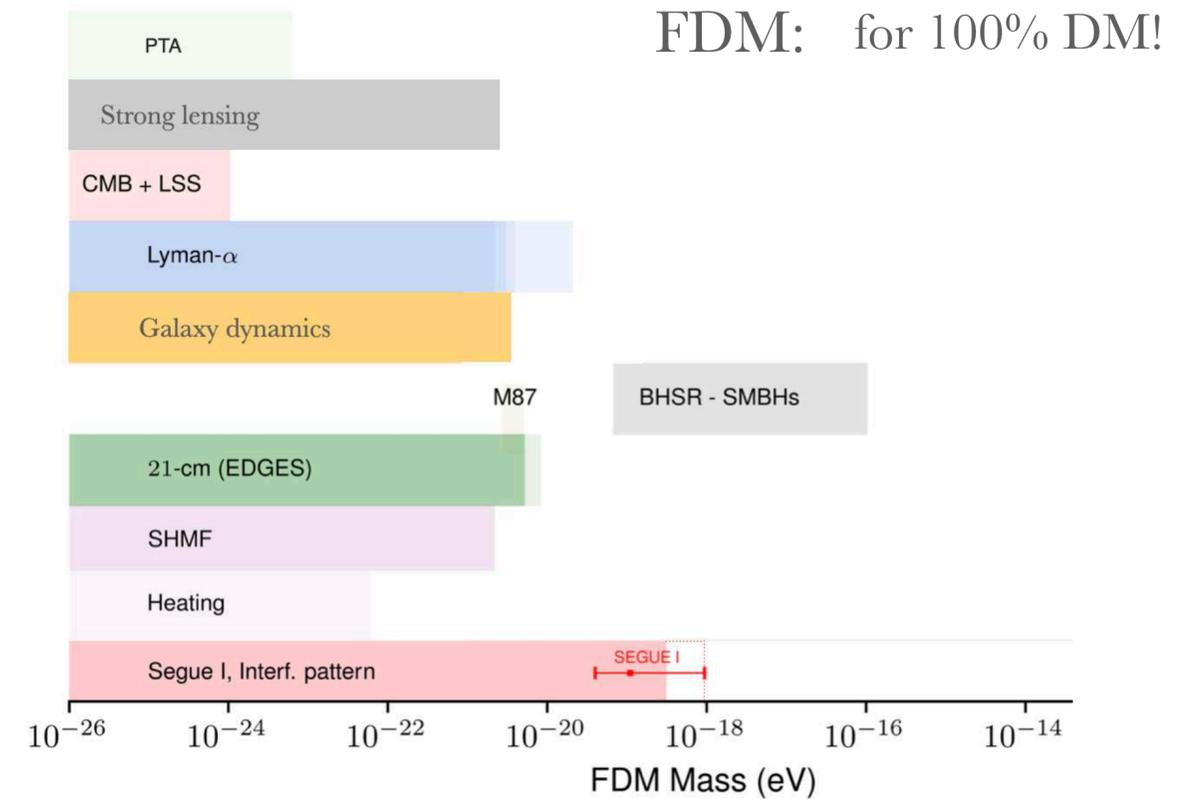
Strong lensing:

$$m_{\text{fdm}} > 4.4 \times 10^{-21} \text{ eV}$$

$$m_{\text{vdm}} > 1.4 \times 10^{-21} \text{ eV}$$

Heating: $m_{\text{FDM}} > 3 \times 10^{-19} \text{ eV}$

Current status



Future

Observations

Improve in simulations
New probes/observables



Thank you!